# A new observable for $m_W$ determination at the LHC

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Based on 2301.04059 in collaboration with A. Vicini, P. Torrielli



The discovery of the Higgs boson and the measurement of its mass allow for the prediction of the W mass with high precision

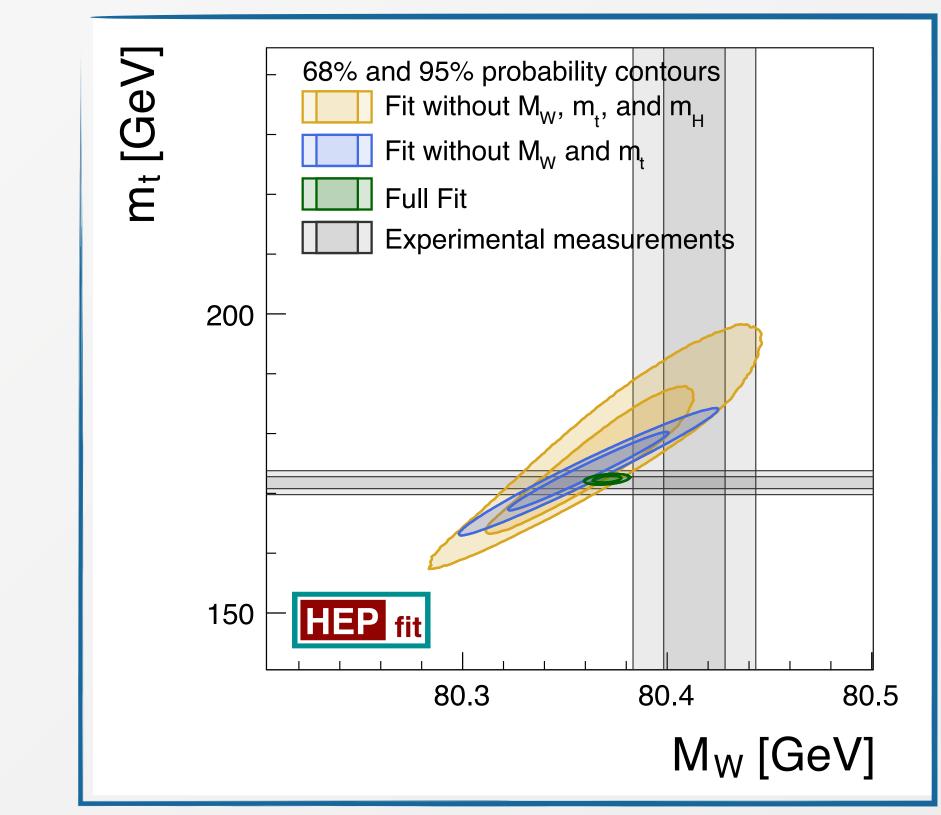
 $m_W = 80.350 \pm 8 \,\mathrm{GeV}$ 

Which is in a  $2\sigma$  agreement with the experimental average (pre-CDF II)

 $m_W = 80.385 \pm 15 \,\mathrm{GeV}$ 







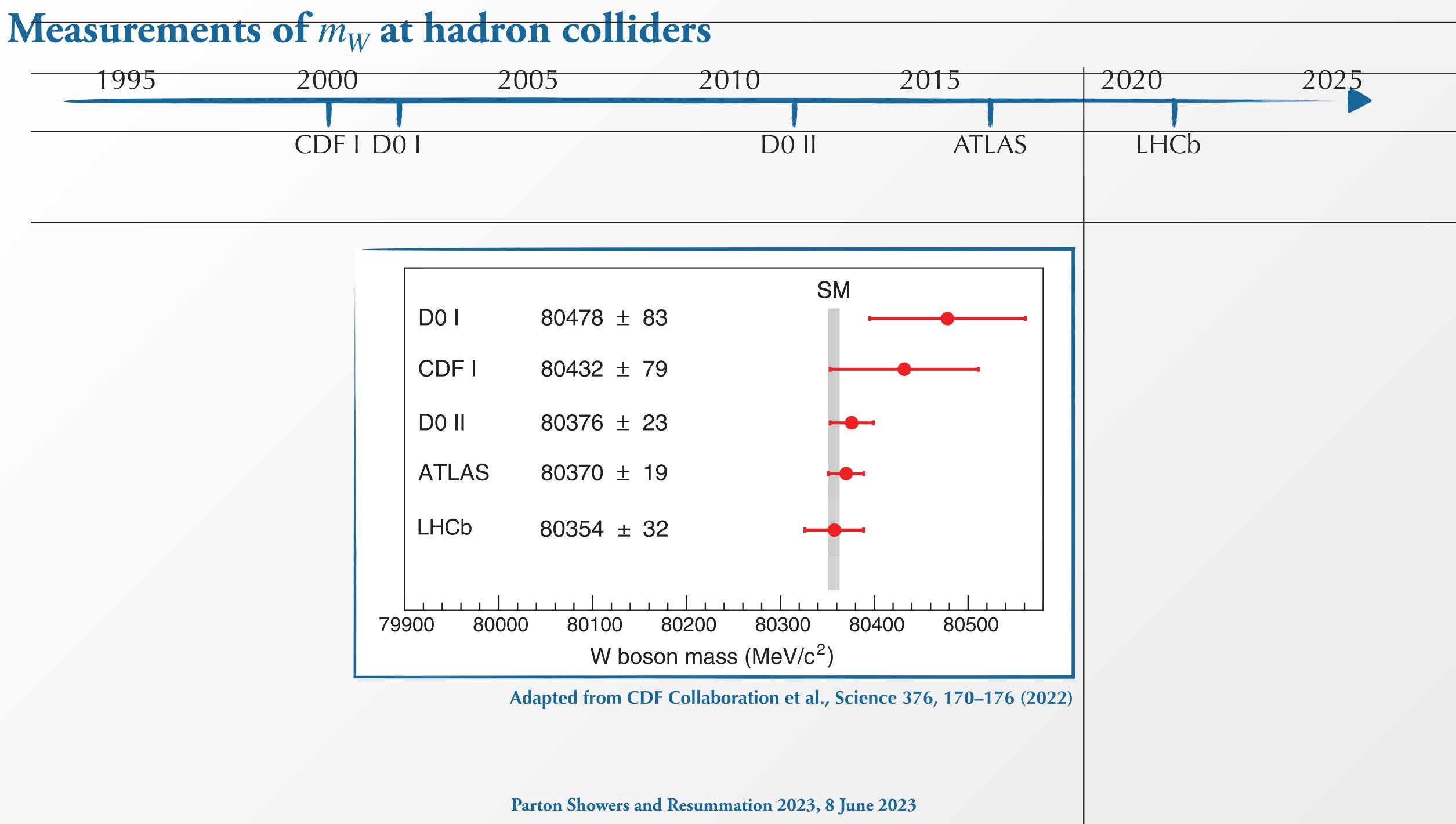
[de Blas, Pierini, Reina, Silvestrini '22]

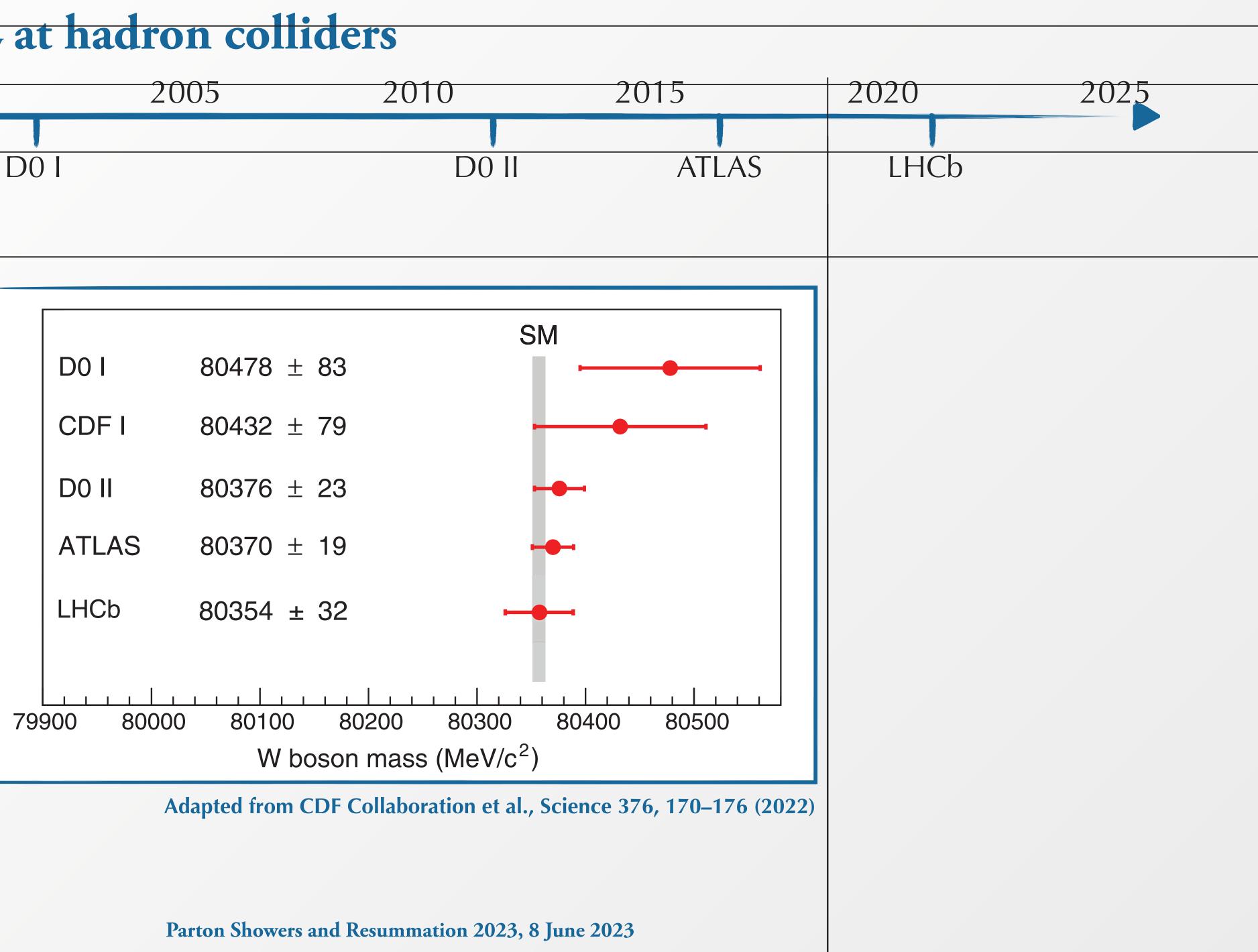




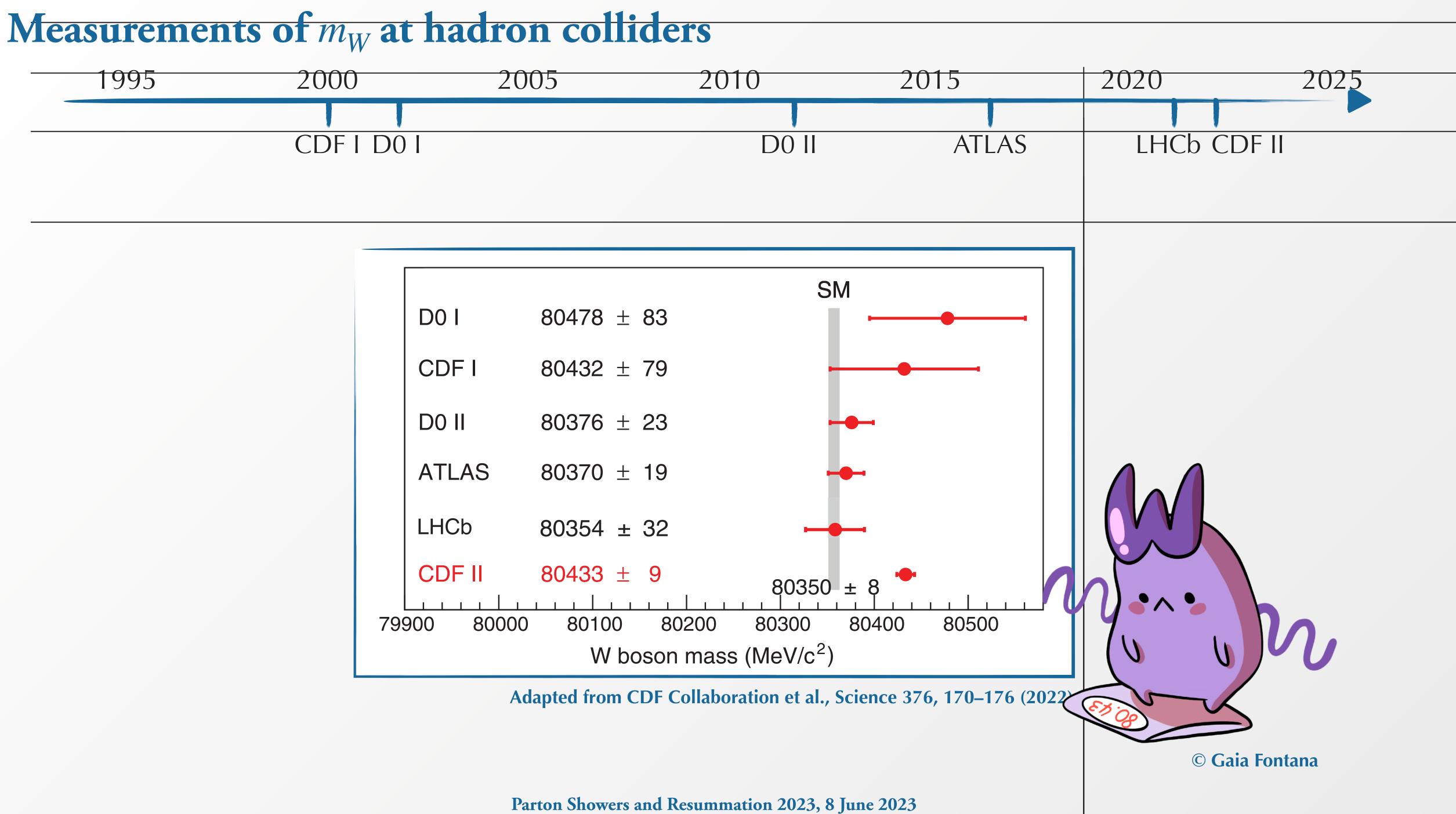
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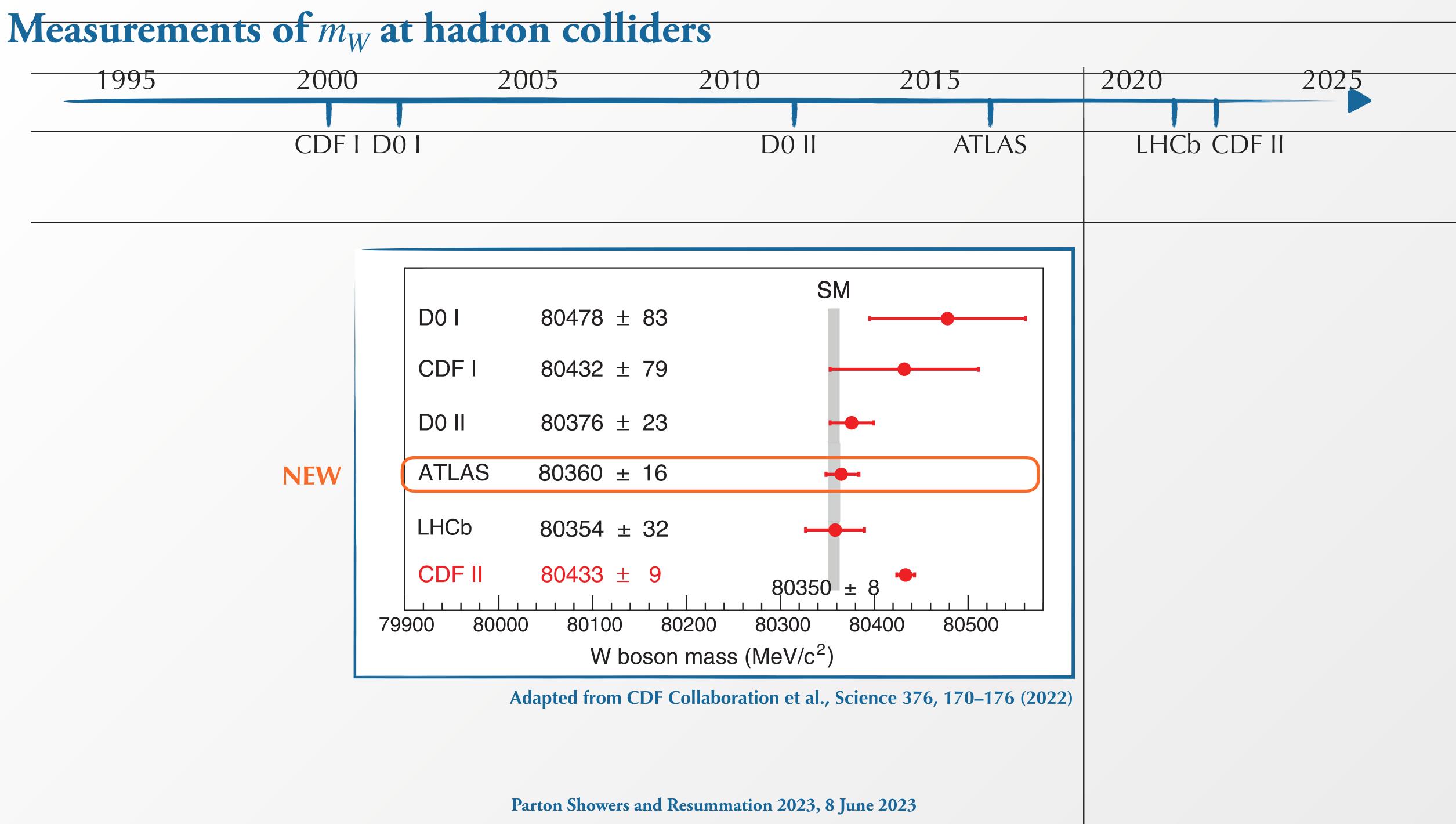


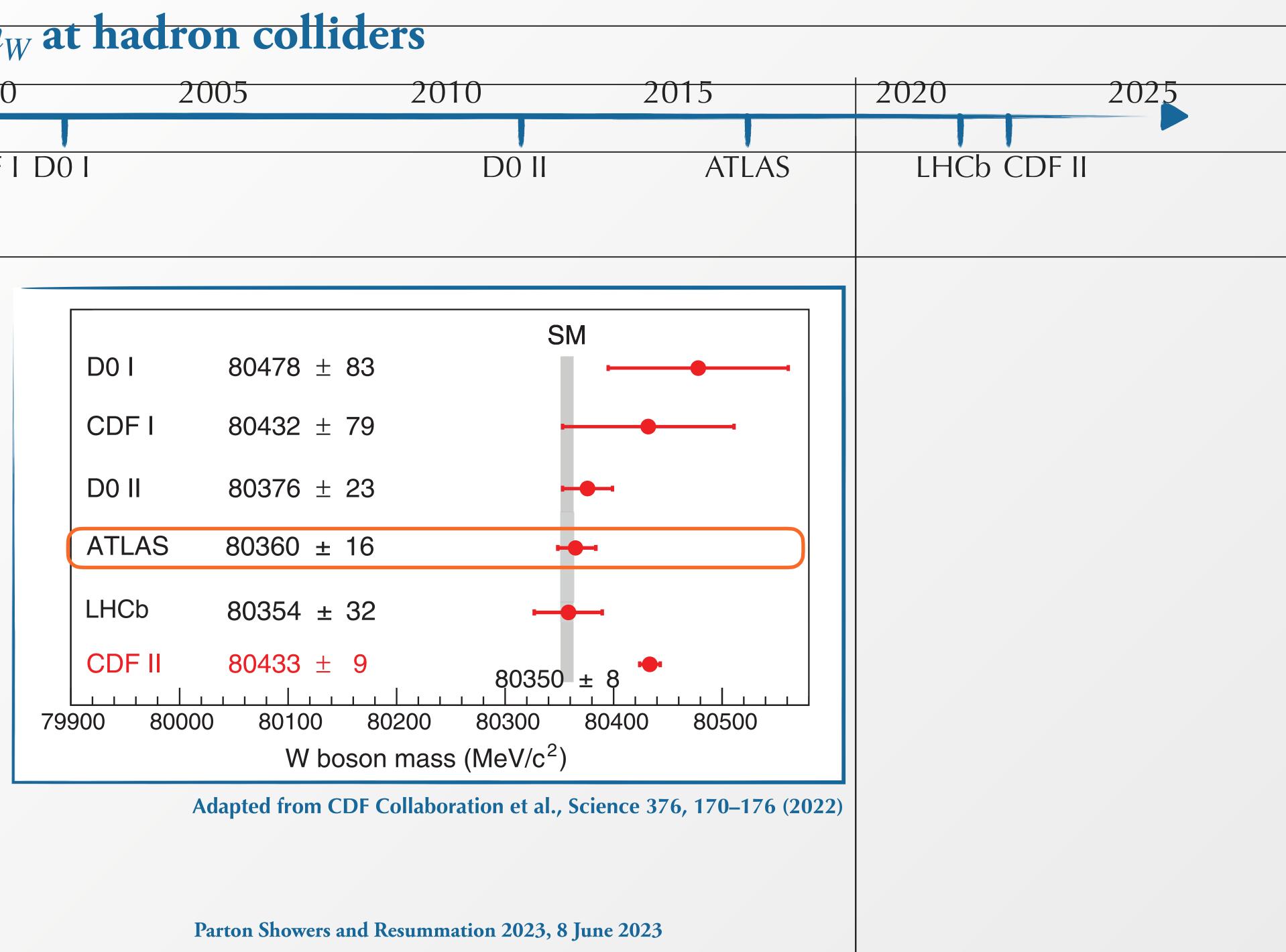




	D0 I	80478 ± 83
	CDF I	80432 ± 79
	D0 II	80376 ± 23
	ATLAS	80370 ± 19
	LHCb	80354 ± 32
	CDF II	80433 ± 9
70		
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#### Outline

- The Drell-Yan kinematical distributions and the  $m_W$  determination: strategy and challenges
- Recent progress in theoretical computations
- Proposal of a new observable and discussion of the associated theory uncertainties

Full kinematics of **charged DY production** is not accessible at hadron colliders; in particular, the invariant mass of the neutrino-lepton pair cannot be reconstructed

Reconstruction possible in the transverse plane (requires precise measurement of the hadronic recoil) such as the lepton transverse momentum  $p_T^{\ell}$  or the transverse mass  $m_T = \sqrt{2p_T^{\ell}p_T^{\nu}(1 - \cos \Delta \phi_{\ell\nu})}$ 

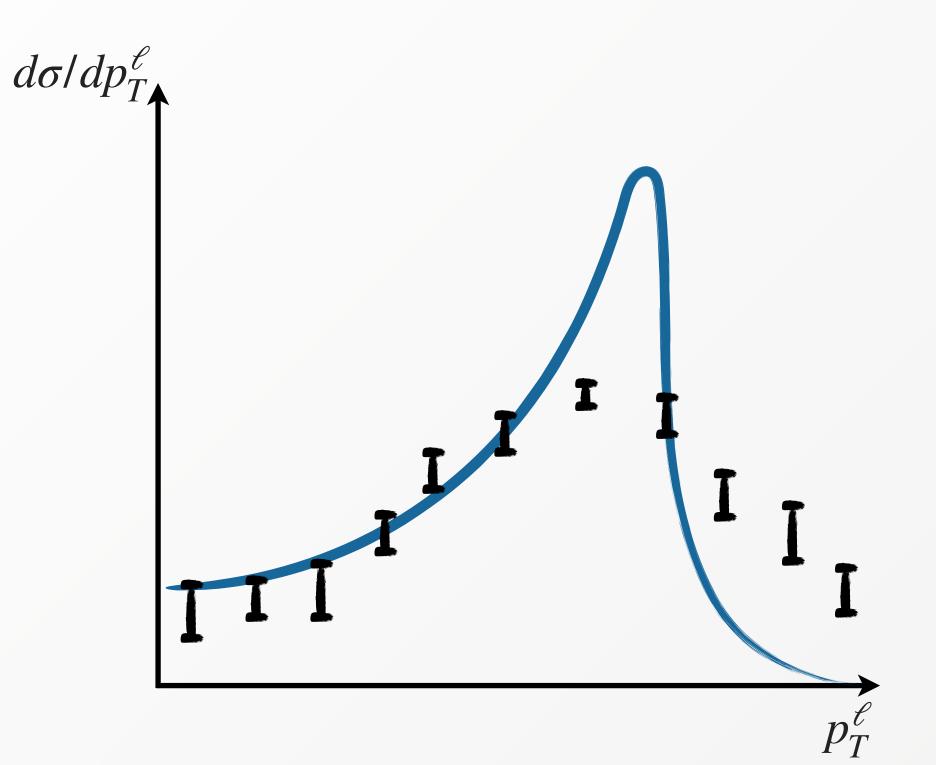
$$\frac{d\sigma}{d|p_T^{\ell}|^2} \sim \frac{1}{\sqrt{1 - 4\frac{|p_T^{\ell}|^2}{\hat{s}}}} \sim \frac{1}{\sqrt{1 - 4\frac{|p_T^{\ell}|^2}{m_W^2}}} \qquad \text{Jacobian peak at } p_T^{\ell} \sim m_W/2$$

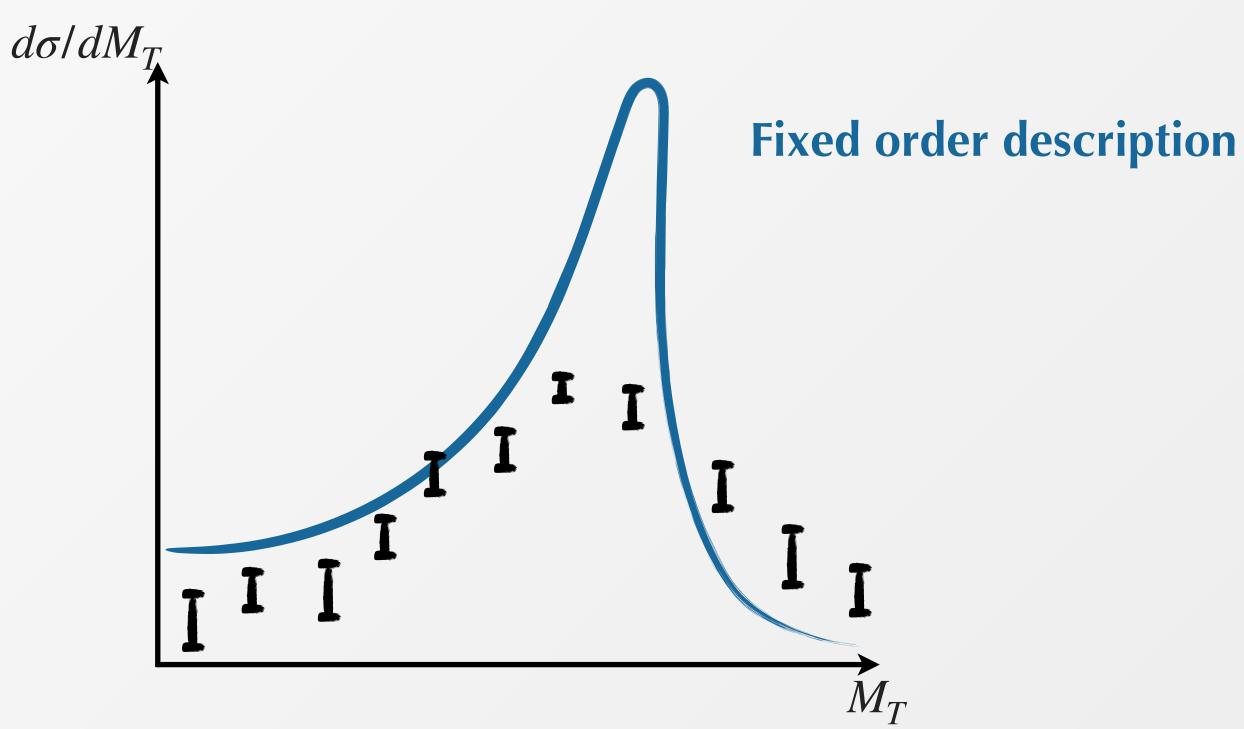
Enhanced sensitivity to  $m_W$  in both distributions at the  $\mathcal{O}(10^{-3}) - \mathcal{O}(10^{-2})$  level.

Precise determinations of the W mass exploit observables with high sensitivity to small variations  $\mathcal{O}(10^{-4})$  of  $m_W$ ,



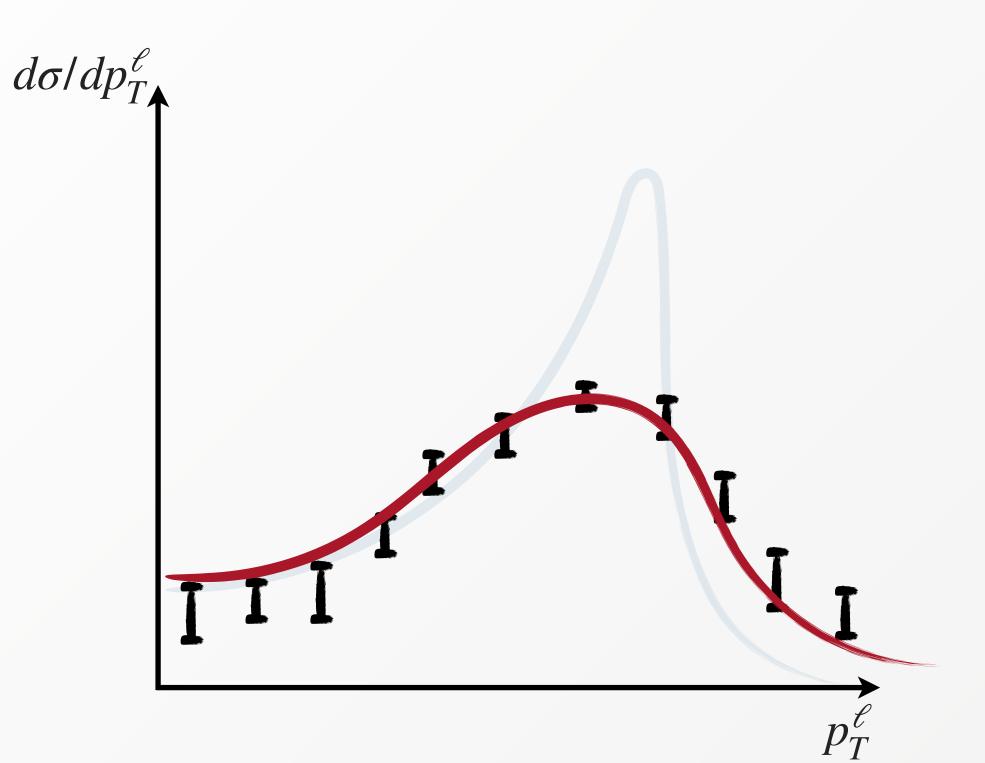
Different sensitivity to experimental uncertainties and quality of theoretical modelling





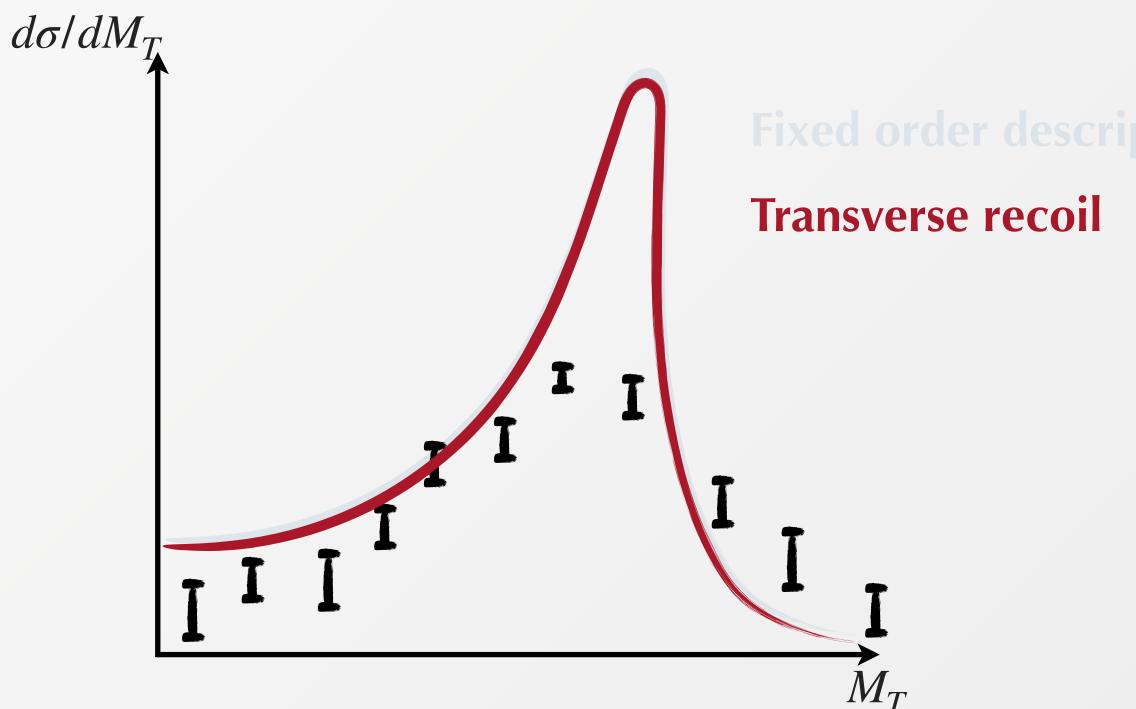


Different sensitivity to experimental uncertainties and quality of theoretical modelling

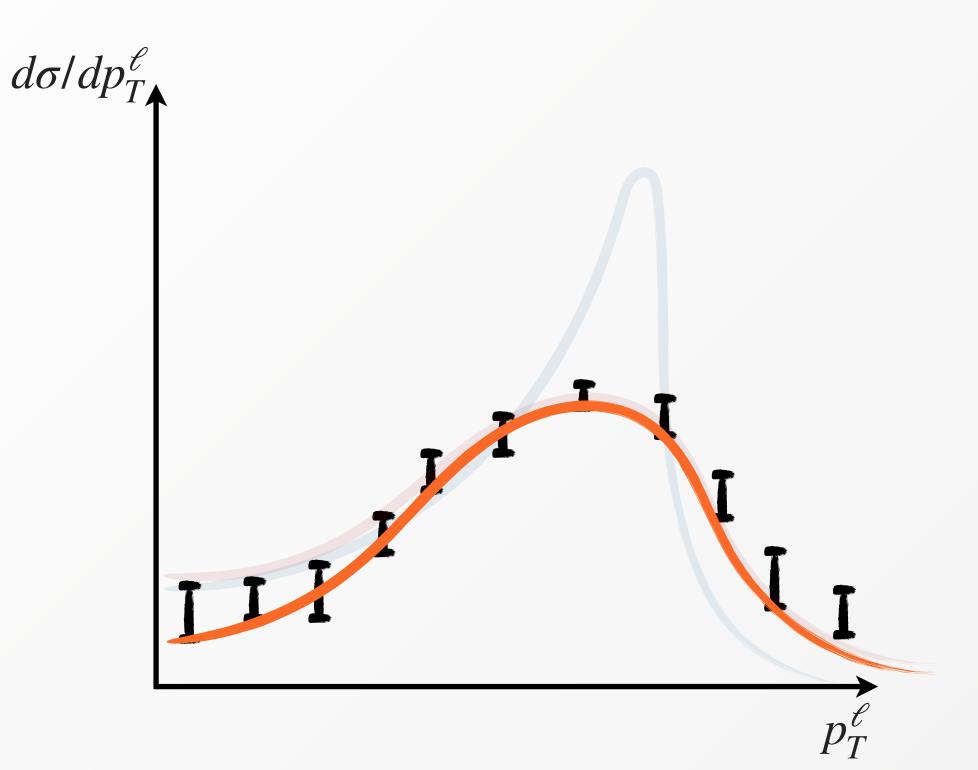


Description of the data requires:

Modelling of IS QCD + FS QED radiation

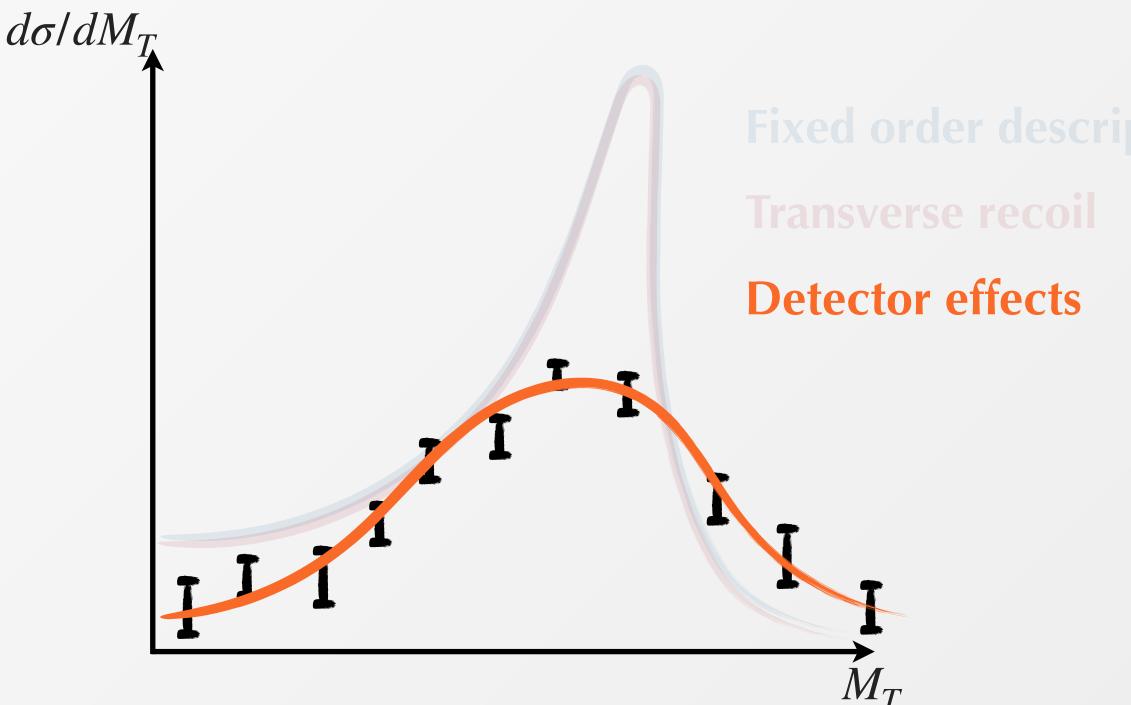


Different sensitivity to experimental uncertainties and quality of theoretical modelling



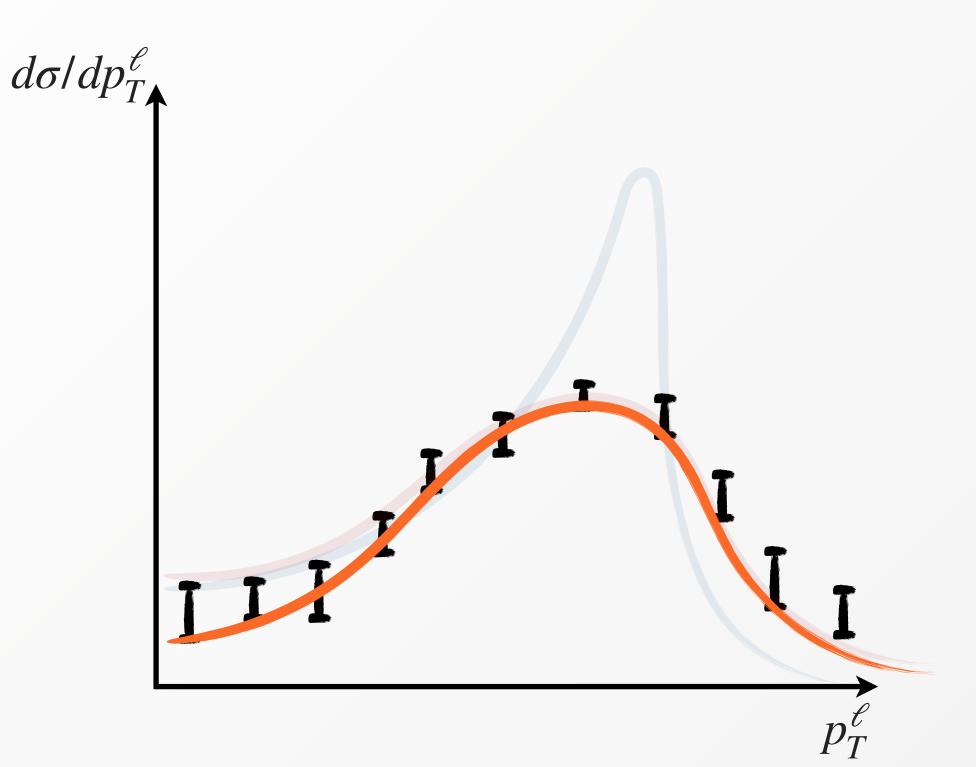
Description of the data requires:

- Modelling of **IS QCD + FS QED radiation**



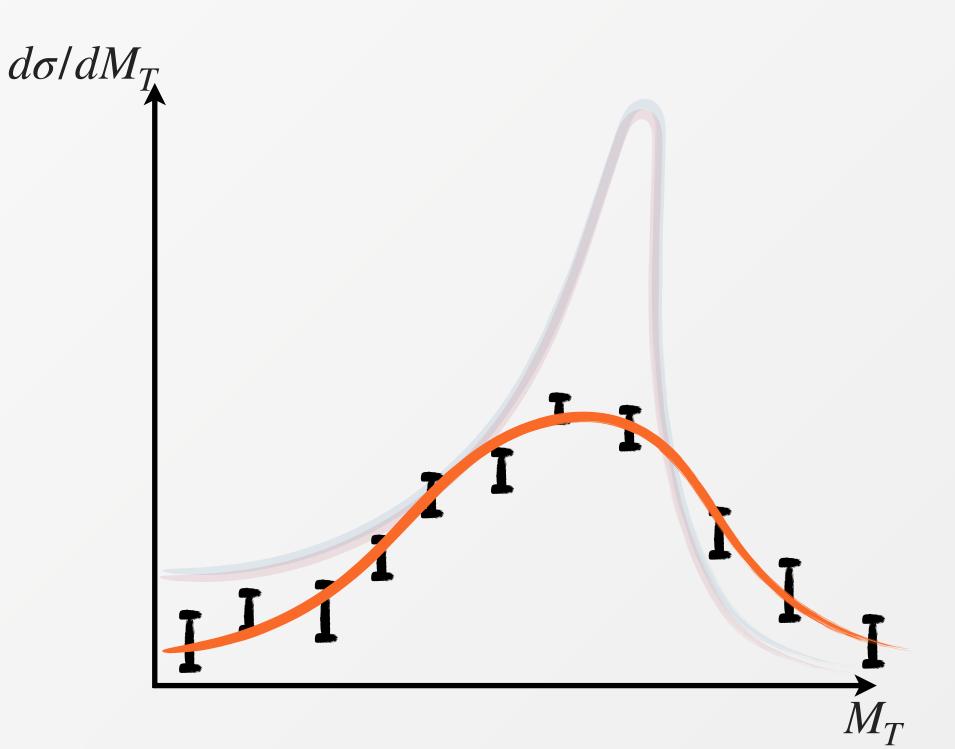
• Modelling of the smearing of the distributions due to the reconstruction of the neutrino in the transverse plane

Different sensitivity to experimental uncertainties and quality of theoretical modelling



#### Mostly QCD + QED radiation

Parton Showers and Resummation 2023, 8 June 2023



#### Mostly **detector effects**

$$m_T = \sqrt{2p_T^{\ell} p_T^{\nu} (1 - \cos \Delta \phi_{\ell\nu})}$$

Requires precise determination of the neutrino transverse momentum: **challenging at the LHC** due to worse control of the hadronic recoil 2023, 8 June 2023

## Measurements of $m_W$ at hadron colliders: template fitting

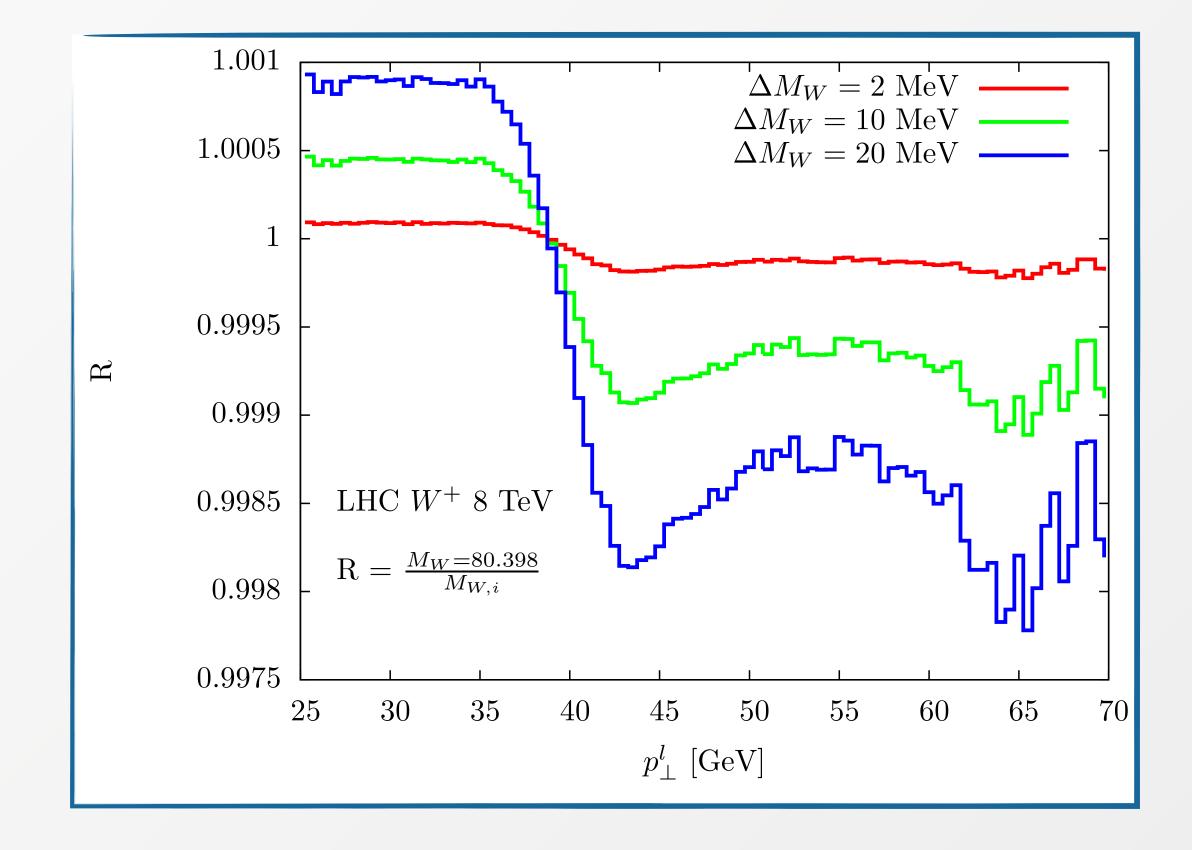
Extraction of  $m_W$  performed by template fittings of relevant kinematic observables e.g. lepton transverse momentum  $p_{\perp}^{\ell}$ 

- Compute theoretical distributions for different values of  $m_W^{(k)}$
- 2. For each hypothesis, compute a figure of merit  $\chi_k^2$  for a defined window in  $p_{\perp}^{\ell} m_W$
- 3. The minimum value of  $\chi_k^2$  defines the experimental value of  $m_W$

Permille-level control of the shape is necessary to obtain  $m_W$  with 10<sup>-4</sup> precision

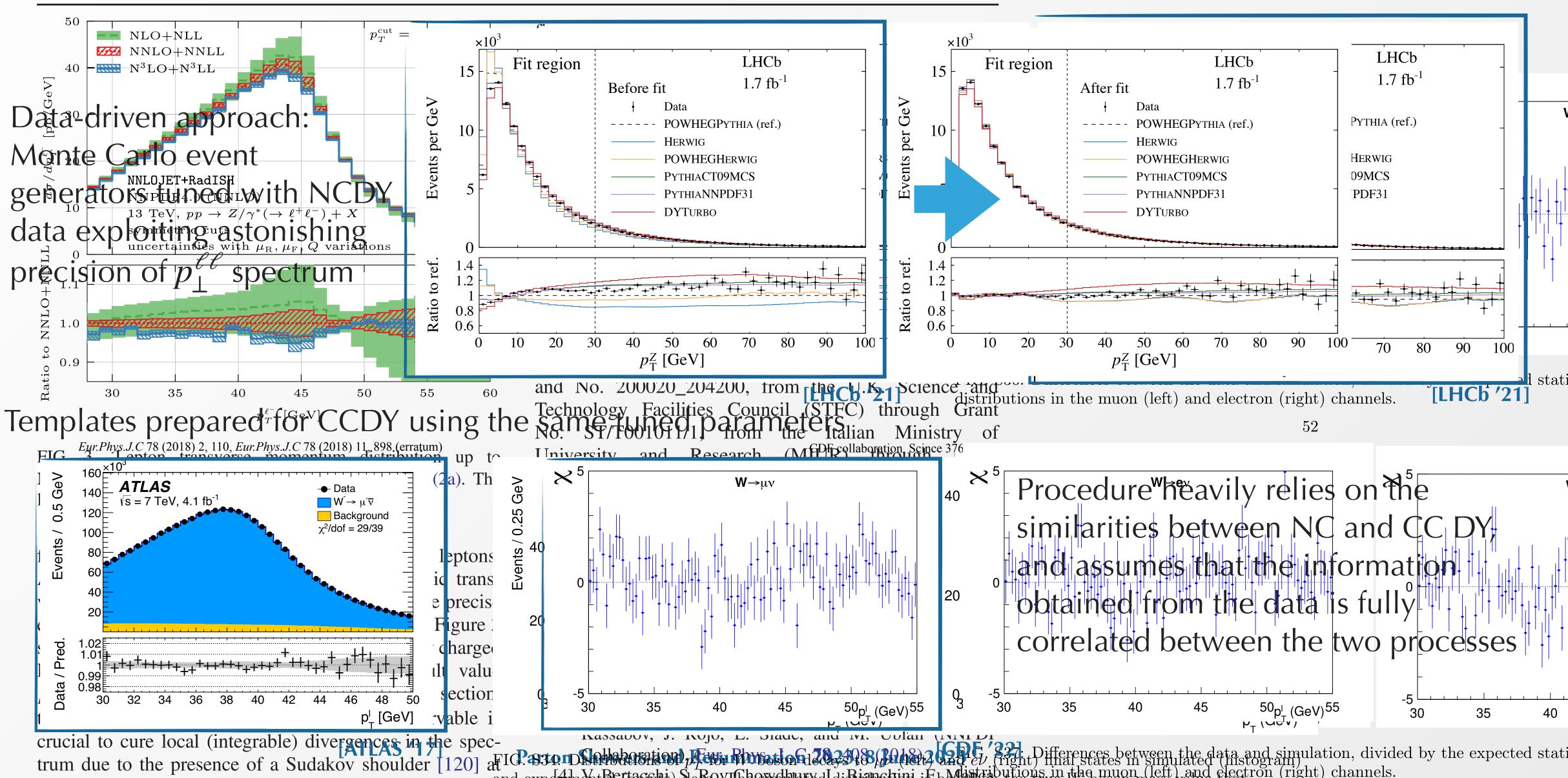
#### The **description of experimental data** plays a crucial role

Precise control of the associated theoretical uncertainties needed to assess the theoretical systematic error on m<sub>W</sub>



### Template fitting and tuning

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## Template fitting procedure requires that the theoretical distribution can describe the data with high quality

### Template fits and their limitations

- Possible that BSM effects are absorbed in the tuning
- acceptances, different phase spaces, different QED corrections, PDFs and heavy quark effects...)
- Tuning performed at the level of the  $p_{\perp}^{\ell\ell}$  spectrum: uncertainty related to the transfer of information to other kinematic distribution in W production  $(p_{\perp}^{\ell}, M_{\perp}^{\ell\nu})$
- Template fitting procedure relies on tools with **low formal accuracy**; missing higher order information captured only within some approximation (e.g. reweighing)
- Minimisation procedure sensible when  $\chi^2/N_{dat} \sim 1$

4.

Inclusion of  $\Sigma_{th}$  contribution to the covariance matrix not possible due to **non-statistical** nature of theory uncertainty

Data-driven approach allows the possibility to determine  $m_W$  via template fits at the **price** of losing the possibility to assess robustly the theoretical uncertainties on the modelling incapability to fully exploit recent progress in theoretical calculations for candle LHC processes

Tuning assumes universality of CCDY and NCDY, although several differences play a role (experimental

$$\chi^{2} = (D - T)^{T} \cdot C^{-1} \cdot (D - T)$$
$$C = \Sigma_{\text{stat}} + \Sigma_{\text{syst}} + \Sigma_{\text{MC}} + \Sigma_{\text{PDF}}$$

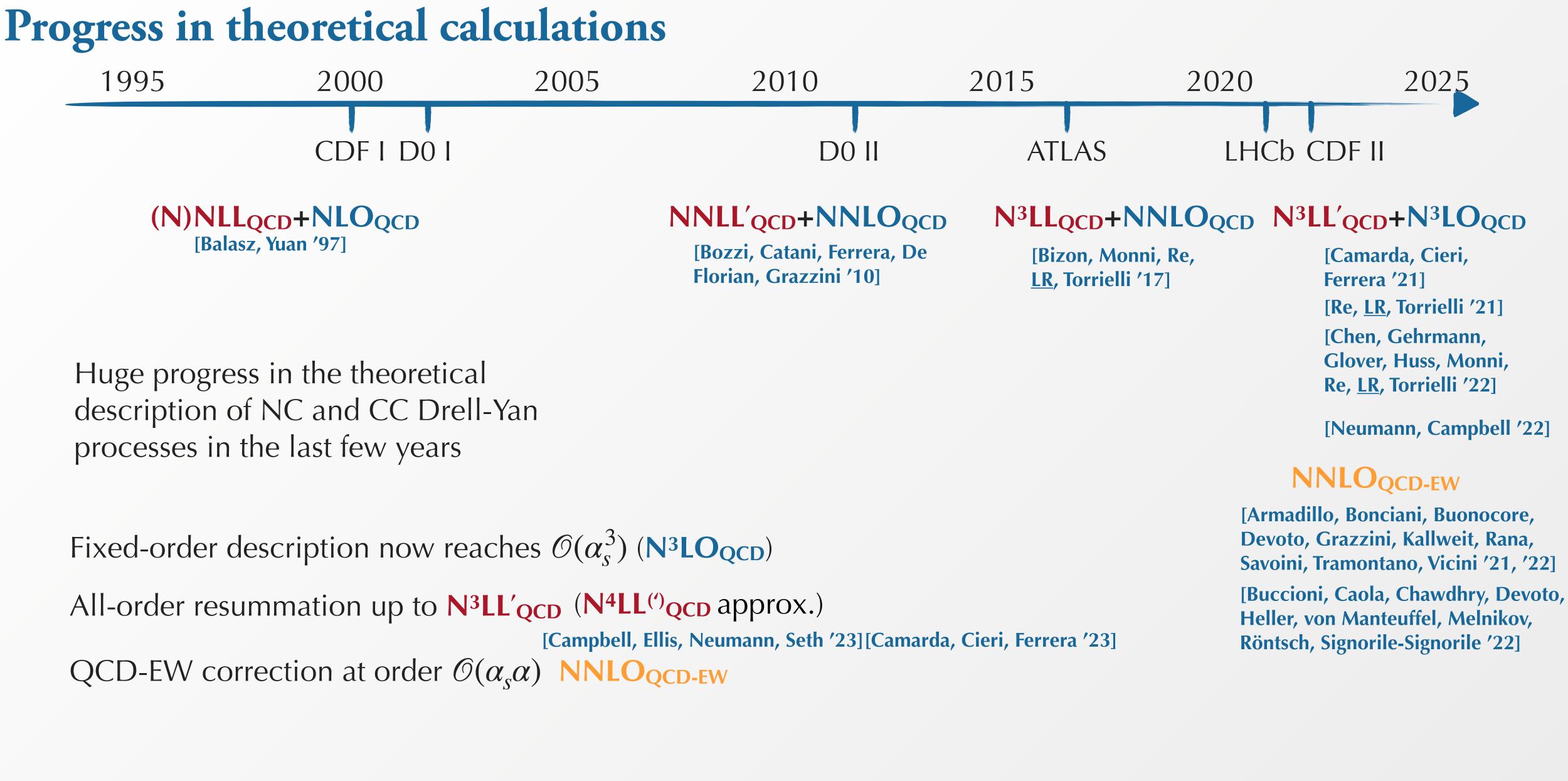
#### Progress in theoretical calculations 1995 2000 2005 2010 CDF I D0 I D0 II NNLL'<sub>QCD</sub>+NNLO<sub>QCD</sub> (N)NLL<sub>QCD</sub>+NLO<sub>QCD</sub> [Balasz, Yuan '97]

Huge progress in the theoretical description of NC and CC Drell-Yan processes in the last few years

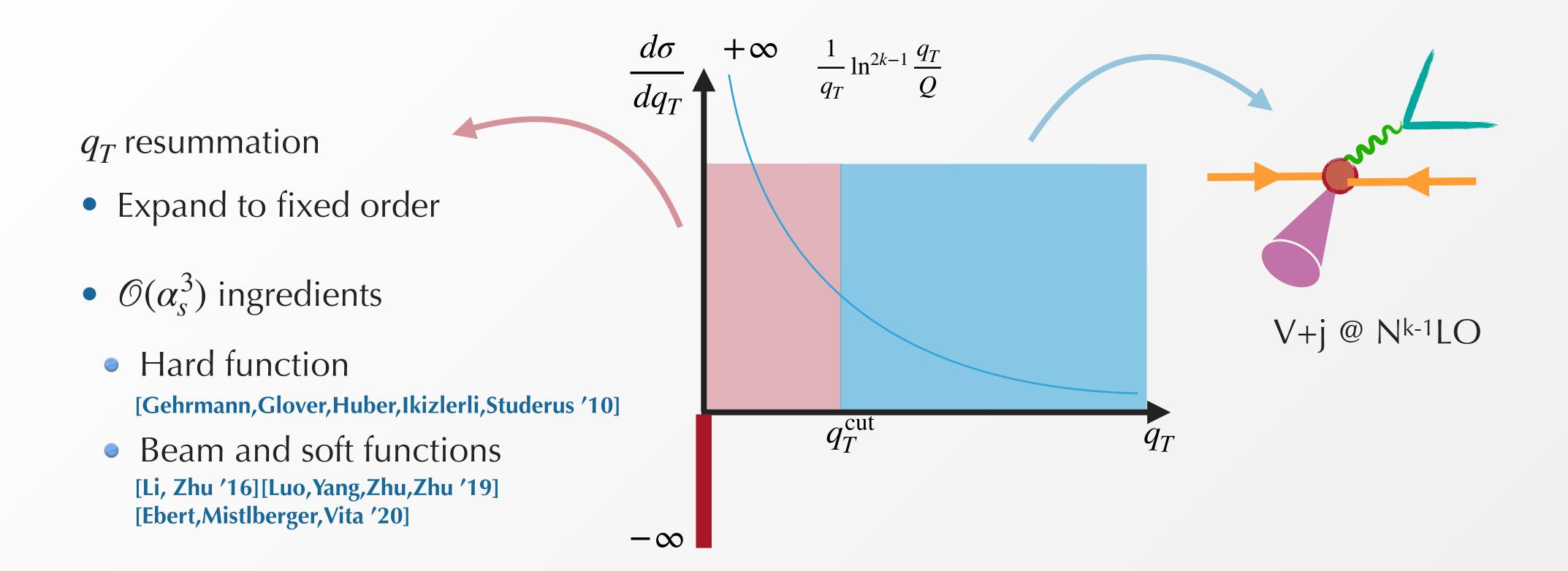


[Bozzi, Catani, Ferrera, De Florian, Grazzini '10]





## Fiducial Drell-Yan production at N<sup>3</sup>LO<sub>QCD</sub>



## Fiducial Drell-Yan production at N<sup>3</sup>LO<sub>QCD</sub>

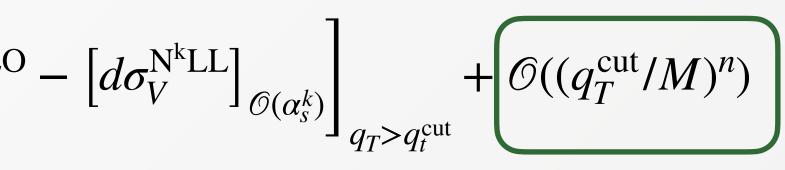
$$d\sigma_{V}^{N^{k}LO} \equiv \mathscr{H}_{V}^{N^{k}LO} \otimes d\sigma_{V}^{LO} + \left[ d\sigma_{V+jet}^{N^{k-1}LO} \right]$$

Competing interests:  $q_T^{\text{cut}}$  as large as possible  $\leftrightarrow q_T^{\text{cut}}$  as small as possible Numerical stability

Power corrections larger when symmetric cuts applied on final state leptons due to enhanced sensitivity to soft radiation in back-to-back configurations [Salam, Slade '21]

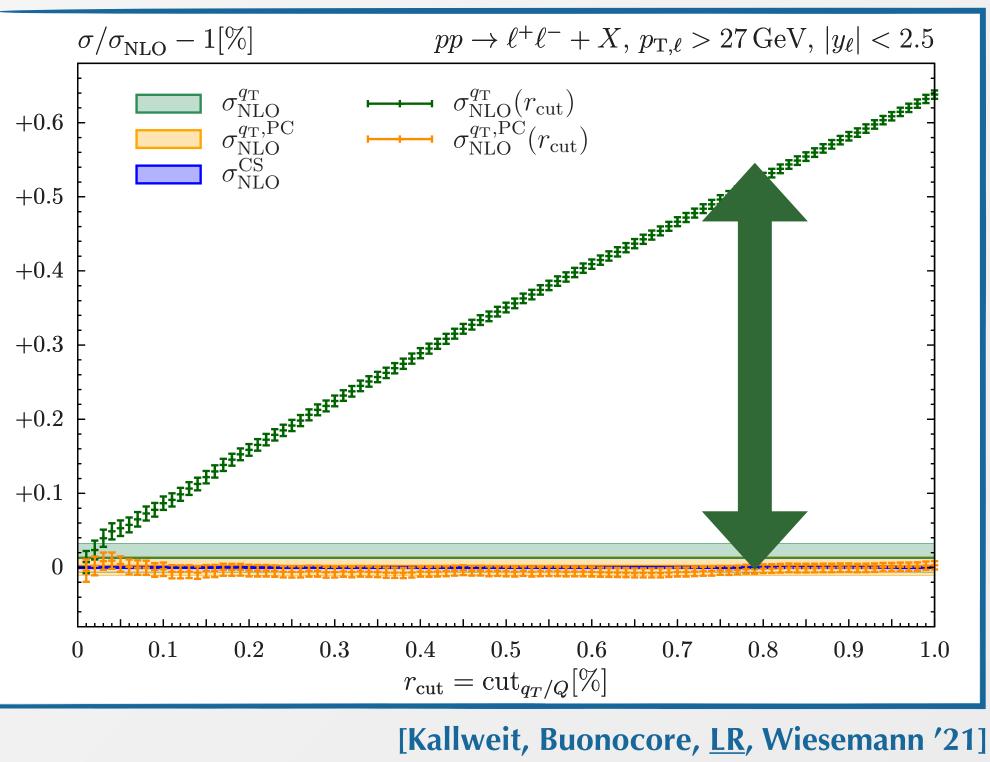
Control of fiducial linear power corrections improves dramatically the efficiency of the non-local subtraction [Kallweit, Buonocore, <u>LR</u>, Wiesemann '21][Camarda, Cieri, Ferrera '21]

Necessary to reach N<sup>3</sup>LO accuracy for fiducial setup

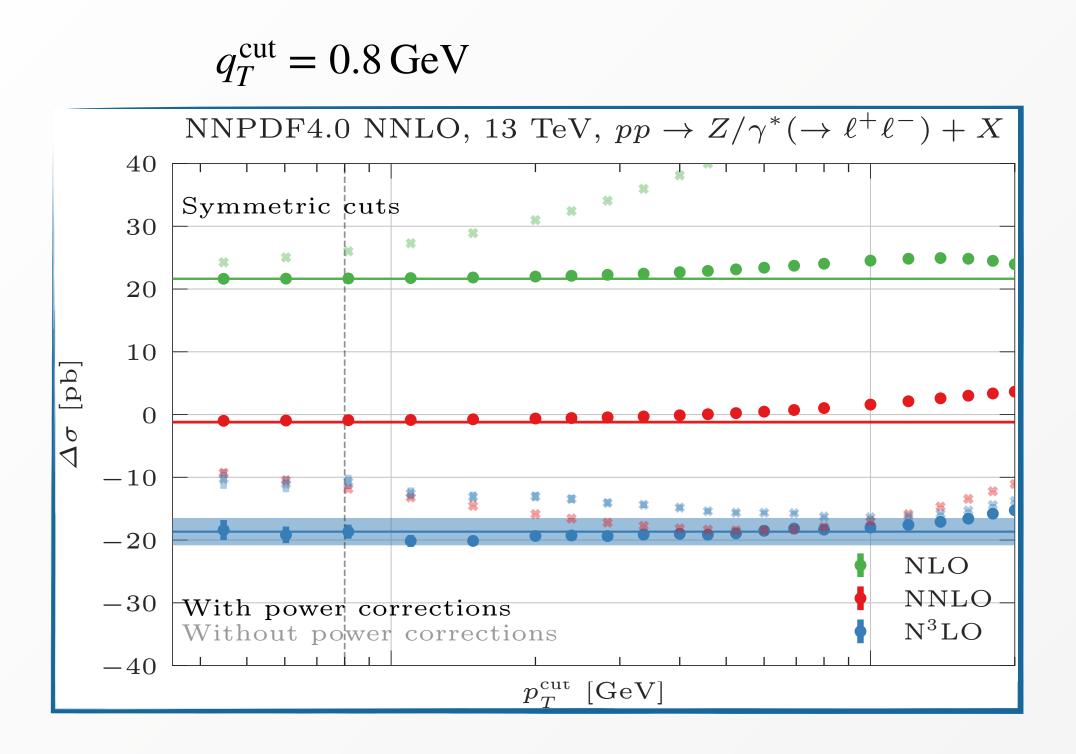


#### Suppress power corrections





## Fiducial Drell-Yan production at N<sup>3</sup>LO<sub>QCD</sub>



- 2.5% negative correction at N<sup>3</sup>LO in the ATLAS fiducial region. N<sup>3</sup>LO larger than the NNLO correction and outside its error band
- More robust estimate of the theory uncertainty when resummation effects are included

Order	$\sigma$ [pb] Symmetric cuts		
k	$N^k LO$	$N^kLO+N^kLL$	
0	$721.16^{+12.2\%}_{-13.2\%}$		Includes
1	$742.80(1)^{+2.7\%}_{-3.9\%}$	$748.58(3)^{+3.1\%}_{-10.2\%}$ $740.75(5)^{+1.15\%}_{-2.66\%}$ $726.2(1.1)^{+1.07\%}_{-0.77\%}$	resumma linear po
2	$741.59(8)^{+0.42\%}_{-0.71\%}$	$740.75(5)^{+1.15\%}_{-2.66\%}$	correctio
3	$722.9(1.1)^{+0.68\%}_{-1.09\%}\pm0.9$	$726.2(1.1)^{+1.07\%}_{-0.77\%}$	

[Chen, Gehrmann, Glover, Huss, Monni, Re, <u>LR</u>, Torrielli]

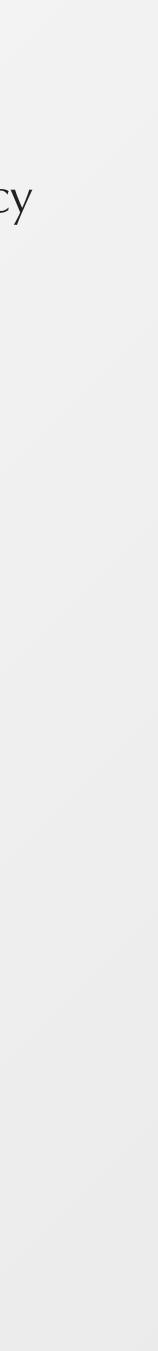


RadISH performs resummation in direct space - similar in spirit to a parton shower, with control on formal accuracy Result at NLL accuracy with scale-independent PDFs

$$\sigma(p_T) = \sigma_0 \int \frac{dv_1}{v_1} \int_0^{2\pi} \frac{d\phi_1}{2\pi} e^{-R(\epsilon v_1)} \qquad v_i = k_{t,i}/M, \quad \zeta_i = k_{t,i}/M, \quad \zeta_i$$



$$v_i = k_{t,i}/M, \quad \zeta_i = v_i/v_1$$



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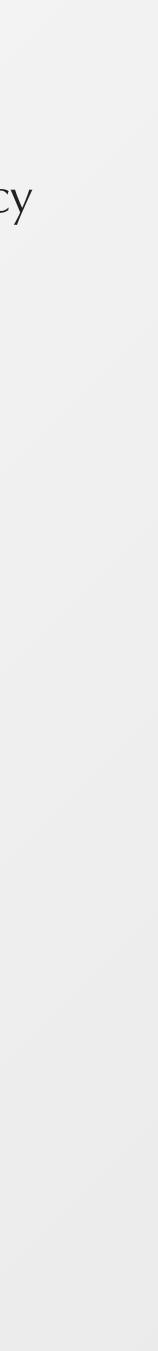
$$\sigma(p_T) = \sigma_0 \int \frac{dv_1}{v_1} \int_0^{2\pi} \frac{d\phi_1}{2\pi} e^{-R(\epsilon v_1)} \quad \text{Simple observable} \qquad v_i = k_{t,i}/M, \quad \zeta_i = k_{t,i}/M, \quad$$



$$v_i = k_{t,i}/M, \quad \zeta_i = v_i/v_1$$

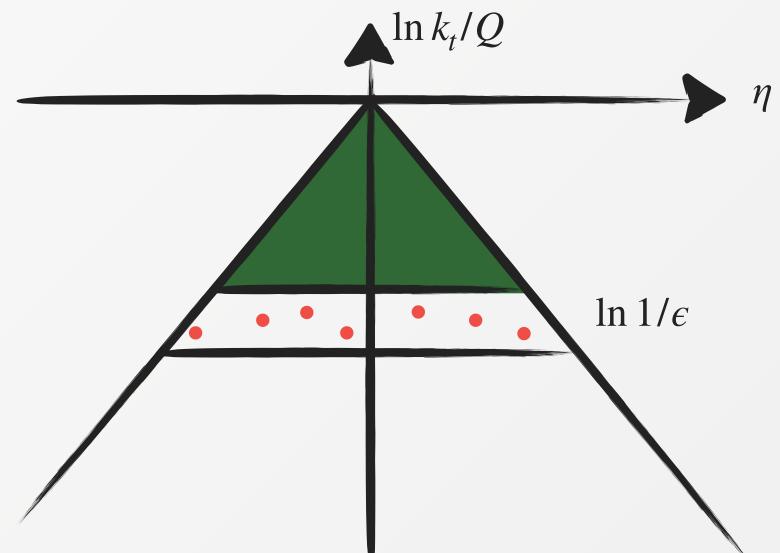
 $\ln k_t/Q$ 





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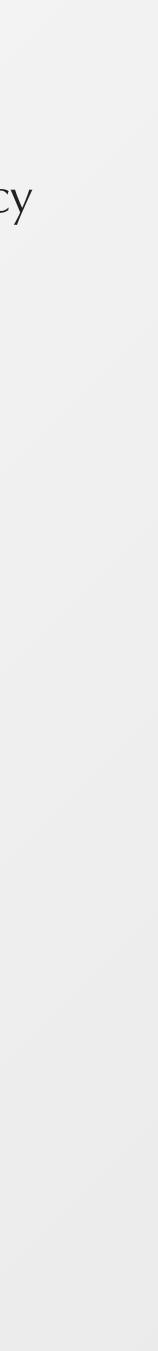




$$v_i = k_{t,i}/M, \quad \zeta_i = v_i/v_1$$

**Transfer function** 

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$$\sigma(p_T) = \sigma_0 \int \frac{dv_1}{v_1} \int_0^{2\pi} \frac{d\phi_1}{2\pi} e^{-R(\epsilon v_1)} \qquad v_i = k_{t,i}/M, \quad \zeta_i = k_{t,i}/M, \quad \zeta_i$$

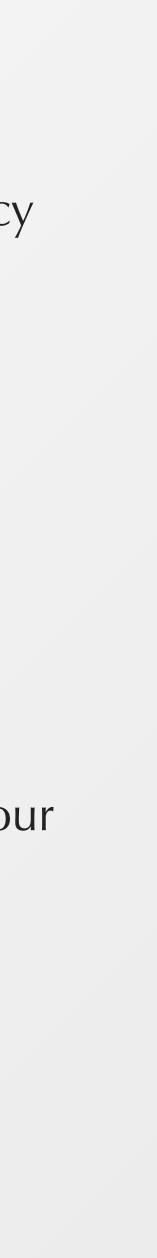
Formula can be evaluated with Monte Carlo methods; dependence on  $\epsilon$  vanishes (as  $\mathcal{O}(\epsilon)$ ) and result is finite in four dimensions

**Logarithmic accuracy** defined in terms of  $\ln(M/k_{t1})$ Result formally equivalent to the *b*-space formulation [Bizon, Monni, Re, LR, Torrielli '17]

Resummation formalism can be extended at higher accuracies; resummation at N<sup>3</sup>LL' available [Re, LR, Torrielli '21]

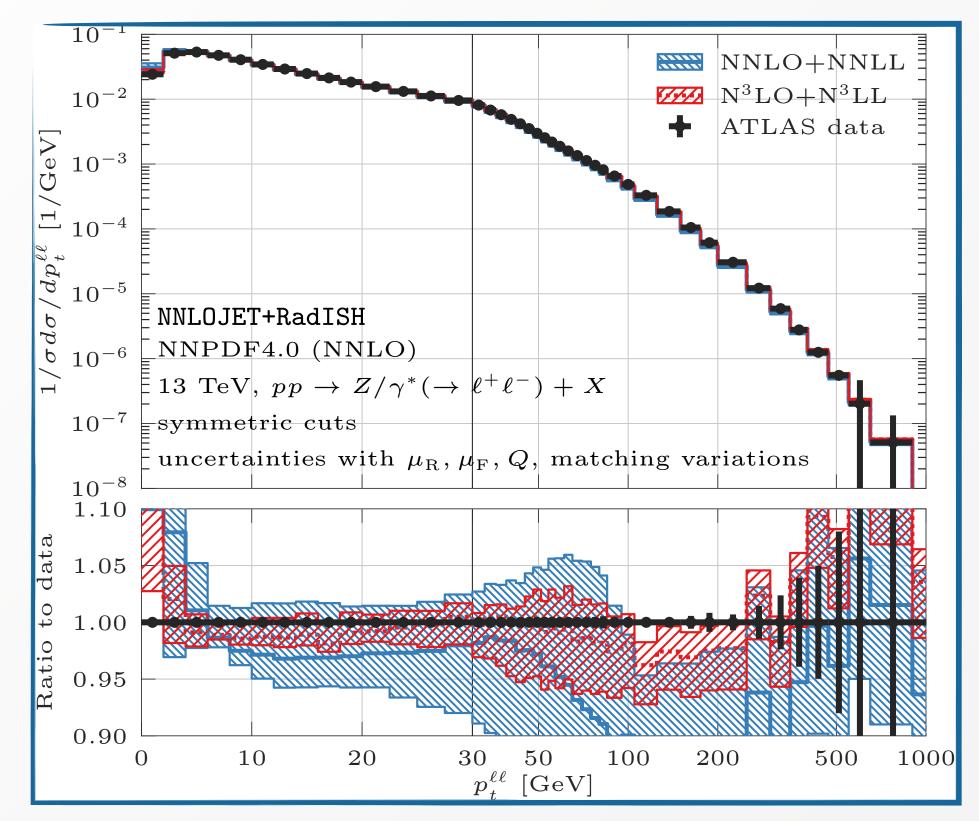


$$v_i = k_{t,i}/M, \quad \zeta_i = v_i/v_1$$

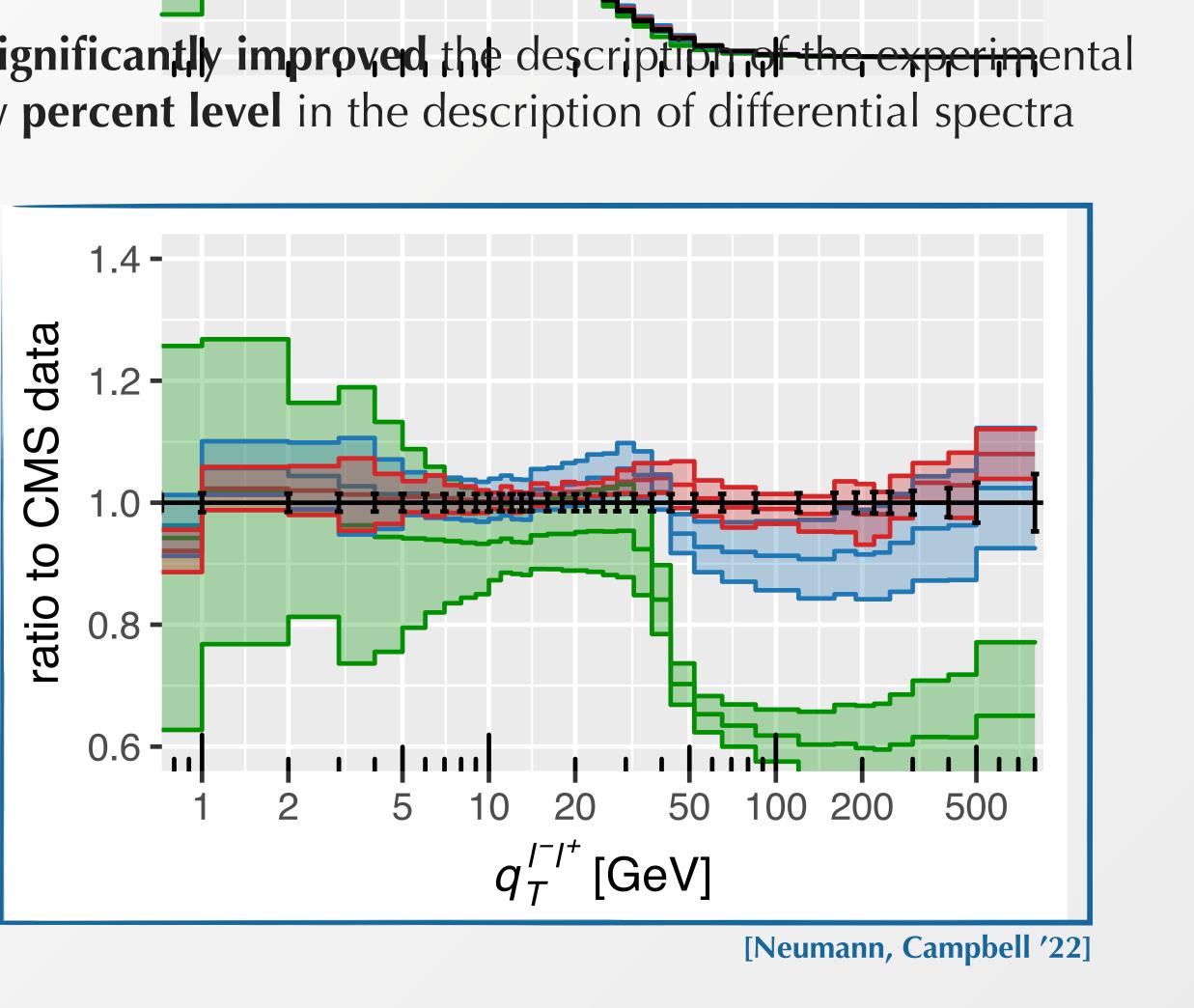


### Description of experimental data at N<sup>3</sup>LO<sub>QCD</sub>+

The theoretical progress made in the the past 5 years has significantly improved the description of the experimental data, pinning down the theoretical uncertainties to the few percent level in the description of differential spectra



[Gehrmann, Glover, Huss, Chen, Monni, Re, <u>LR</u>, Torrielli, 2203.01565]



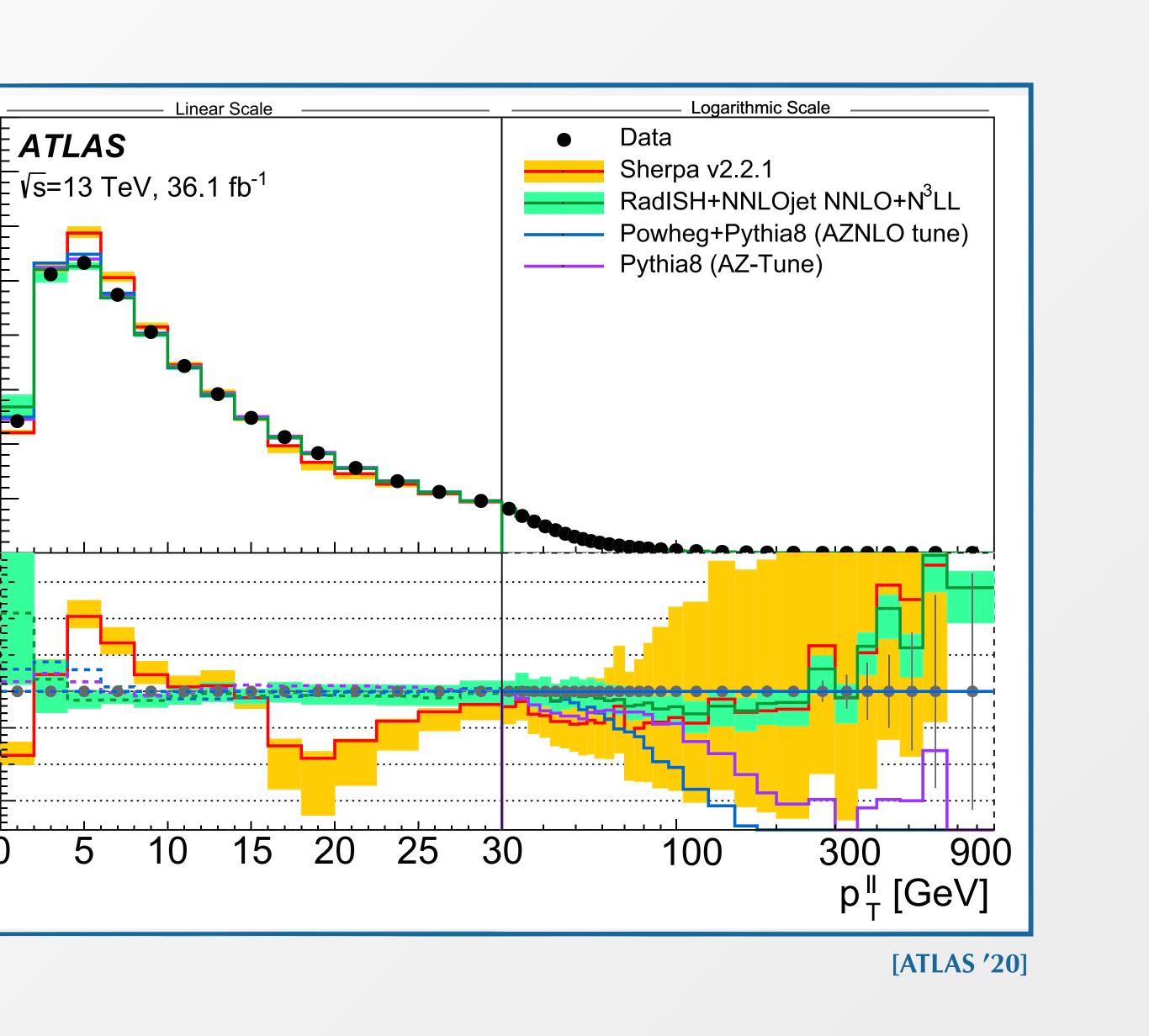
blue:	NNLL' <sub>QCD</sub> +NNLO <sub>QCD</sub>
red:	N <sup>3</sup> LL' <sub>QCD</sub> +N <sup>3</sup> LO <sub>QCD</sub>

### Description of experimental data at N<sup>3</sup>LO<sub>QCD</sub>+N<sup>3</sup>LL'<sub>QCD</sub>

Theoretical predictions now are capable of describing the data **precisely** across a wide range of scales

green: N<sup>3</sup>LL<sub>QCD</sub>+N<sup>3</sup>LO<sub>QCD</sub>

0.08 > 0.07 9 0.06 0.05 0.04 1/σ 0.03 0.02 0.01⊦ Data 1.15 .05 MC 0.95 0.9 0.85 0



### Description of experimental data at N<sup>3</sup>LO<sub>QCD</sub>+N<sup>3</sup>LE<sub>QCD</sub>

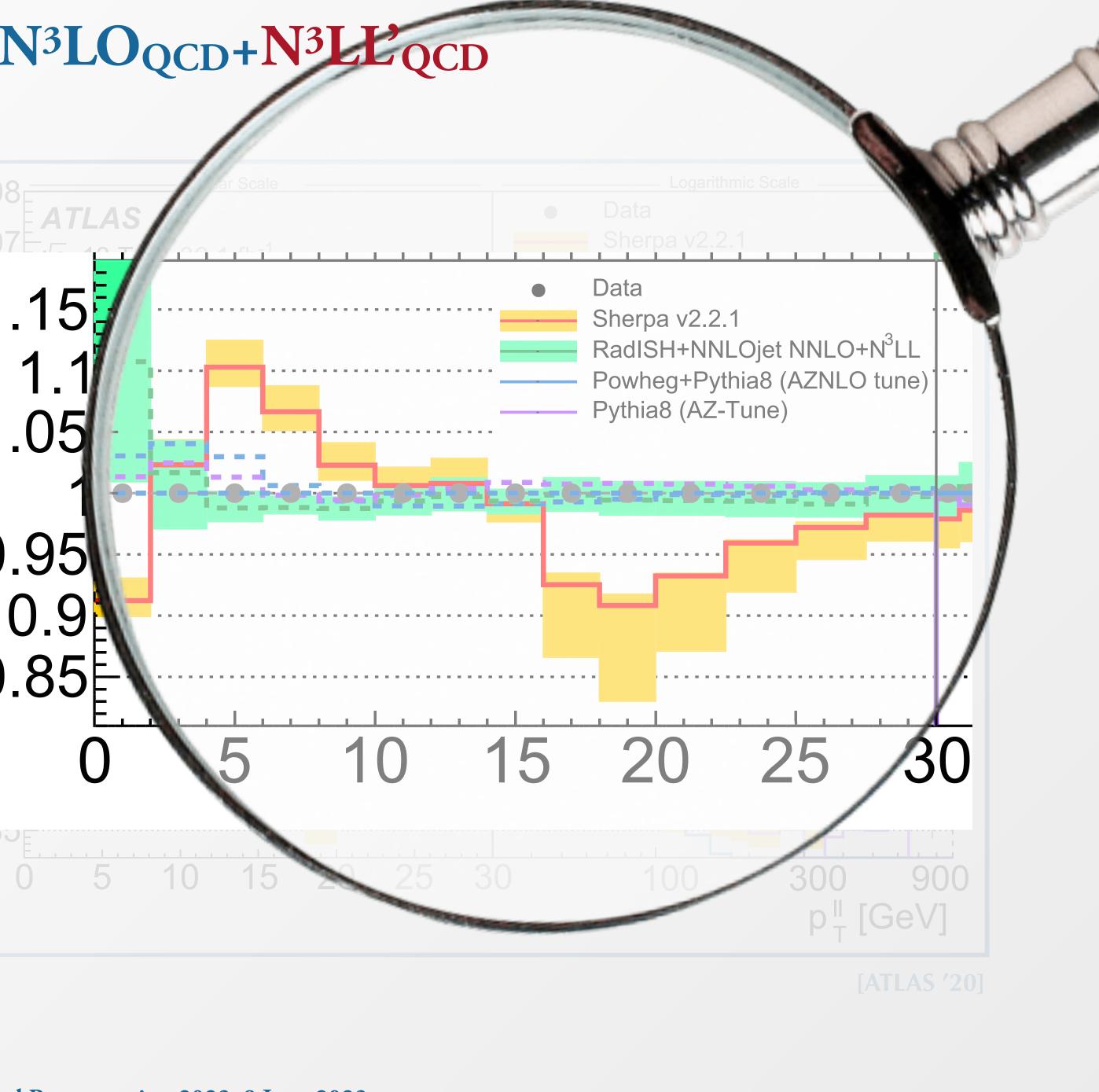
Theoretical predictions now are capable of describing the data **precisely** across a wide range of scales

#### green: N<sup>3</sup>LL<sub>QCD</sub>+N<sup>3</sup>LO<sub>QCD</sub>

And are on par, if not better, than parton showers predictions that have been tuned to experimental data

N.B. : RadISH+NNLOJET predictions **do not** include any non-perturbative modelling at low q<sub>T</sub>

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### Understanding the Z and W correlations

Thanks to the availability of theoretical prediction at high accuracy, it is possible to assess reliably the behaviour of the perturbative series for crucial observables such as  $p_T^Z/p_T^W$  ratio

$$\frac{1}{\sigma^{W}} \frac{d\sigma^{W}}{p_{\perp}^{W}} \sim \frac{1}{\sigma_{\text{data}}^{Z}} \frac{d\sigma_{\text{theory}}^{Z}}{\sigma_{\text{theory}}^{Z}} \frac{1}{p_{\perp}^{W}} \frac{d\sigma_{\text{theory}}^{W}}{\rho_{\perp}^{Z}}$$

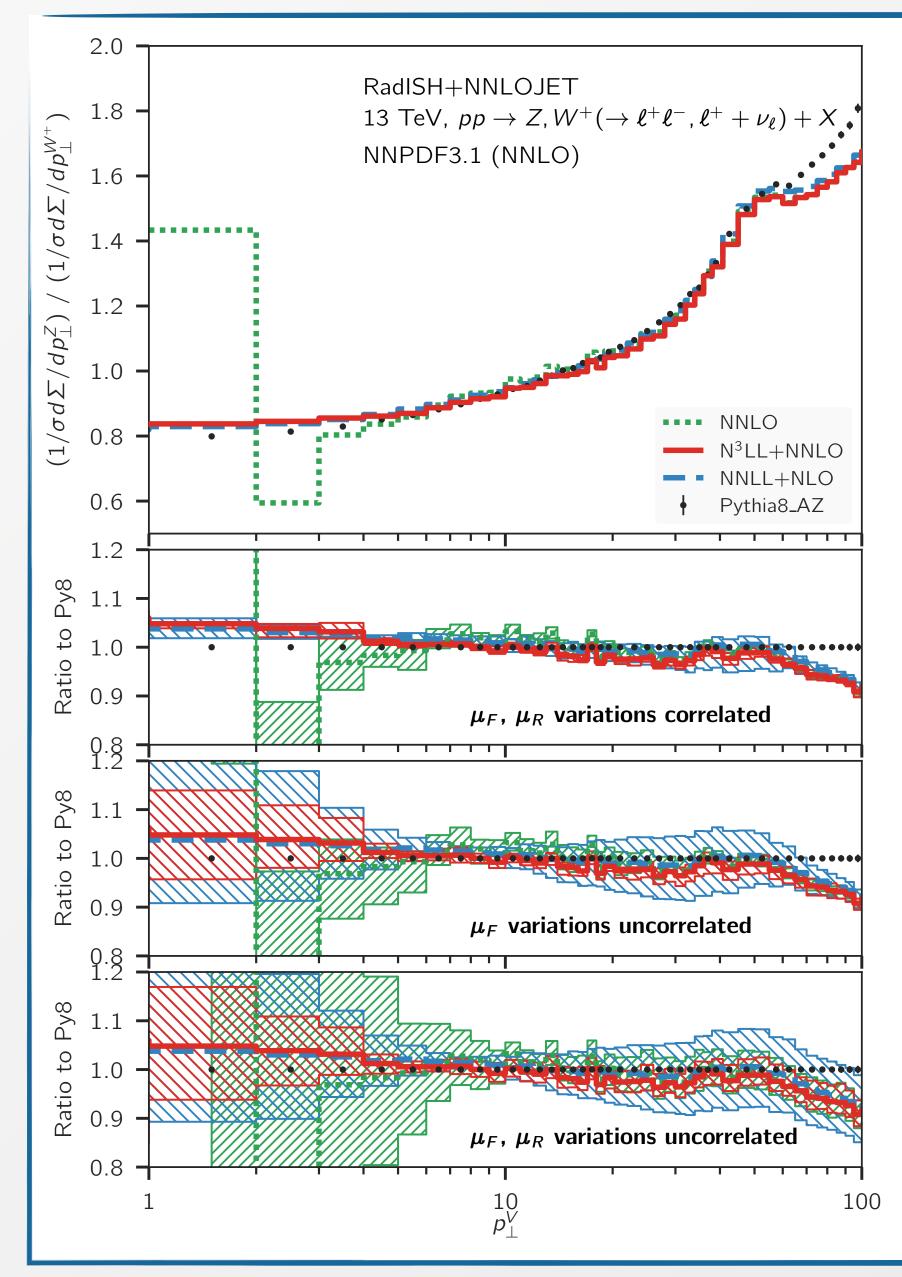
Stability of the ratio indicates high level of correlation between the two spectra

Comparison with tuned event generator such as **PYTHIA\*** however indicates that full correlation might be too strong an assumption

\* "PYTHIA is not QCD"

[Kirill Melnikov, QCD@LHC 2016]

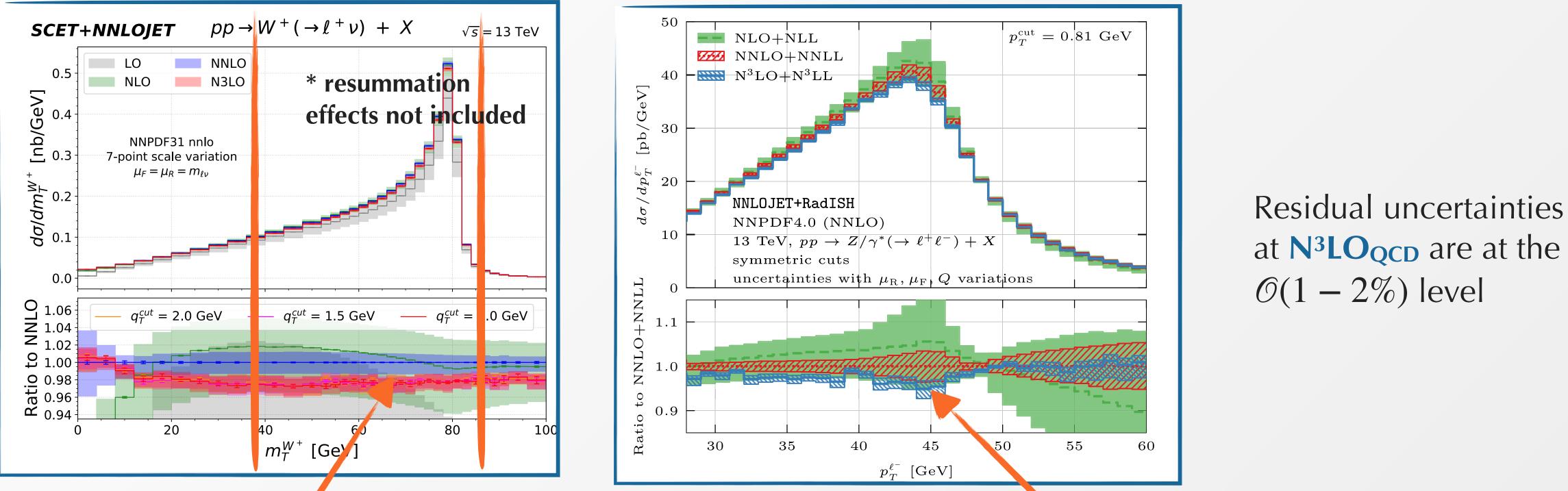
[Bizon, de Ridder, Gehrmann, Glover, Huss, Chen, Monni, Re, <u>LR</u>, Walker, 1905.05171] Parton Showers and Resummation 2023, 8 June 2023





## **Control of the differential distributions in DY production**

Shape of differential spectra is affected by higher order predictions



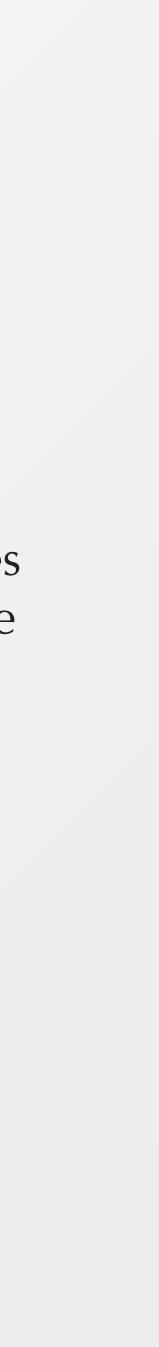
[Gehrmann, Glover, Huss, Chen, Yang, Zhu 2205.11426]

Impact of N<sup>3</sup>LO<sub>QCD</sub> corrections relatively flat in the fit window for m<sub>T</sub>

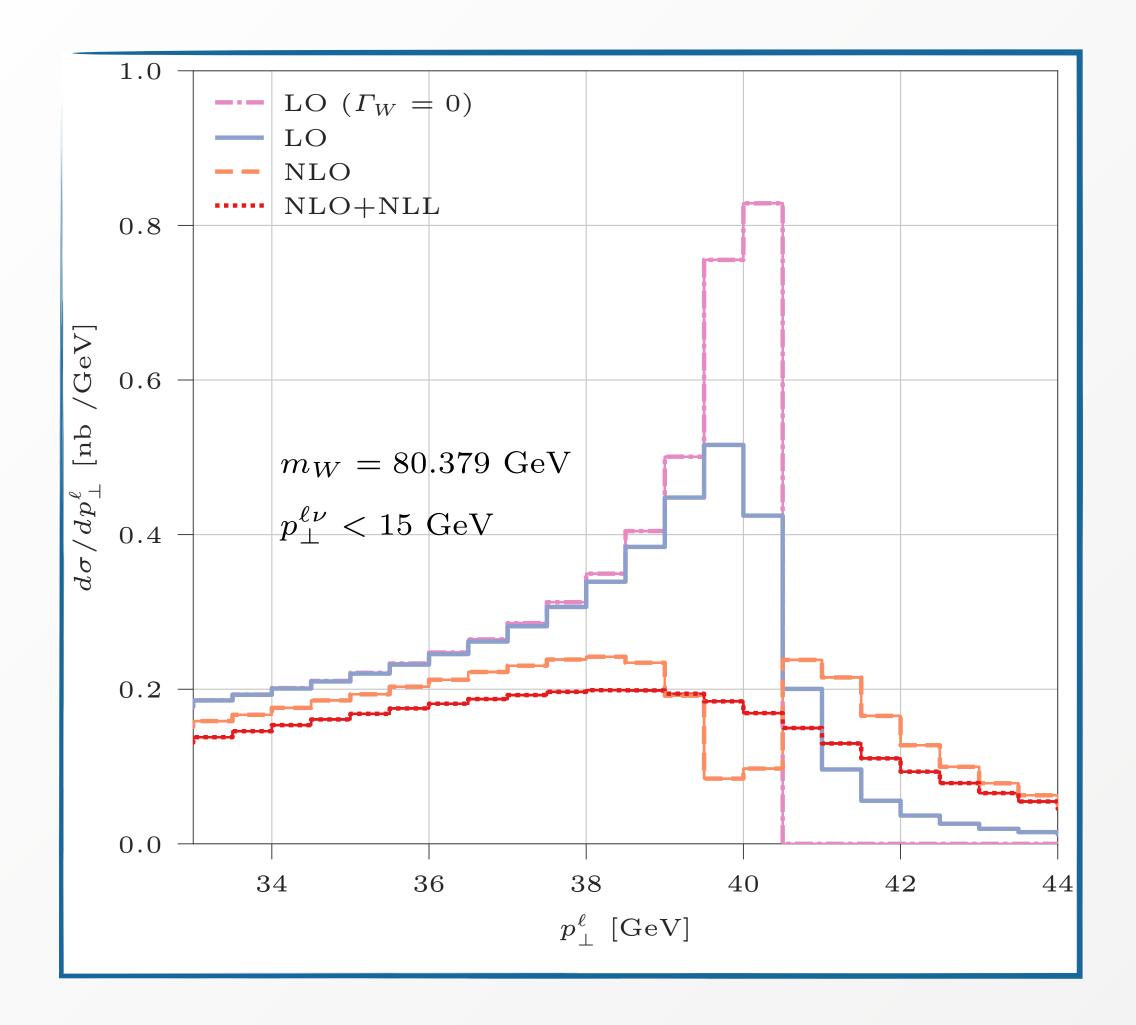
Interplay of QCD and EW corrections further modify the shape of the differential distributions See previous talk by G. Ferrera

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[Gehrmann, Glover, Huss, Chen, Monni, R. LR, Torrielli, 2203.01565] N<sup>3</sup>LL'<sub>QCD</sub>+N<sup>3</sup>LO<sub>QCD</sub> modifies the shape after the Jacobian peak for  $p_T^{\ell}$ 



### The lepton transverse momentum distribution in CC DY



Presence of the endpoint makes the distribution particularly sensitive to  $m_W$ 

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The lepton transverse momentum distribution features a **Jacobian peak** at  $p_T^{\mathscr{C}} \bigvee m_W A \mathfrak{P}_{\perp}^2$ 

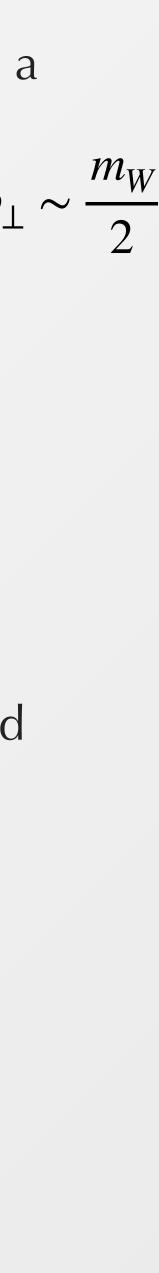
At **LO**, in the narrow width approx., the distribution  $p_{\perp}$  features a kinematical endpoint at  $m_W/2$ 

Width effects broaden the distribution above  $m_W/2$ 

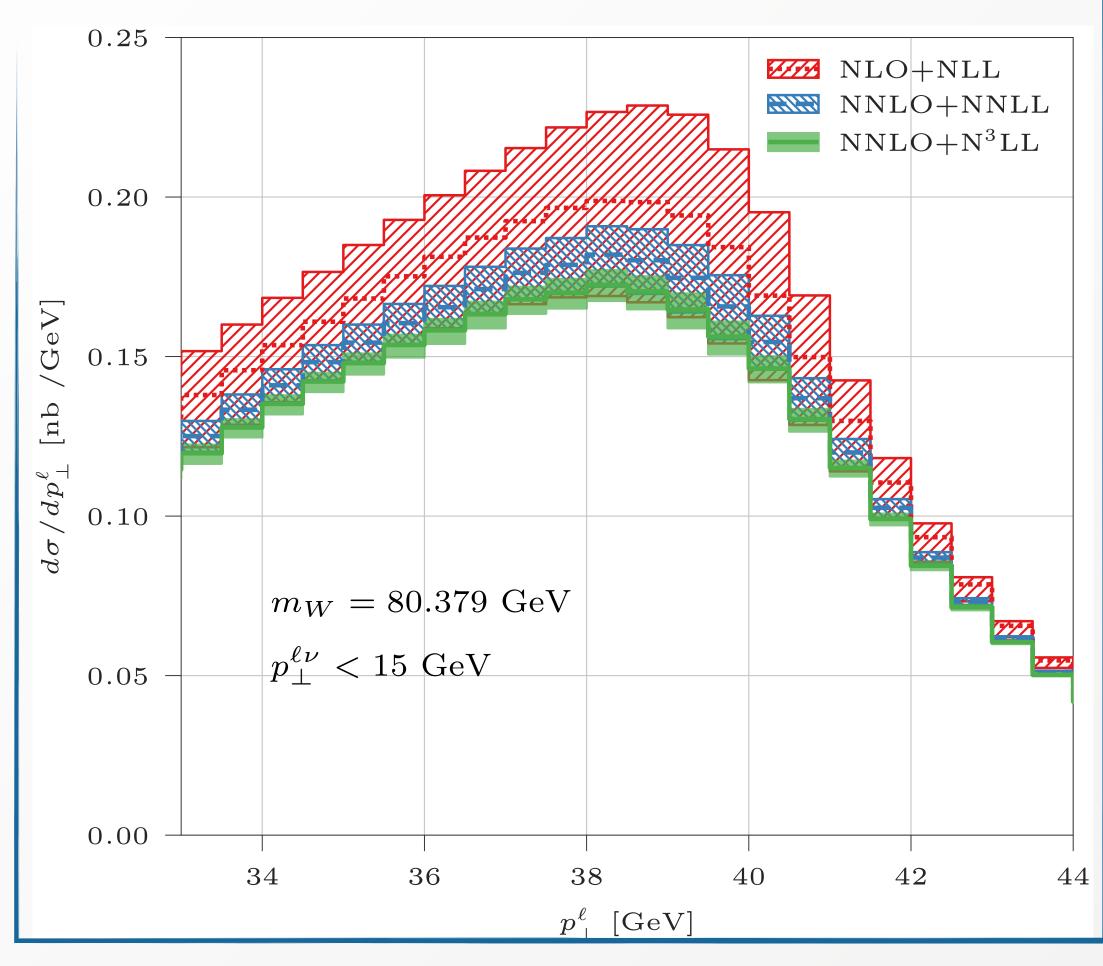
Beyond LO, sensitivity to **soft radiation** creates unphysical instabilities around  $m_W/2$  in fixed-order computations [Catani, Webber '97]

All-order resummation effects cure such instabilities ad provide **physical prediction** 

 $m_W$ 



### The lepton transverse momentum distribution in CC DY



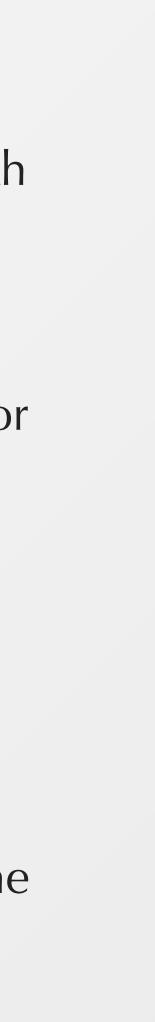
[LR, P. Torrielli, A. Vicini '23]

Progress in theoretical computations allows for a **precise theoretical description** of the distribution, with O(2%) residual uncertainties

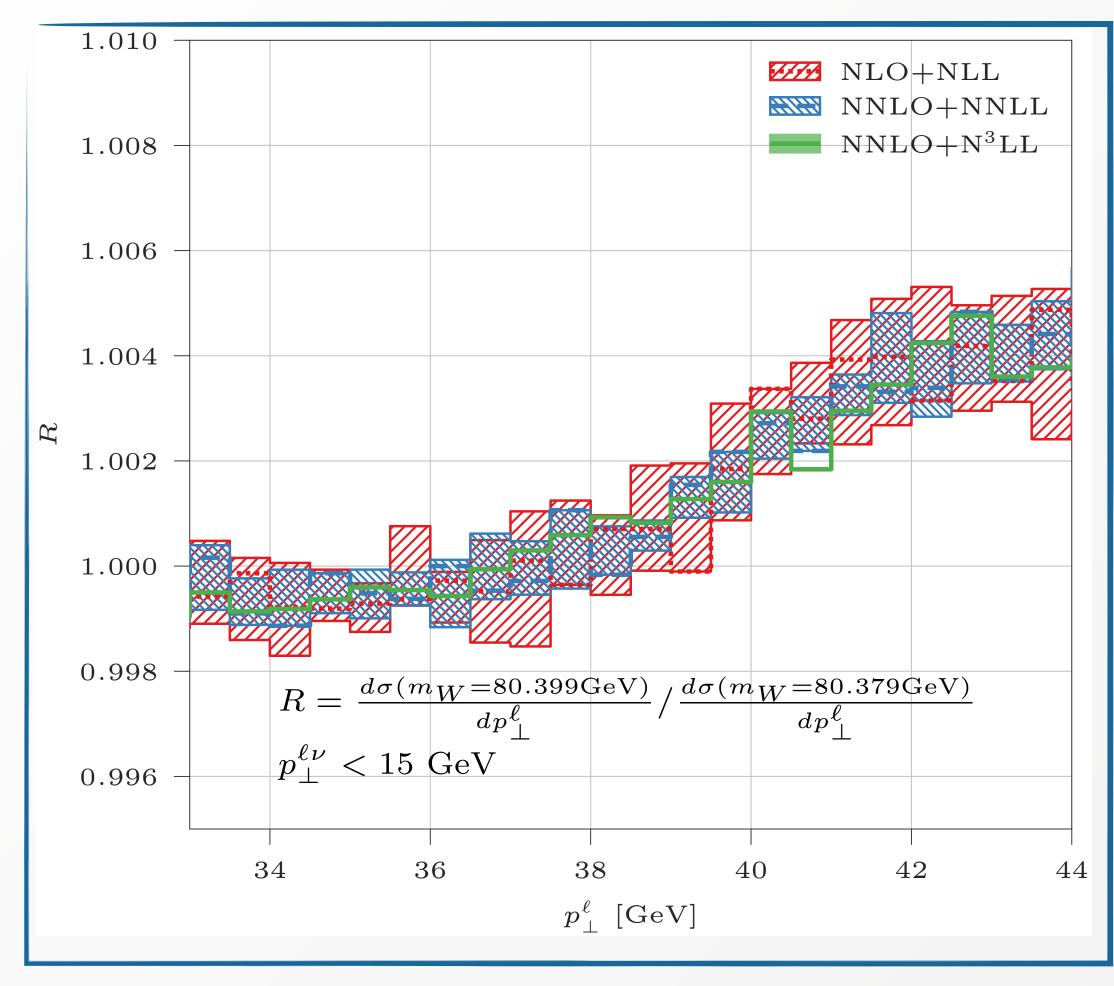
Uncertainty band encodes canonical 7-point scale variation envelope and resummation scale variation for central scales (total: 9-point envelope)

$$\mu_{F,R} = \xi_{F,R} \sqrt{m_{\ell\nu}^2 + p_{\perp,\ell\nu}^2} \qquad Q = \xi_Q m_{\ell\nu}$$
  
$$\xi_{F,R} \in \{1/2,1,2\}, \qquad \xi_Q \in \{1/4,1/2,1\}$$

When width and resummation effects are included, the peak is located at ~38.5 GeV



### The lepton transverse momentum distribution in CC DY



[LR, P. Torrielli, A. Vicini '23]

Determination of  $m_W$  with  $\mathcal{O}(10 \,\text{MeV})$  precision requires control of the shape at the few permille level

Distortion of the shape largely independent of the accuracy or scale choice in pure QCD

Sensitivity to  $m_W$  related to propagation and decay of the W boson

Consequence of the factorisation between production (subject to QCD effect) and propagation and decay

Sensitivity to *m<sub>W</sub>* independent on the QCD approximation

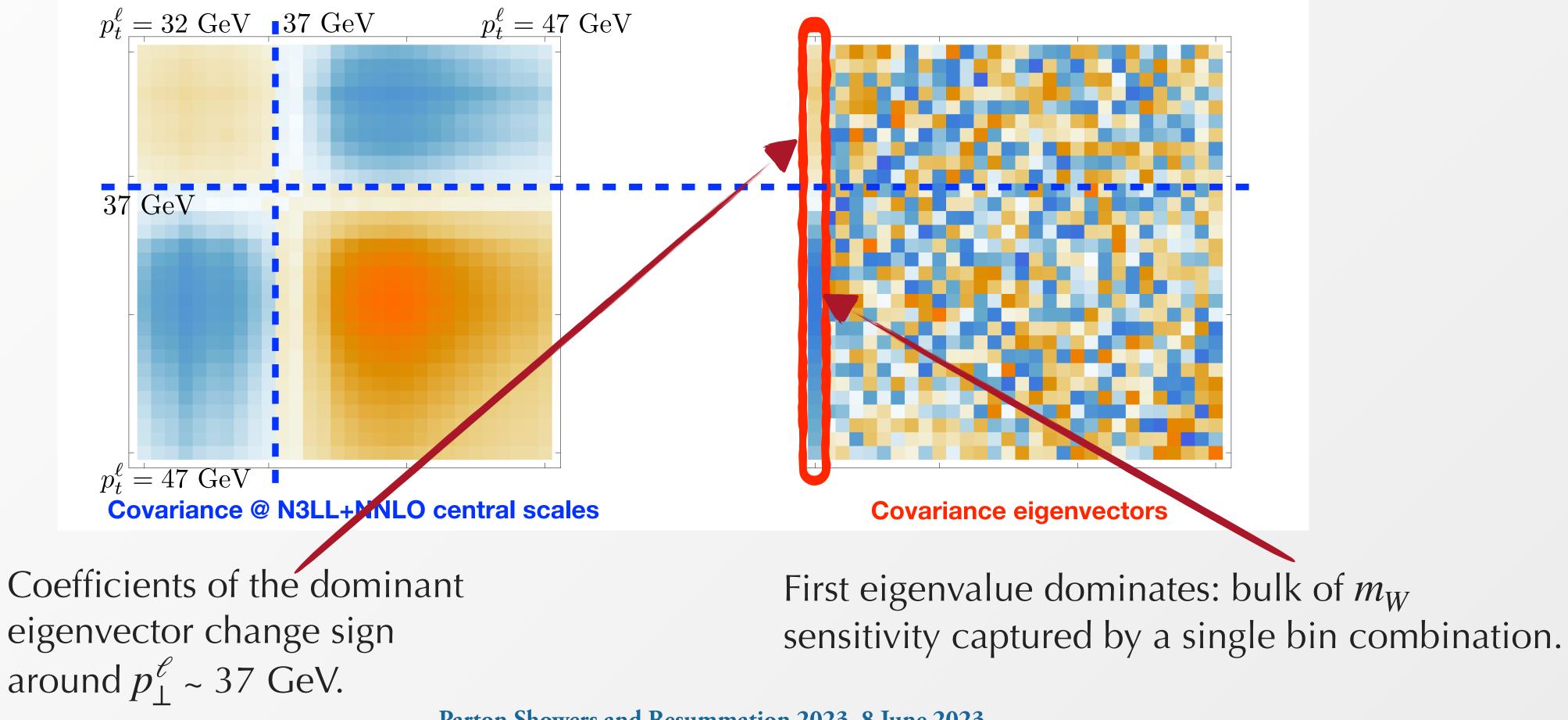
Uncertainty on  $m_W$  instead related to the QCD approximation

#### $p_{\perp}^{\ell}$ covariance matrix

Sensitivity on  $m_W$  of the bins of the  $p_T^{\ell}$  distribution can be quantified by means of the **covariance matrix** with respect to  $m_W$  variations

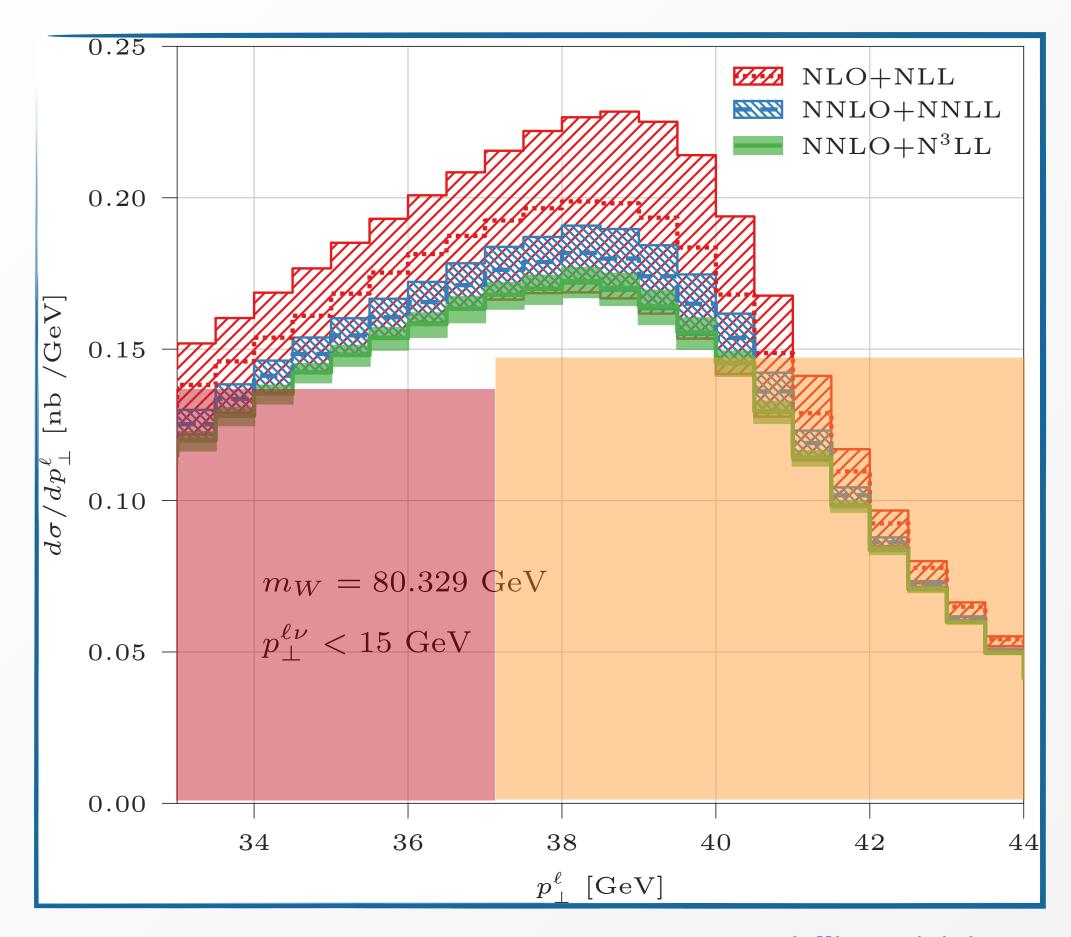
$$C_{ij}^{(m_W)} = \langle \sigma_i \sigma_j \rangle - \langle \sigma_i \rangle \langle \sigma_j \rangle$$

The eigenvalues of this matrix express sensitivity on  $m_W$  on linear combinations of bins of the distribution



$$\langle x \rangle = \frac{1}{N} \sum_{k=1}^{N} x_k$$

## The jacobian asymmetry $\mathscr{A}_{p^{\ell}}$



$$L = \int_{p_{\perp,\min}^{\ell}}^{p_{\perp,\min}^{\ell}} dp_{\perp}^{\ell} \frac{d\sigma}{dp_{\perp}^{\ell}}$$

[LR, P. Torrielli, A. Vicini '23]

$$U = \int_{p_{\perp,\text{mid}}^{\ell}}^{p_{\perp,\text{max}}^{\ell}} dp_{\perp}^{\ell} \frac{d\sigma}{dp_{\perp}^{\ell}}$$

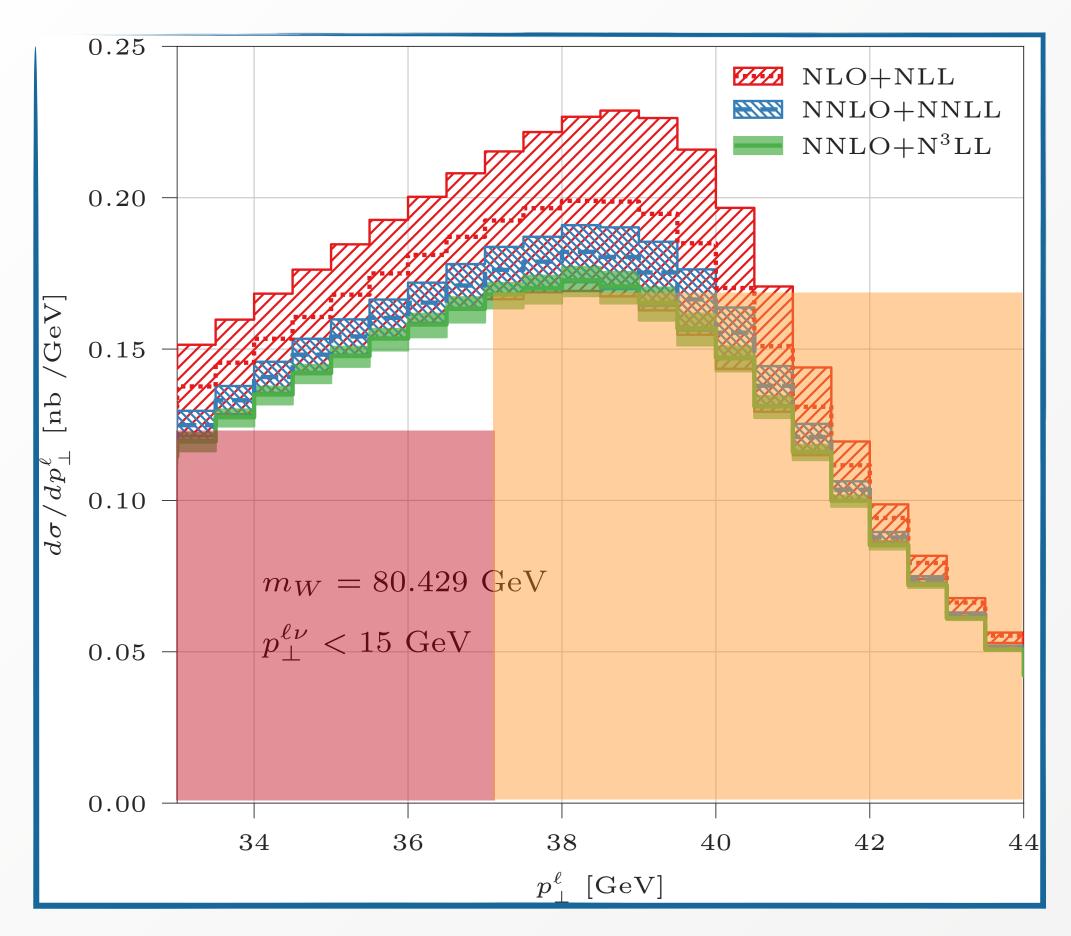
Following this indication, we design a **new observable** 

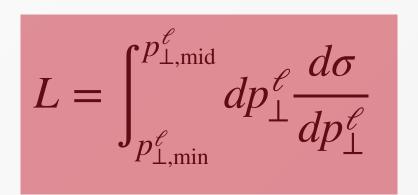
$$\mathscr{A}(p_{\perp,\min}^{\ell}, p_{\perp,\min}^{\ell}, p_{\perp,\max}^{\ell}) = \frac{L_{p_{\perp}^{\ell}} - U_{p_{\perp}^{\ell}}}{L_{p_{\perp}^{\ell}} + U_{p_{\perp}^{\ell}}}$$

Scalar observable (i.e. it is measurable via counting) which depends only on the edges of the two defining bins



## The jacobian asymmetry $\mathscr{A}_{p^{\ell}}$





[LR, P. Torrielli, A. Vicini '23]

$$U = \int_{p_{\perp,\text{mid}}^{\ell}}^{p_{\perp,\text{max}}^{\ell}} dp_{\perp}^{\ell} \frac{d\sigma}{dp_{\perp}^{\ell}}$$

Following this indication, we design a **new observable** 

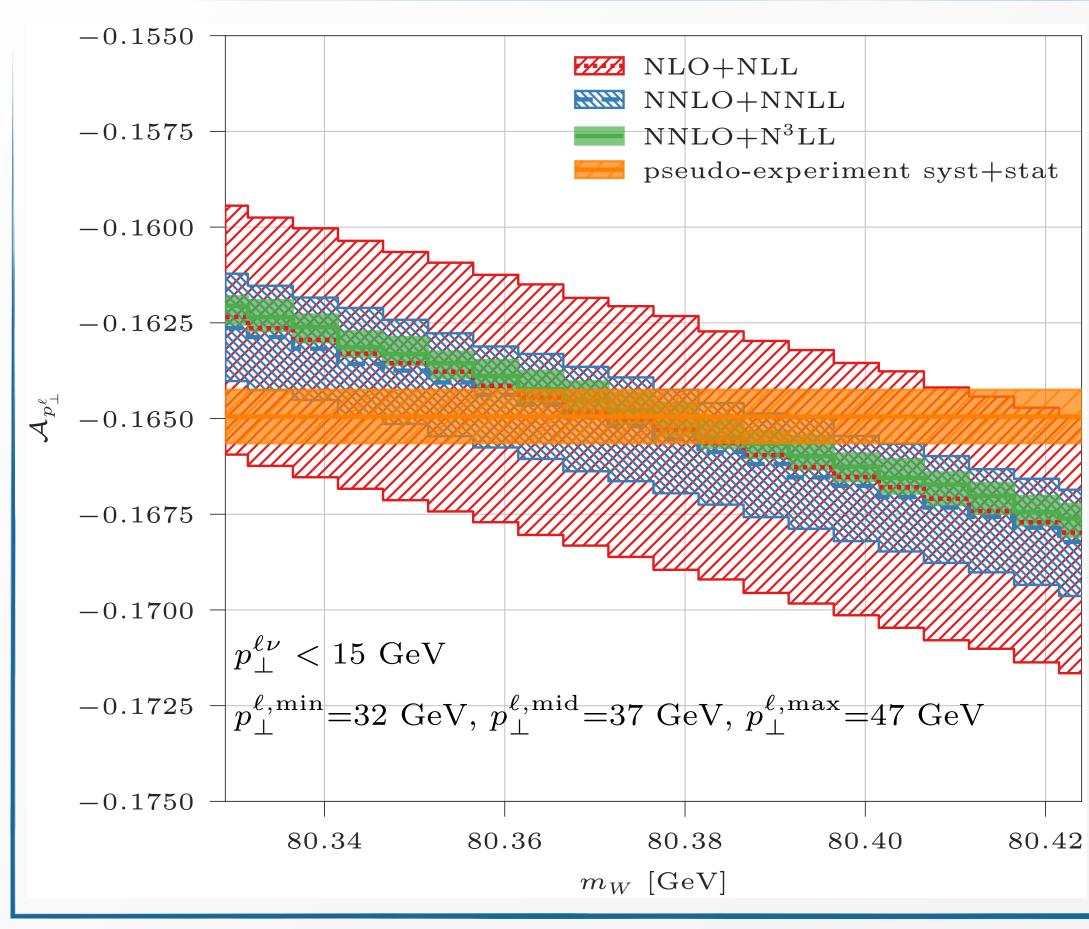
$$\mathscr{A}(p_{\perp,\min}^{\ell}, p_{\perp,\min}^{\ell}, p_{\perp,\max}^{\ell}) = \frac{L_{p_{\perp}^{\ell}} - U_{p_{\perp}^{\ell}}}{L_{p_{\perp}^{\ell}} + U_{p_{\perp}^{\ell}}}$$

Scalar observable (i.e. it is measurable via counting) which depends only on the edges of the two defining bins

Increasing  $m_W$  shifts the peak to the right

Orange bin gets more populated  $\rightarrow$  asymmetry decreases

## The jacobian asymmetry $\mathscr{A}_{p_1^\ell}$ and $m_W$



#### [LR, P. Torrielli, A. Vicini '23]

The main systematics on the two fiducial cross sections is related to the lepton momentum scale resolution Determination at the ±15 MeV level from the experimental side seems possible ( $\delta A_{p_1^{\ell}}$ =0.0007 with 140 fb<sup>-1</sup> and 0.001 systematic error on U, L)

The asymmetry features a linear dependence on  $m_{W'}$ which stems from the linear dependence of the endpoint position in the  $p_{\perp}^{\ell}$  distribution

Sensitivity to  $m_W$  expressed through the slope in each  $(p_{\perp,\min}^{\ell}, p_{\perp,\min}^{\ell}, p_{\perp,\max}^{\ell})$  window

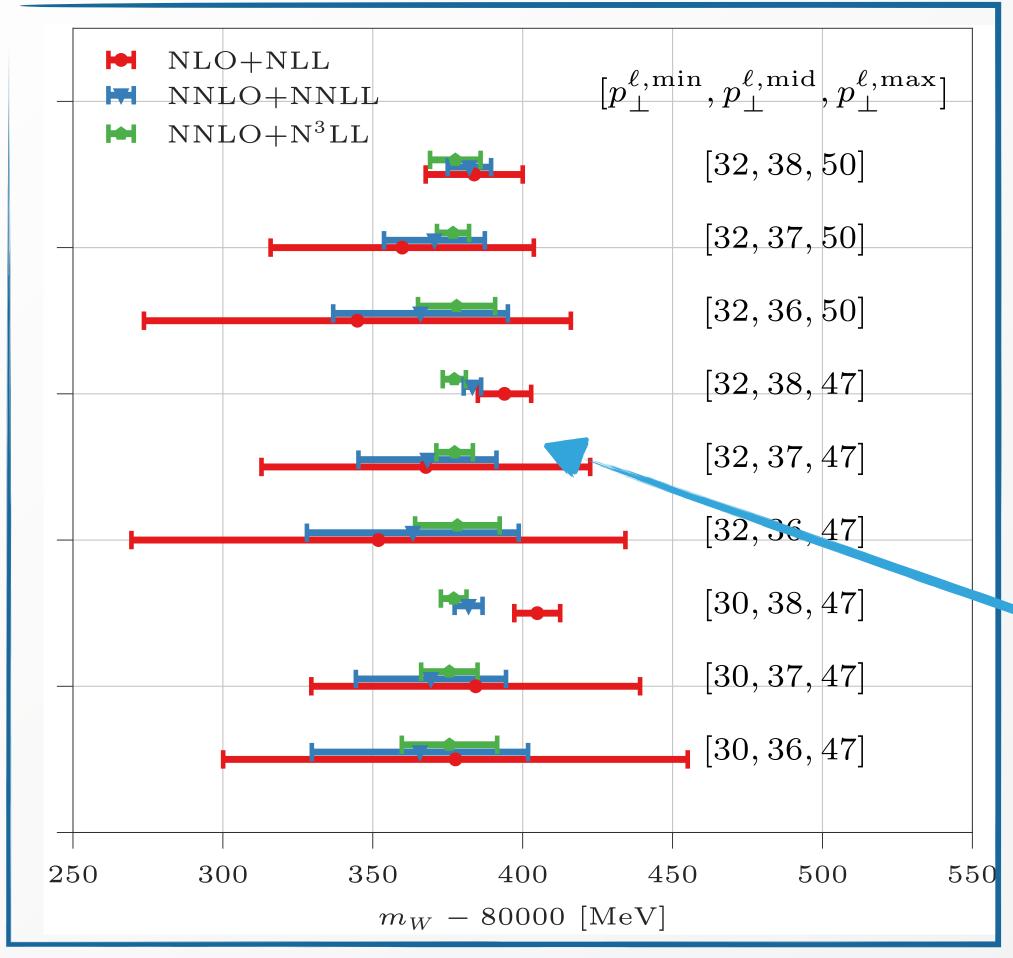
Slope **independent** on the QCD approximation

Bin size  $\mathcal{O}(10 \,\text{GeV})$  has threefold advantage

- 1. Small statistical error
- 2. Perturbative stability of the QCD result
- 3. Unfolding to particle level viable

Experimental result and theoretical predictions can be directly compared by looking at the intersection between the lines

## The jacobian asymmetry $\mathscr{A}_{p_1^\ell}$ and its theoretical uncertainty



[LR, P. Torrielli, A. Vicini '23]

For each interval choice the QCD scale-variation band determines a given  $m_W$  interval

N<sup>3</sup>LL corrections play an important role in reducing uncertainty band

We check the convergence order-by-order. If we observe convergence the size of the  $m_W$  interval provides an estimate of the QCD uncertainty

A perturbative QCD uncertainty at the  $\pm 5$  MeV level is achievable using CC DY data alone

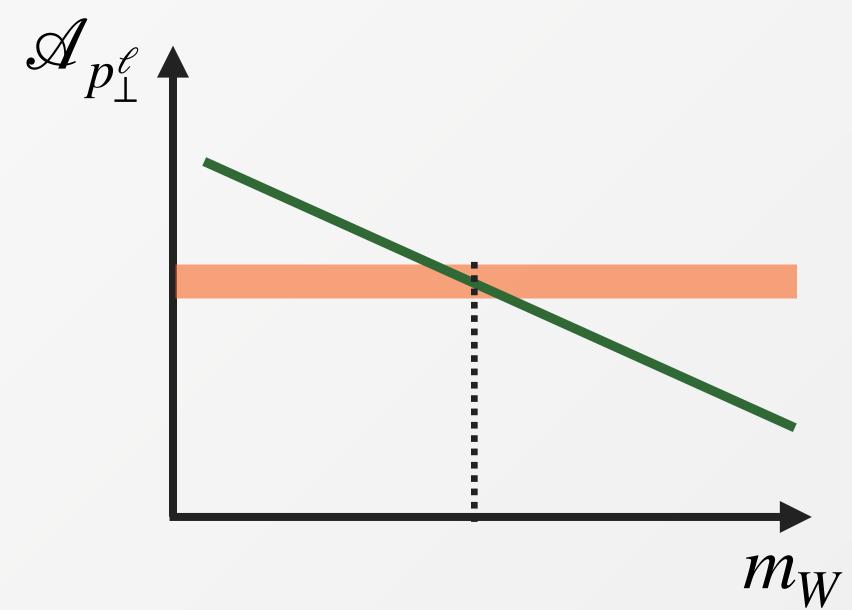
The choice of the midpoint is important to identify two regions with excellent QCD convergence (see regions with  $p_{\perp,\text{mid}}^{\ell} = 38 \,\text{GeV}$ )

# The jacobian asymmetry $\mathscr{A}_{p\ell}$ : additional effects and uncertainties

Excellent convergence properties of the asymmetry in perturbative QCD are a good starting point to discuss additional effects we did not include:

Impact on the central  $m_W$  value of

- missing perturbative corrections (QED, QCDxEW)
- non-perturbative effects



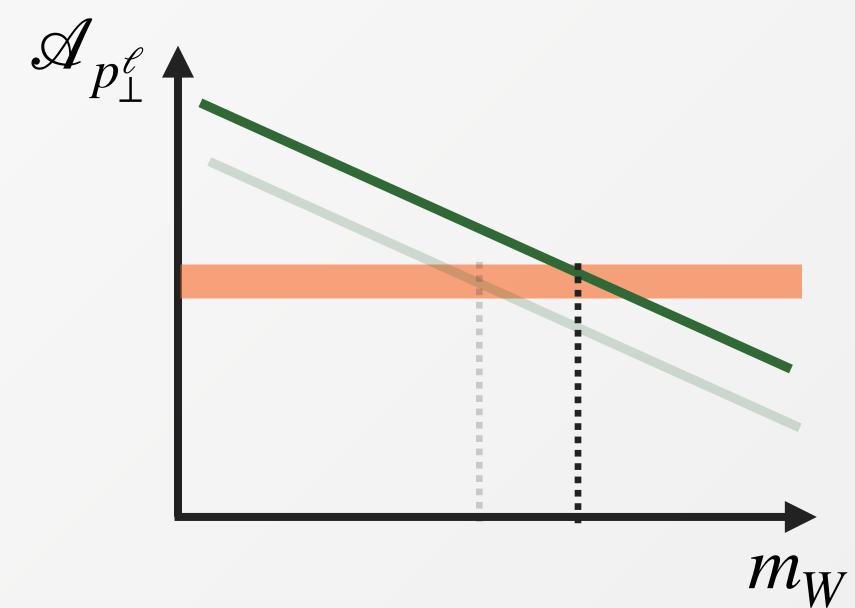
# The jacobian asymmetry $\mathscr{A}_{p_1^\ell}$ : additional effects and uncertainties

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Each effect yields a vertical offset on the asymmetry



# The jacobian asymmetry $\mathscr{A}_{p^{\ell}}$ : additional effects and uncertainties

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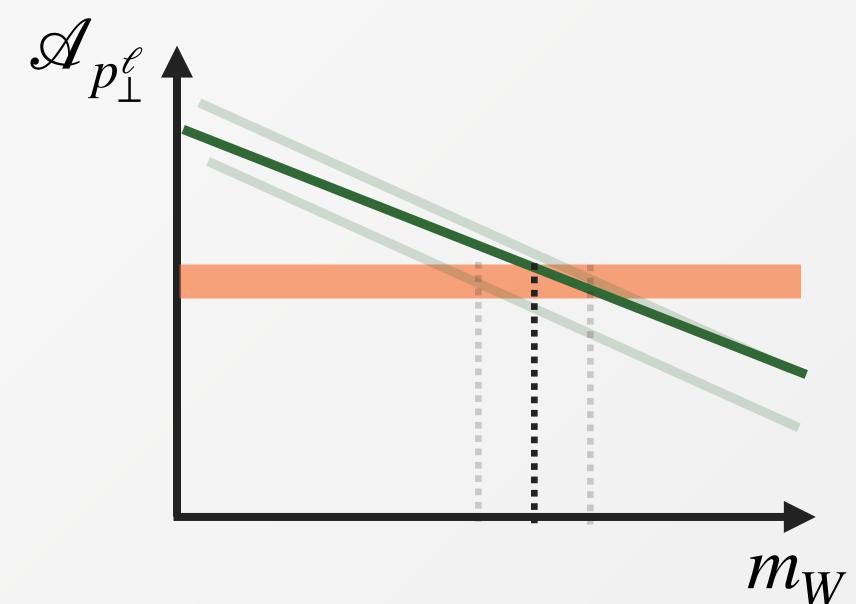
Impact on the central  $m_W$  value of

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Each effect yields a vertical offset on the asymmetry

QED corrections might also change the shape

 $\rightarrow$  shift on  $m_W$ 



# The jacobian asymmetry $\mathscr{A}_{p_1^{\ell}}$ : additional effects and uncertainties

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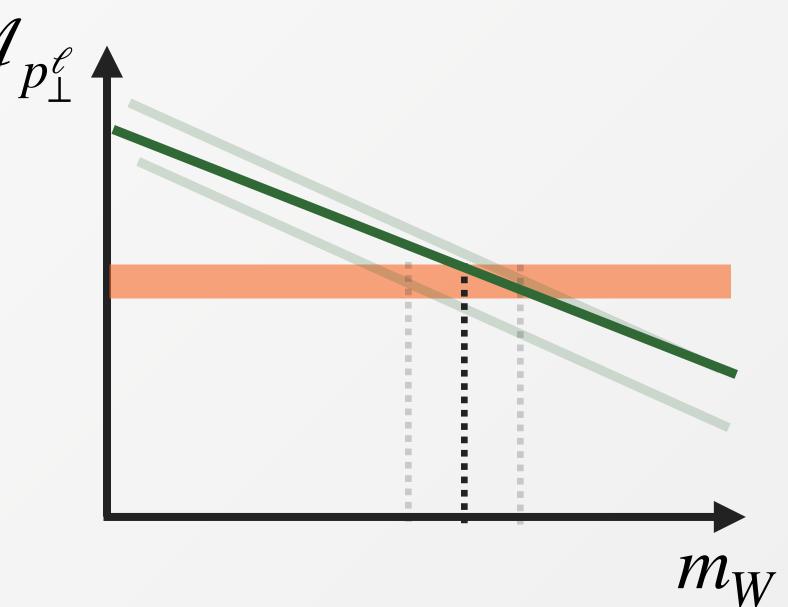
QED corrections might also change the shape

 $\rightarrow$  shift on  $m_W$ 

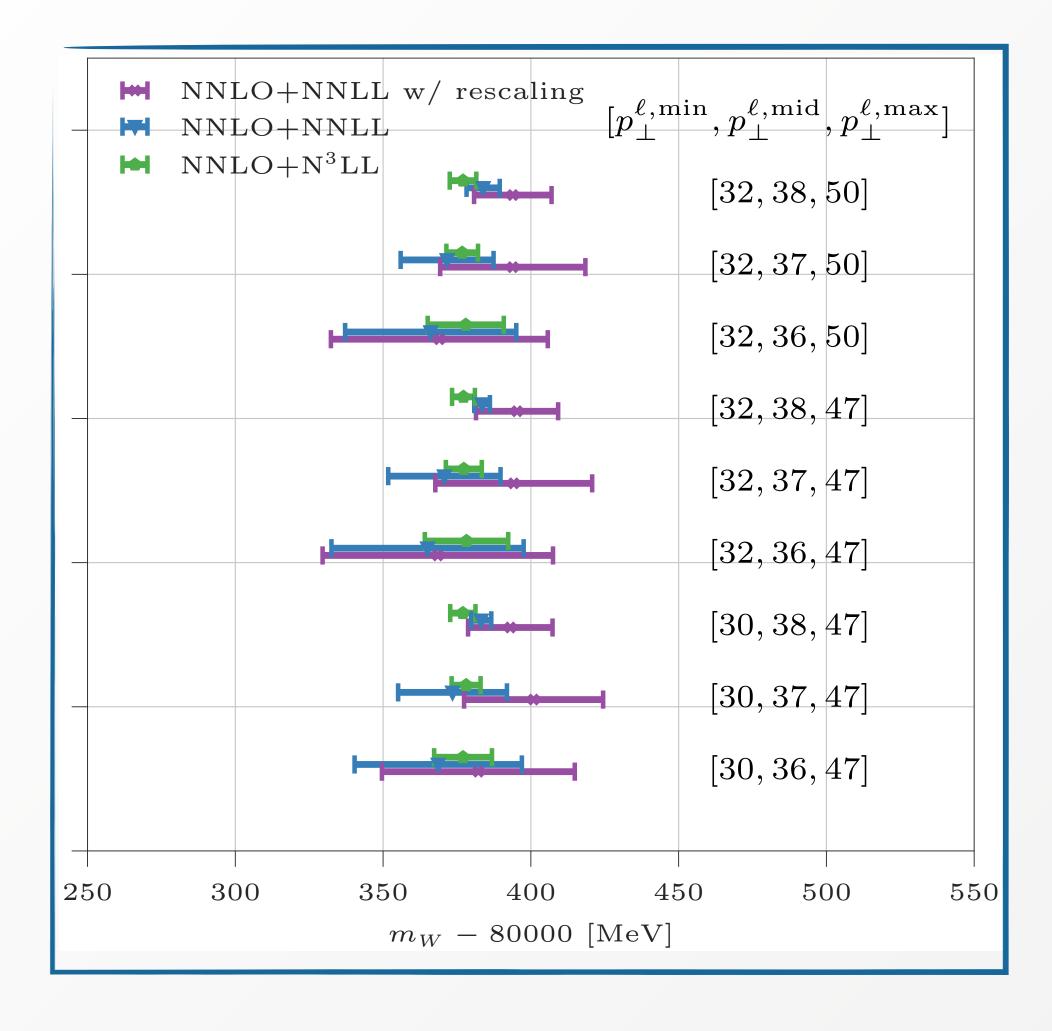
Impact of non-perturbative corrections expected to reduce when using NNLO+N<sup>3</sup>LL predictions with respect to results with lower accuracy: interplay of NP QCD model and perturbative accuracy

Parton distribution functions are an additional source of theoretical uncertainty

Linearity of the dependence on  $m_W$  allows an easy propagation of each uncertainty source



### Information transfer from NCDY to CCDY



NNLO+NNLL taken as our theory model

NNLO+N<sup>3</sup>LL with central scales as our MC truth

- pseudo-data generated both for NCDY and CCDY
- reweighting function computed from NNLO+NNLL to the pseudo-data in NC
- same reweighing function applied in CC DY

The  $p_{\perp}^{\ell \nu}$  and the  $p_{\perp}^{\ell}$  distributions get closer to the CCDY pseudodata but still maintain some shape differences

 $\rightarrow$  delicate to assume that  $p_{\perp}^{\ell \nu}$  rescaling

applies equally well to  $p_{\perp}^{\ell}$ 

Perturbative QCD uncertainty on  $m_W$ estimated with or without reweighing is of similar size

Usage of the highest available perturbative order is recommended to minimize the systematics in the transfer from *Z* to *W* 

### **Conclusion and outlook**

- Huge amount of theoretical work in the last few years in the computation of higher-order and accurate description of neutral and charged DY production
- Future measurement of  $m_W$  should exploit these computation for a reliable estimates of the theoretical uncertainties
- Shape of the  $p_T^{\ell}$  distribution and presence of the Jacobian peak motivates the definition of a scalar **observable** which **maximises the sensitivity** on *m*<sub>*W*</sub> and has several advantages
  - excellent pQCD convergence
  - large linear dependence on  $m_W \rightarrow$  sensitivity for a precision measurement
- uncertainty at the  $\pm 5$  MeV level is achievable using CC DY data alone

corrections (QCD resummation, mixed QCD and QED corrections), which now allows for a precise

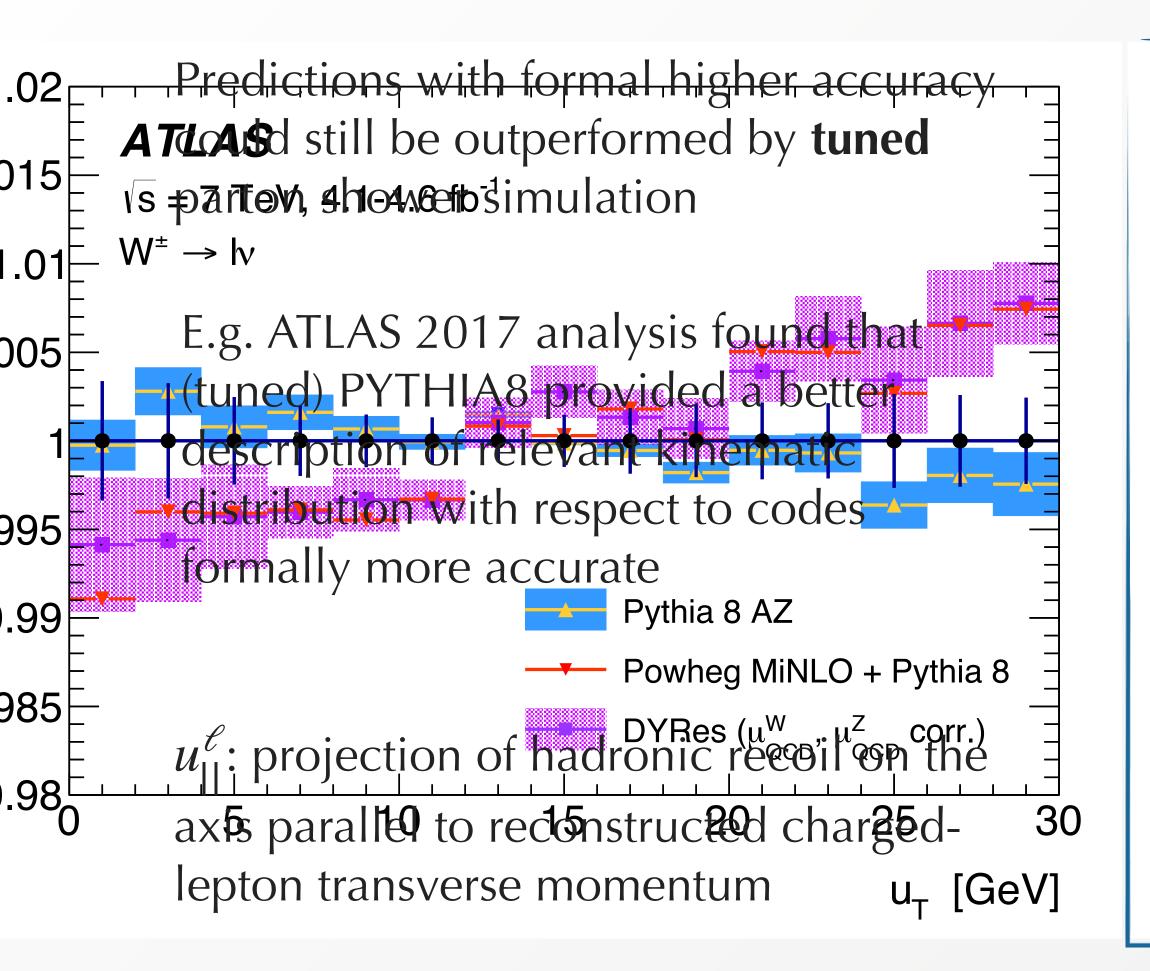
- possibility to unfold the data to particle level → simplicity in a global combination

• Determination at the ±15 MeV level from the experimental side seems possible; perturbative QCD

• For the future: thorough phenomenological study, including all the available SM radiative corrections

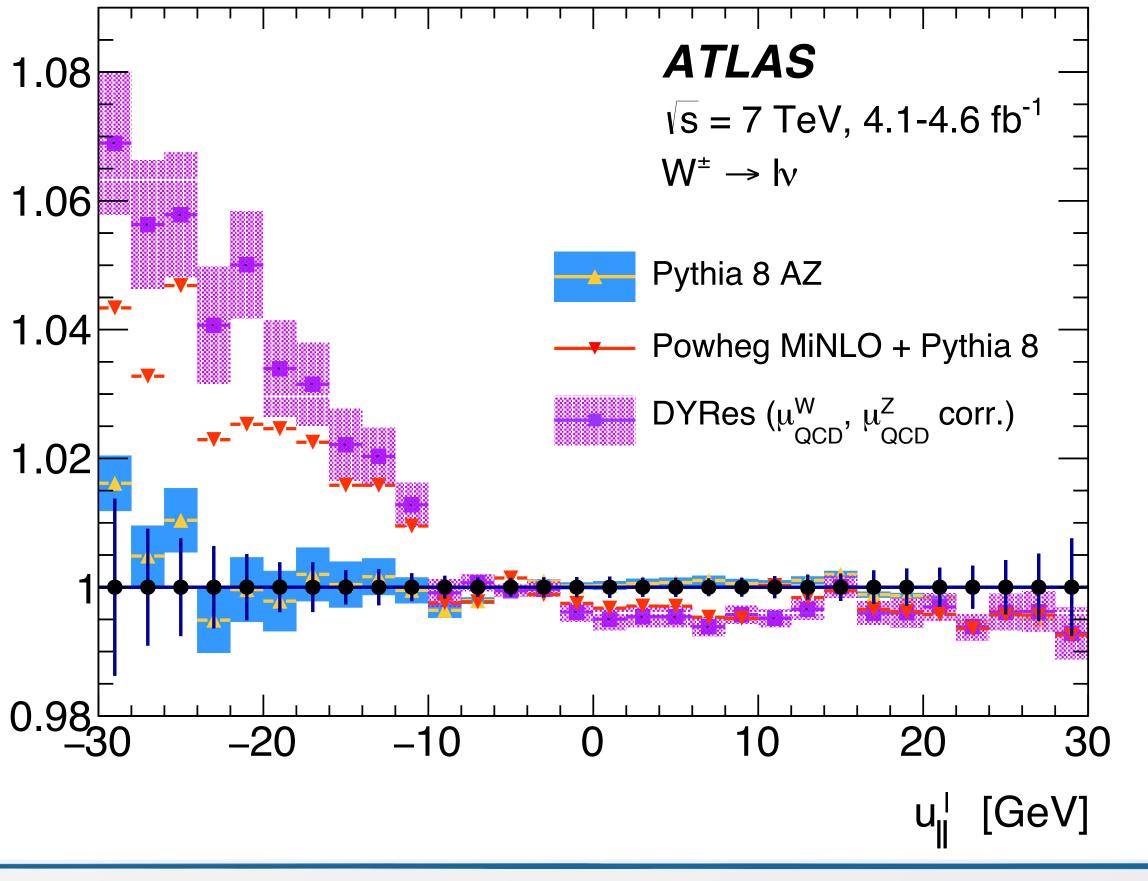


## Description of experimental data

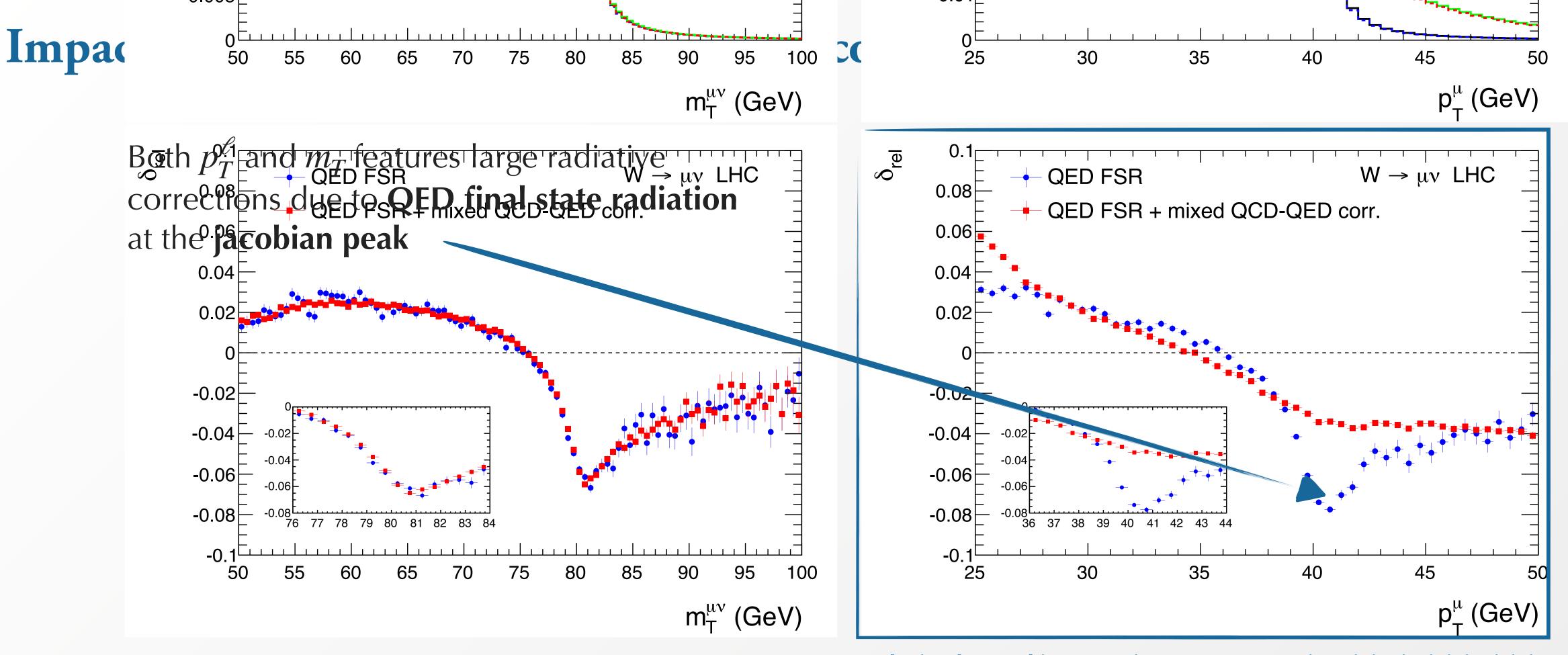


/ Data

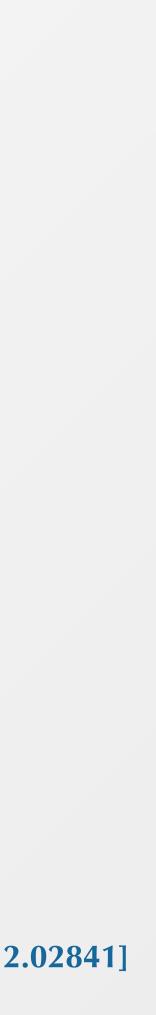
Pred.

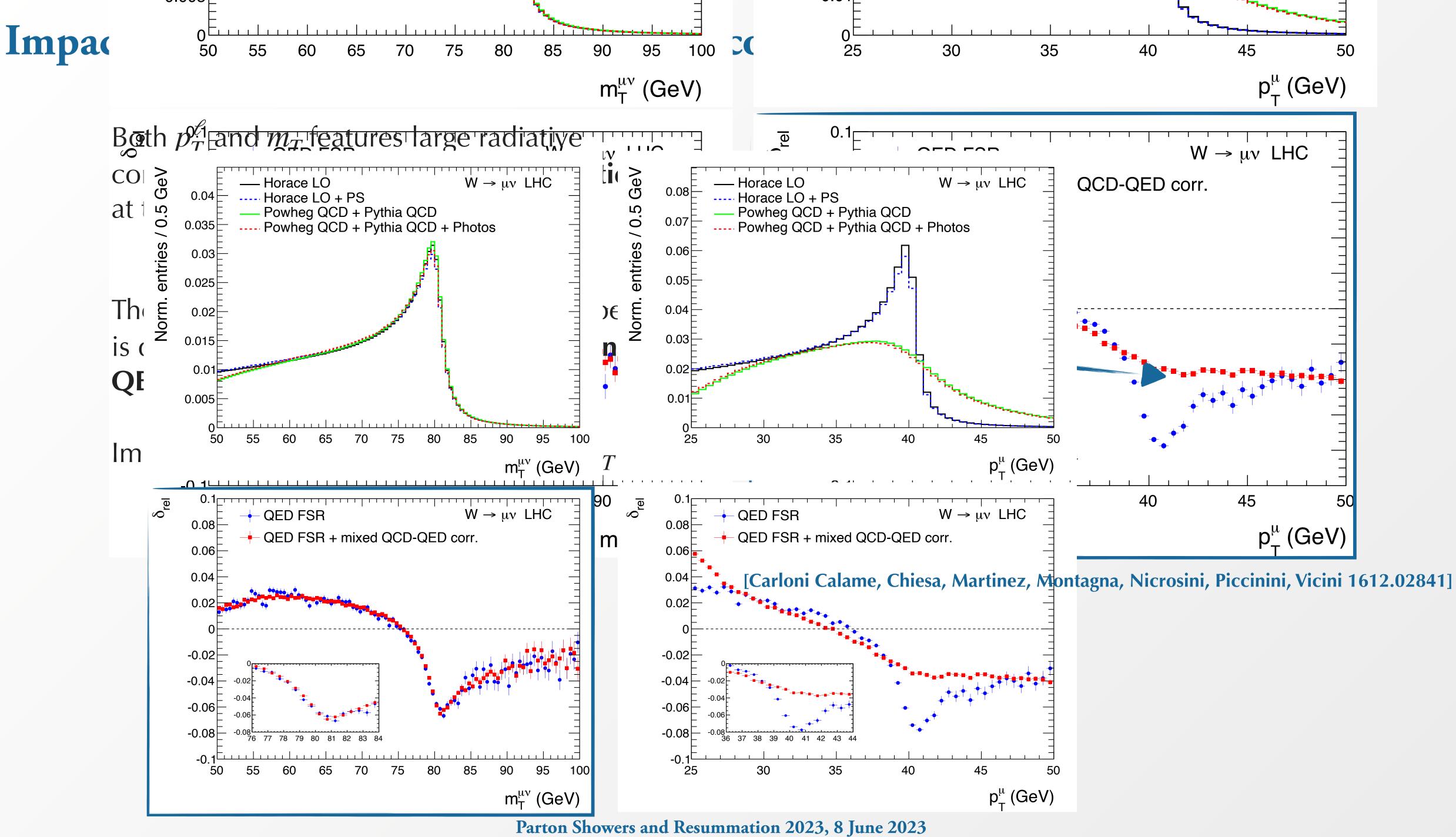


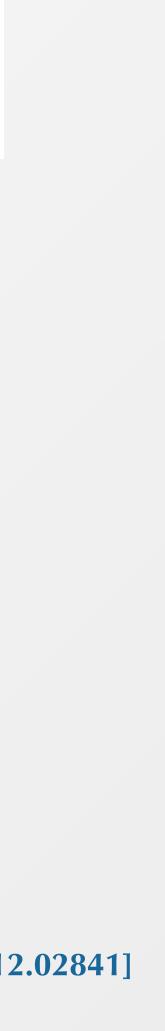
[ATLAS '17]



[Carloni Calame, Chiesa, Martinez, Montagna, Nicrosini, Piccinini, Vicini 1612.02841]







### Impact of QED and mixed QCD×QED corrections

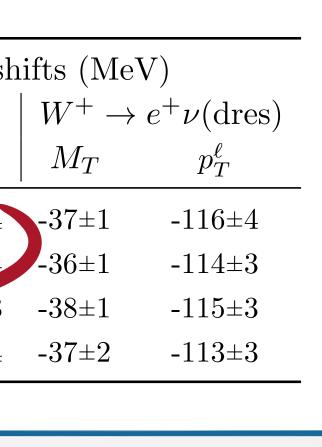
### Largest shifts induced by **QED FSR**

Subleading EW effects induce few MeV shifts

	$p\bar{p} \rightarrow W^+, \sqrt{s} = 1.96 \text{ TeV}$	$M_W$ shi				
Templates accuracy: NLO-QCD+QCD <sub>PS</sub>				$W^+ \to \mu^+ \nu$		
	Pseudodata accuracy	QED FSR	$M_T$	$p_T^\ell$		
1	$NLO-QCD+(QCD+QED)_{PS}$	Рутніа	-91±1	-308±4 -282±4		
2	$NLO-QCD+(QCD+QED)_{PS}$	Pнотоз	-83±1	$-282 \pm 4$		
3	$\text{NLO-}(\text{QCD+EW})\text{-two-rad} + (\text{QCD+QED})_{\text{PS}}$	Pythia	$-86 \pm 1$	-291±3		
4	$\text{NLO-}(\text{QCD+EW})\text{-two-rad}+(\text{QCD+QED})_{\text{PS}}$	Рнотоз	$-85 \pm 1$	$-290 \pm 4$		

[Carloni Calame, Chiesa, Martinez, Montagna, Nicrosini, Piccinini, Vicini 1612.02841]

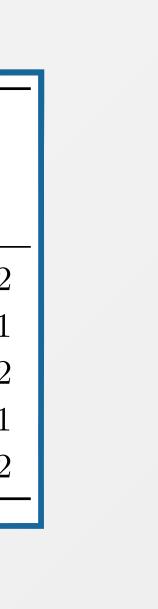
	$pp \to W^+, \sqrt{s} = 14 \text{ TeV}$	$M_W$ shifts (MeV)				
	Templates accuracy: LO		$W^+ \to \mu^+ \nu$		$W^+ \to e^+ \nu$	
	Pseudo-data accuracy	$M_T$	$p_T^\ell$	$M_T$	$p_T^\ell$	
1	HORACE only FSR-LL at $\mathcal{O}(\alpha)$	-94±1	$-104 \pm 1$	$-204 \pm 1$	$-230\pm2$	
2	HORACE FSR-LL	$-89 \pm 1$	$-97 \pm 1$	$-179 \pm 1$	$-195 \pm 1$	
3	HORACE NLO-EW with QED shower	$-90{\pm}1$	$-94{\pm}1$	$-177 \pm 1$	$-190\pm2$	
4	HORACE $FSR-LL + Pairs$	$-94{\pm}1$	$-102 \pm 1$	$-182 \pm 2$	$-199 \pm 1$	
5	Рнотоs FSR-LL	$-92 \pm 1$	$-100\pm 2$	-182±1	$-199 \pm 2$	



Analyses do include the bulk of the QCDxQED corrections

The impact on the  $m_W$  shifts of the mixed QCDXQED corrections strongly depends on the underlying QCD model

Note: in this approach non-factorizable contributions are neglected







## Progress in mixed QCD×EW corrections

Complete set of corrections to neutral and charged current Drell-Yan production recently obtained by two groups NNLO QCD-EW corrections to charged-current DY (2-loop contributions in pole approximation).

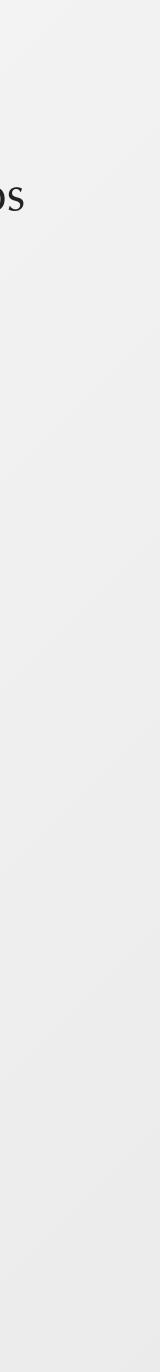
[Buonocore, Grazzini, Kallweit, Savoini, Tramontano 2102.12539]

exact NNLO QCD-EW corrections to neutral-current DY [Bonciani, Buonocore, Grazzini, Kallweit, Rana, Tramontano, Vicini, 2106.11953] [Armadillo, Bonciani, Devoto, Rana, Vicini 2201.01754] [Buccioni, Caola, Chawdhry, Devoto, Heller, von Manteuffel, Melnikov, Röntsch, Signorile-Signorile 2203.11237]

Impact of mixed  $\mathcal{O}(\alpha_s \alpha)$  corrections estimated to be potentially relevant for  $\mathcal{O}(10 \text{ MeV})$  extraction at the LHC [Behring, Buccioni, Caola, Delto, Jaquier, Melnikov, Röntsch 2103.02671]

Matching of such corrections to QCD and QED all-order resummation of high relevance for accurate and precise analysis of the  $p_T^{\ell}$  distribution

Combination of QCD+QED resummation so far available only for Z/W production without decays [Autieri, Cieri, Ferrera, Sborlini '18, '23]



### Understanding the Z and W correlations

Thanks to the availability of theoretical prediction at high accuracy, it is possible to assess reliably the behaviour of the perturbative series for crucial observables such as  $p_T^Z/p_T^W$  ratio

$$\frac{1}{\sigma^{W}} \frac{d\sigma^{W}}{p_{\perp}^{W}} \sim \frac{1}{\sigma_{\text{data}}^{Z}} \frac{d\sigma_{\text{theory}}^{Z}}{\sigma_{\text{theory}}^{Z}} \frac{p_{\perp}^{W}}{p_{\perp}^{U}}$$

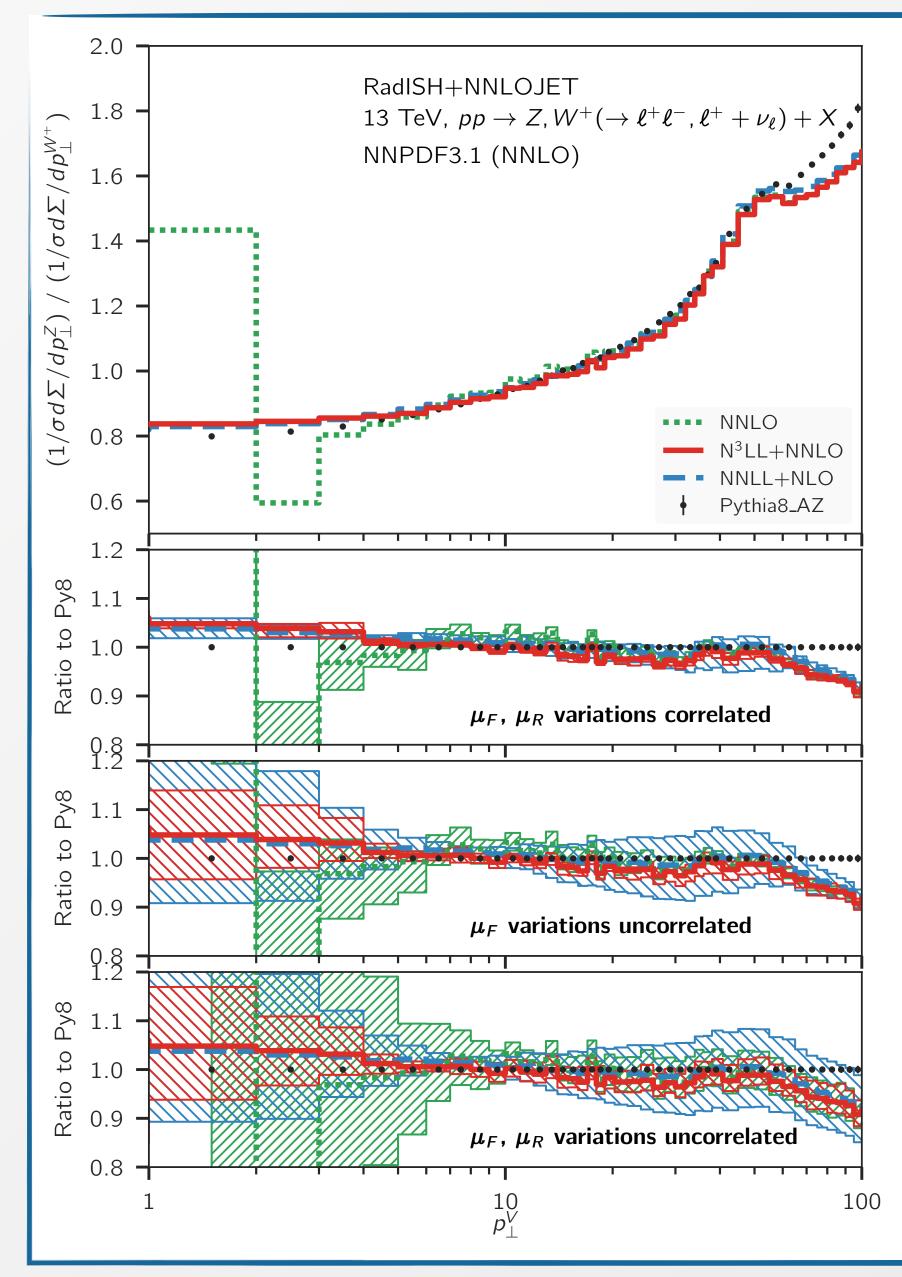
Stability of the ratio indicates high level of correlation between the two spectra

Comparison with tuned event generator such as **PYTHIA\*** however indicates that full correlation might be too strong an assumption

\* "PYTHIA is not QCD"

[Kirill Melnikov, QCD@LHC 2016]

[Bizon, de Ridder, Gehrmann, Glover, Huss, Chen, Monni, Re, <u>LR</u>, Walker, 1905.05171] Parton Showers and Resummation 2023, 8 June 2023





### **CDF** measurement and theoretical accuracy

CDF II measurement features very aggressive estimates for theory uncertainties, especially when compared to CDF I results with lower luminosity, as all the errors are reduced by a factor 2-3

$p_T(W)$ model	5
Parton distributions	10
QED radiation	4

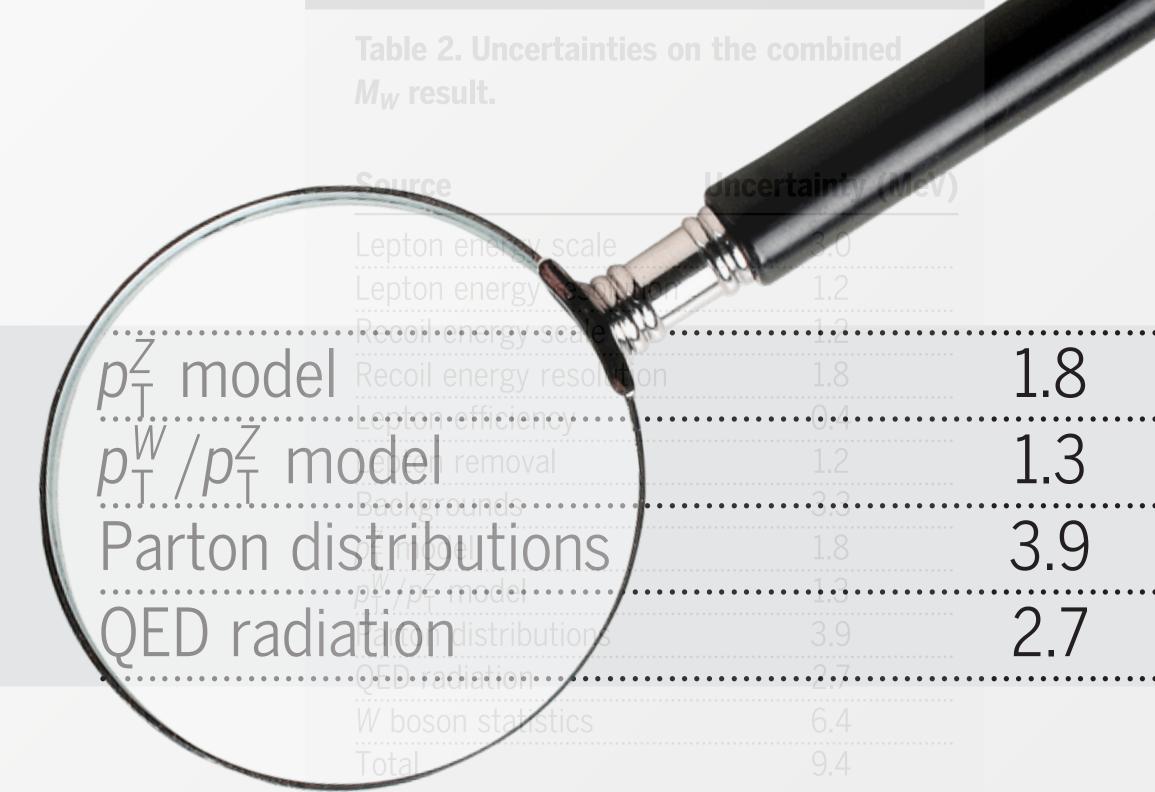
[CDF collaboration, 1203.0275]

CDF II, 2.2 fb<sup>-1</sup>  $m_W = 80.387 \pm 19$ (2012)

Do these error reflect the **improved theoretical understanding** of Z/W production at hadron colliders?

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CDF II, 8.8 fb<sup>-1</sup>  $m_W = 80.433 \pm 9$ (2022)



### **CDF** measurement and theoretical accuracy

**Not really**: despite being published 10 years apart, the two analyses share most of the same underlying **theoretical model** 

### CDF II, 2.2 fb<sup>-1</sup> (2012)

**ResBos** (private '03 version) [Balasz, Yuan '97] (N)NLL<sub>QCD</sub>+NLO<sub>QCD</sub> CTEQ6.6 NLO PDFs QED modelling with PHOTOS+HORACE

> Reduction of the theoretical error obtained via additional data constraint and use of more modern PDF sets

> > Parton Showers and Resummation 2023, 8 June 2023



### CDF II, 8.8 fb<sup>-1</sup> (2022)

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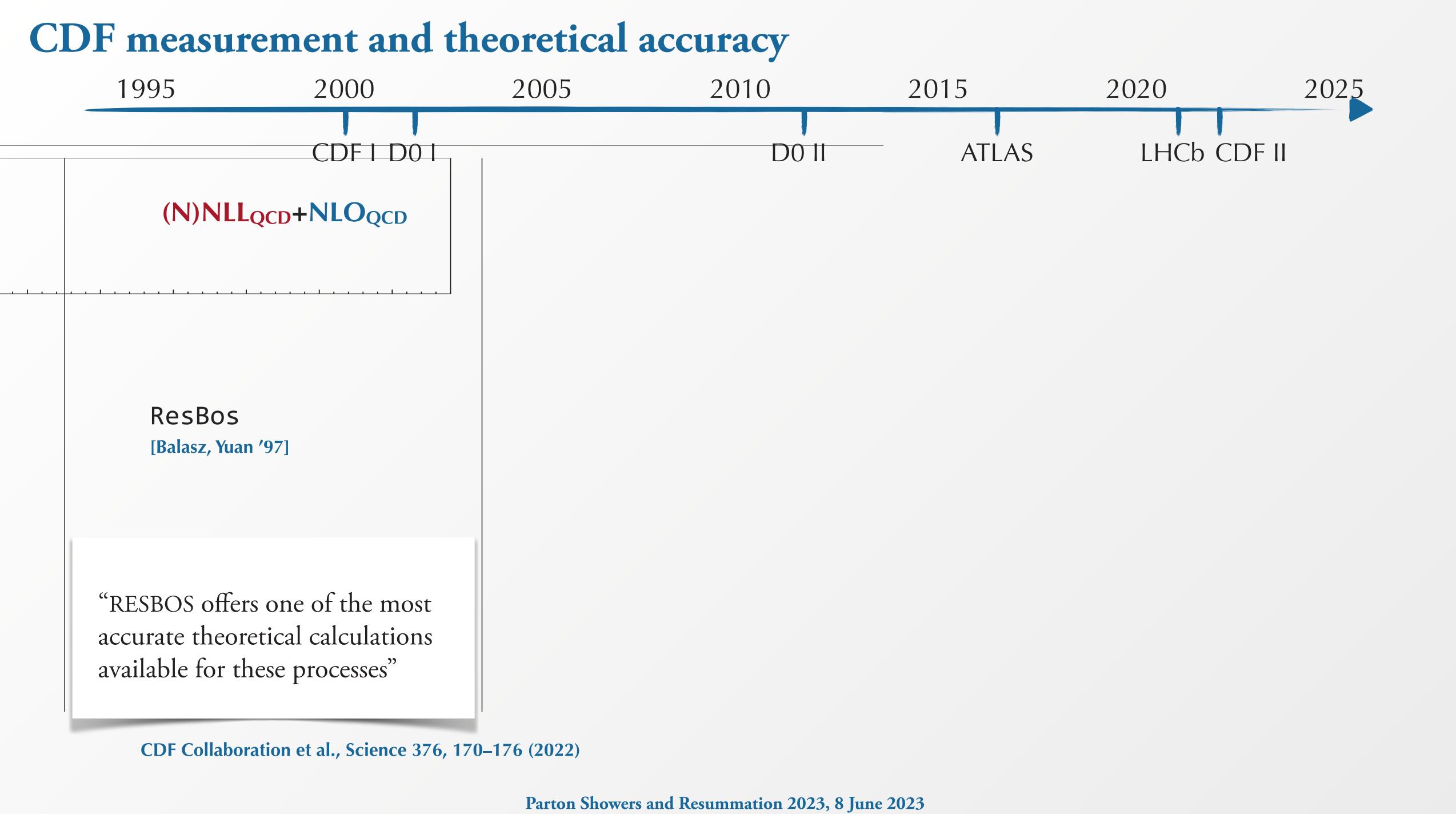
### **CDF measurement and theoretical accuracy** 1995 2000 2005 2010

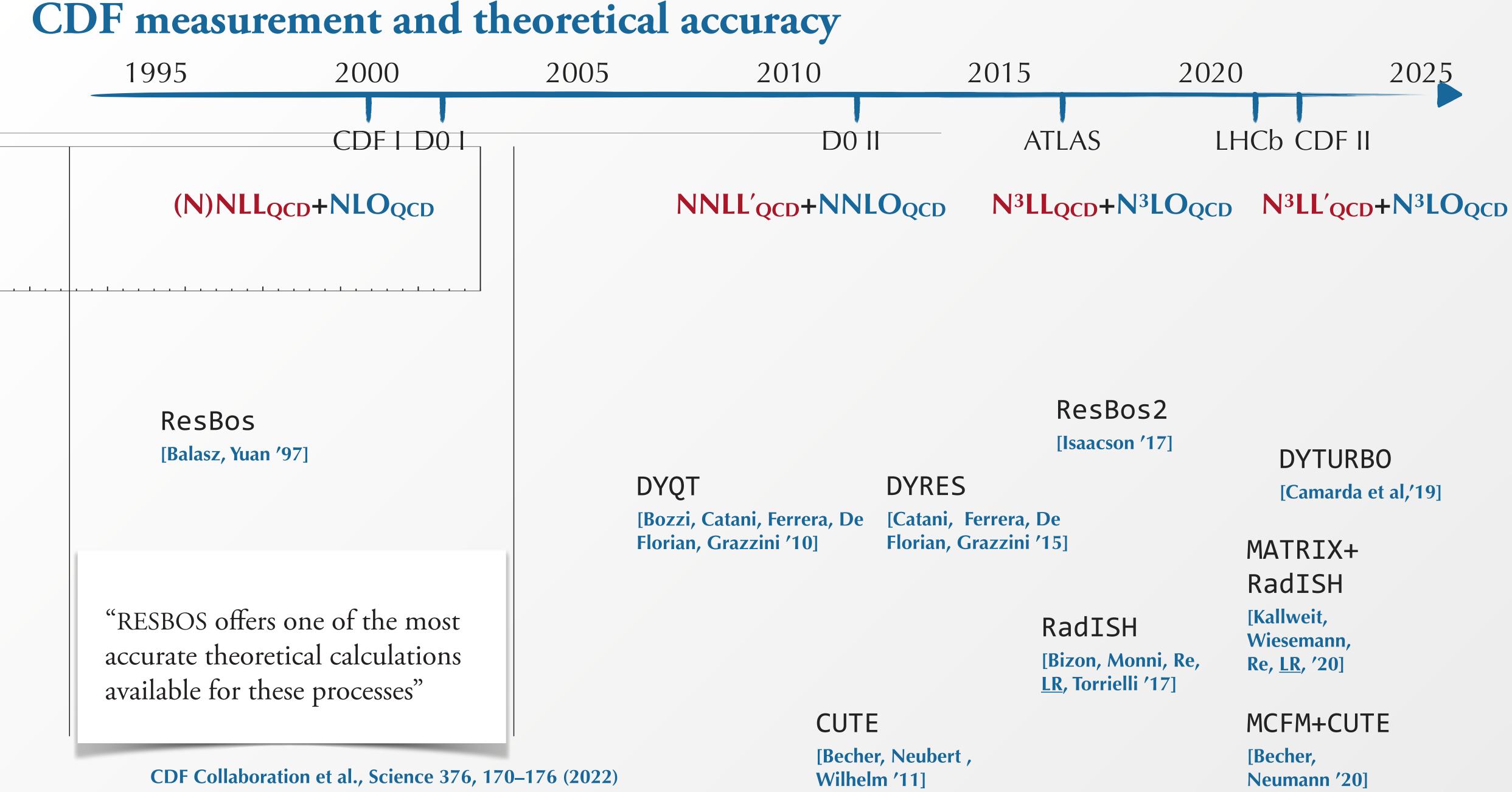
# 1995 2000 2005 CDFID01

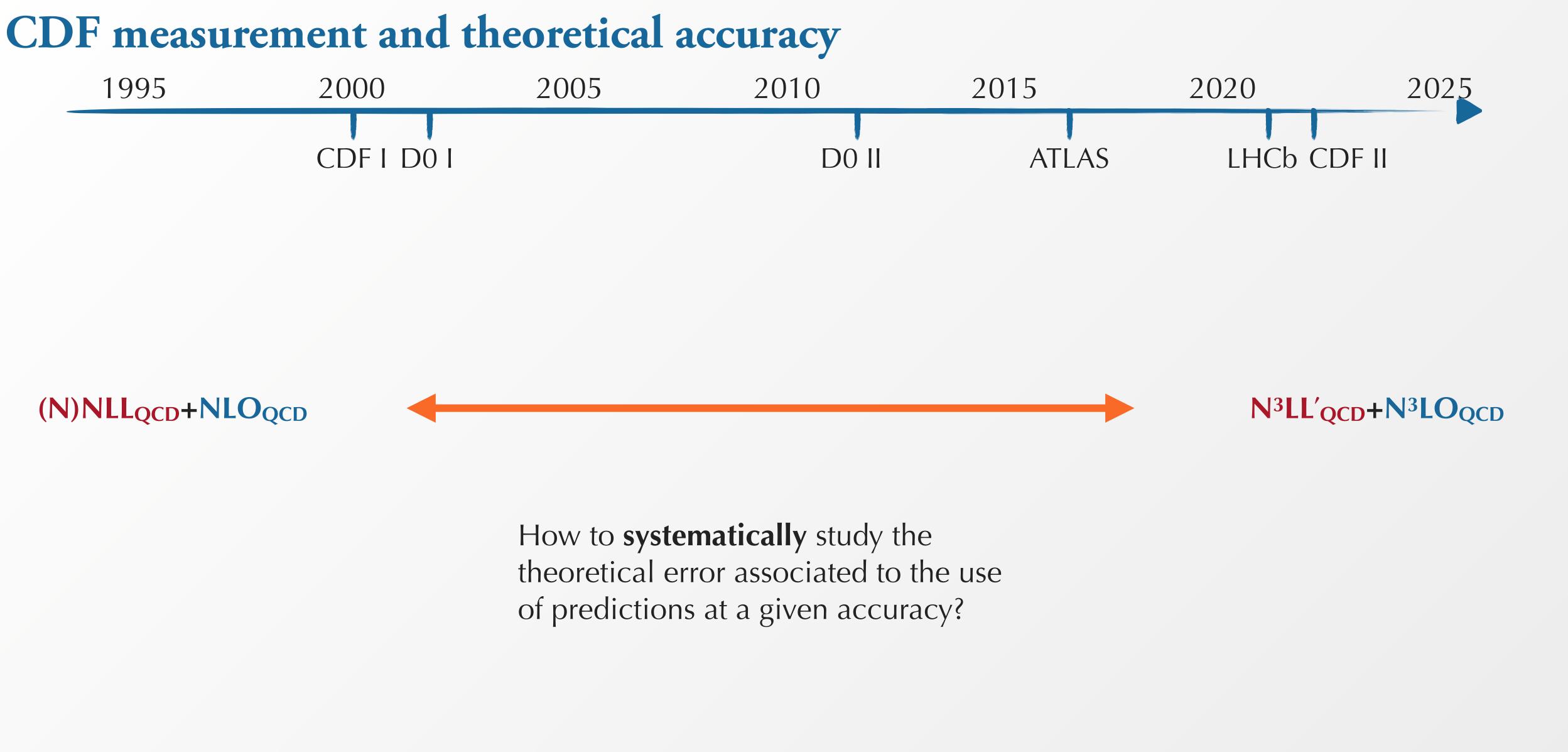
### (N)NLL<sub>QCD</sub>+NLO<sub>QCD</sub>



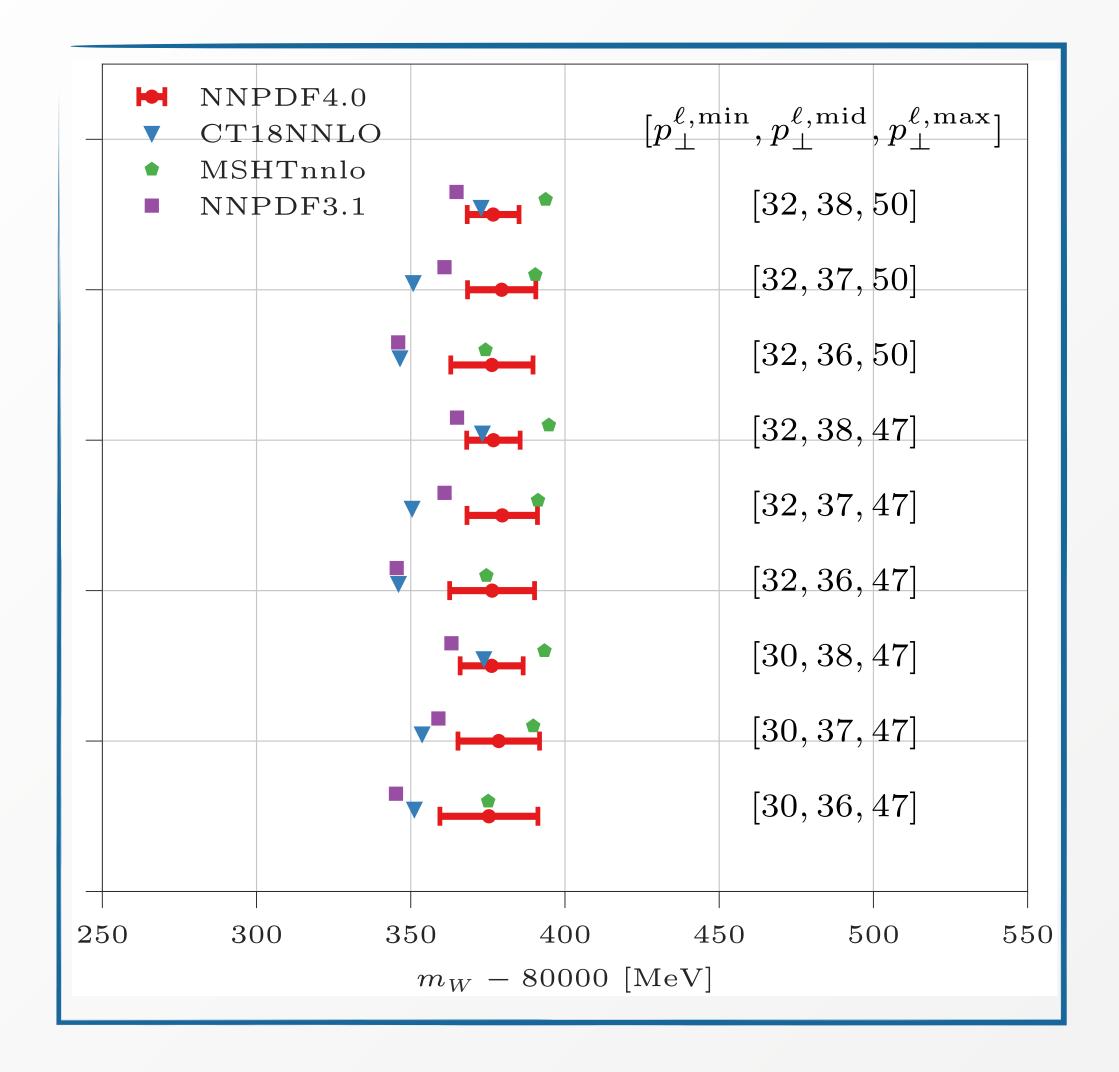








### The lepton transverse momentum distribution in CC DY



PDF uncertainties on  $m_W$  evaluated conservatively using the 100 replicas of the NNPDF4.0 set at NLO+NLL

$$\delta m_W = \pm 11 \,\mathrm{MeV}$$

Spread of the central values of CT18NNLO, MSHTnnlo, NNPDF4.0 of  $\sim 30 \,\mathrm{MeV}$ 

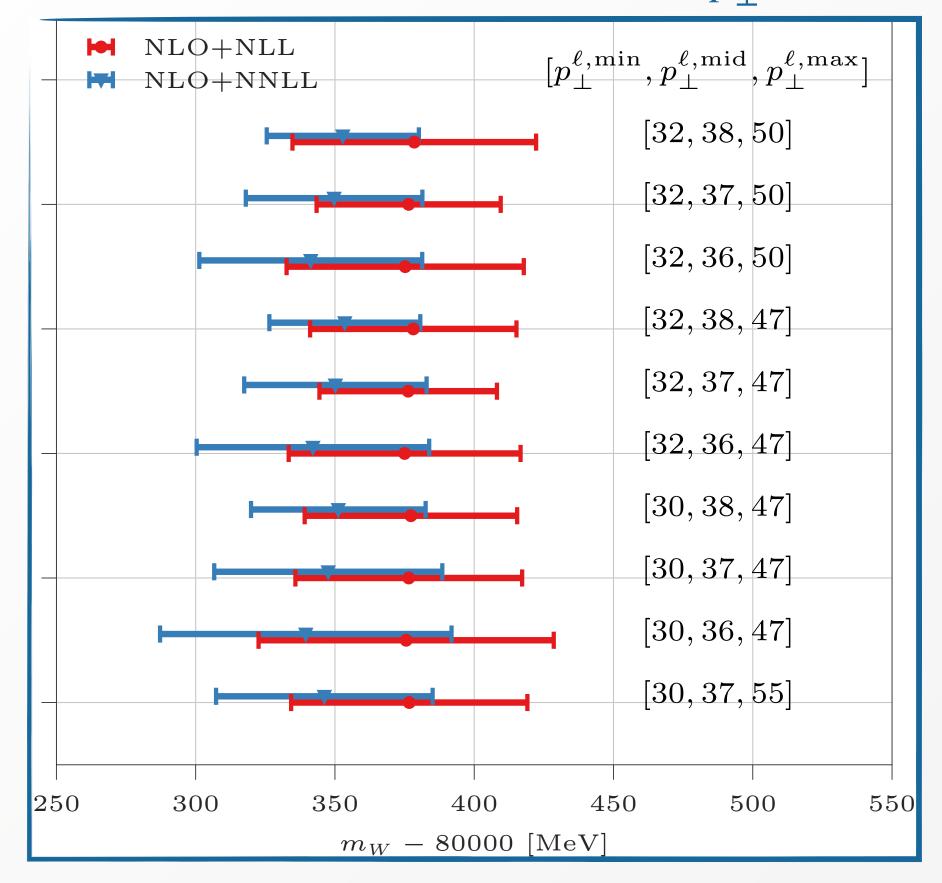
Size of the uncertainty expected, as the asymmetry is a single scalar observable particularly sensitive to PDF variations

More information needed to mitigate PDF uncertainty, e.g. profiling using additional bins of the  $p_{\perp}^{\ell}$  distribution

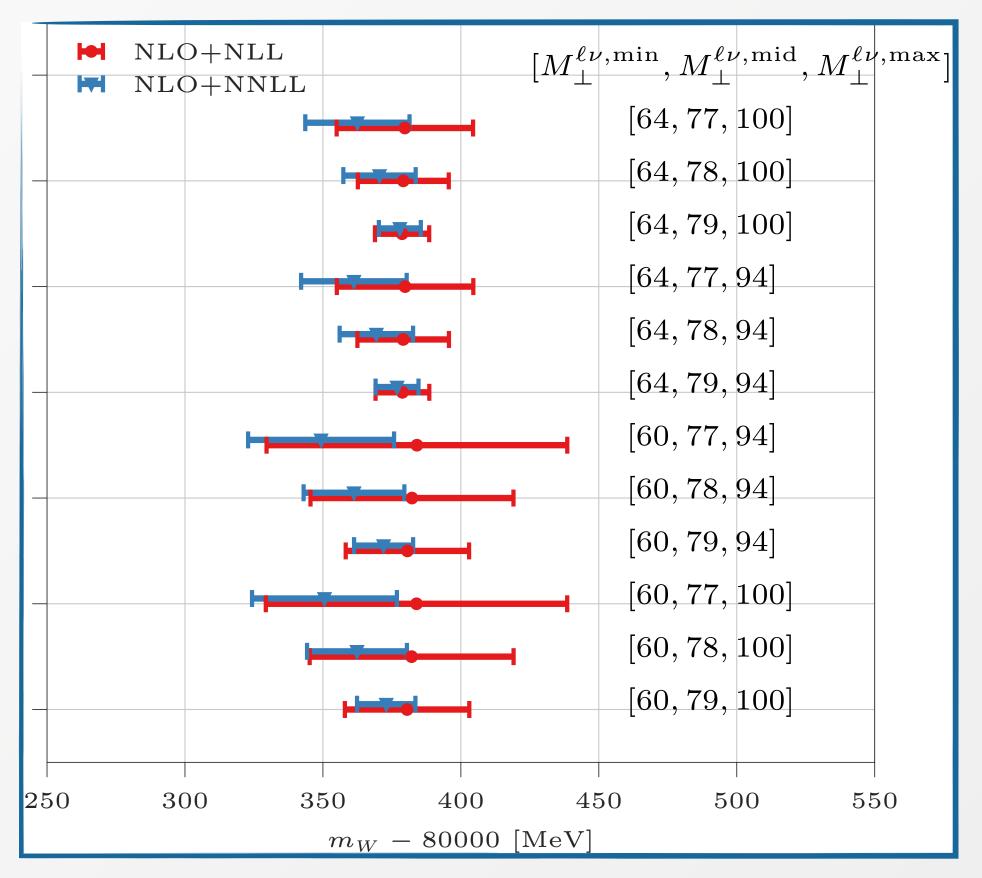
PDF uncertainty can be reduced to the few MeV level thanks to the strong anti correlated behaviour of the two tails of  $p_{\perp}^{\ell}$ 



## The jacobian asymmetry $\mathscr{A}_{p_1^\ell}$ and its theoretical uncertainty



Asymmetry good starting point to investigate size of the QCD uncertainty at a given accuracy (**without tuning**) QCD uncertainty at lower accuracy considerably larger than state-of-the-art predictions for  $p_{\perp}^{\ell}$ (more than ±30 MeV at Tevatron, CDF kinematics for some combinations) QCD uncertainties can be smaller for transverse mass but still notably larger than those quoted by CDF See also [Isaacson, Fu, Yuan 2205.02788] [CERN-LPCC-2022-06]



### **PDFs and their uncertainties**

Uncertainties related to PDFs can have different origin:

- Uncertainty propagated from the statistical and systematic errors on the measurements used in their determination (canonical "**PDF uncertainty**")
- Theoretical uncertainties of the predictions used in PDF fits, such as missing higher order uncertainty: these are starting to be addressed only recently, and are typically not included in the nominal PDF uncertainty [Abdul Khalek, Ball, LR, et al, (NNPDF Coll.), 1905.04311] [J. McGowan, T. Cridge, L. Harland-Lang, R. Thorne (MSHT Coll.) 2207.04739]

encompasses the envelope of various PDF sets

- Comparisons between different groups used to assess sources of methodological uncertainty in the PDF extraction
- $m_W$  measurements typically include the nominal PDF uncertainty and, more conservatively, they also assess that it

### **PDFs and their uncertainties**

Numerous studies on the impact of PDF uncertainties have been performed at both colliders [Tevatron 0707.0085,0708.3642,0908.0766,1203.0275,1203.0293,1307.7627] [Bozzi, Citelli, Rojo, Vesterinen, Vicini 1104.2056, 1501.05587, 1508.06954] [ATLAS 1701.07240] [Kotwal PRD 98, 033008] [Manca, Cerri, Foppiani, Rolandi 1707.09344] [Bianchini, Rolandi 1902.03028] [Farry, Lupton, Pili, Vesterinen, 1902.04323] [Bagnaschi, Vicini 1910.04726] [Hussein, Isaacson, Huston 1905.00110] [Gao, Liu, Xie 2205.03942]

The relative size of PDFs uncertainties at the Tevatron and at the LHC is affected by the different centre-of-mass energy of the collision and the **different initial states** 

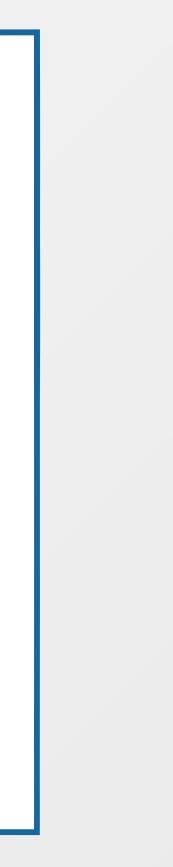
PDFs uncertainties **not an obstacle at Tevatron**; they have long been considered a limiting factor at the **LHC** due to the smaller values of the partonic *x* probed (higher collider energy) and the larger contribution from the second quark generation

Latest generation of NNPDF parton densities (large number of LHC datasets included, new machinelearning based methodology) achieves substantial **reduction** of PDF uncertainty

 $\sqrt{s} = 13 \text{ TeV}$ 1.20 1.15 1.10 1.05  ${\cal L}_{ar{S}{\cal C}}$ 1.00 0.95 0.90 0.85 NNPDF4.0 0.80  $10^{1}$  $10^{2}$  $10^{3}$  $M_{x}$ 

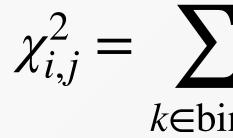
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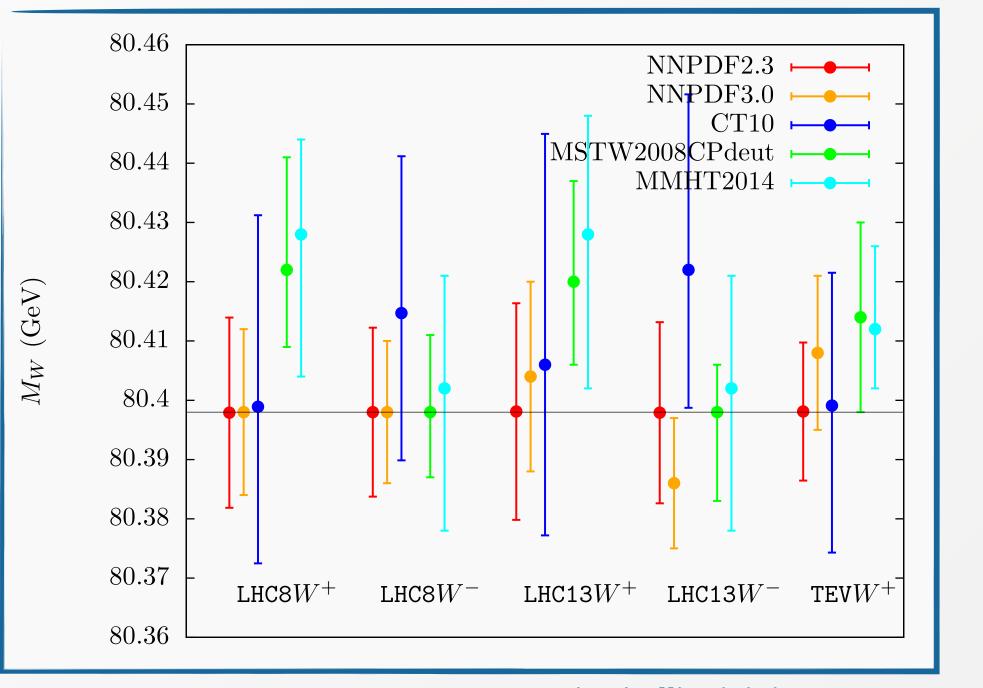


### PDFs and their uncertainties: template fits

PDF-induced uncertainty typically computed by generating templates with a given PDF member *i* for various values of  $m_W$ , and subsequently fitting all other members *j* defining a proper figure of merit



Once the preferred value for m<sub>W</sub> for each member has been determined by minimising the figure of merit, compute PDF-induced uncertainty



[Bozzi, Citelli, Vicini 1501.05587]

$$\frac{(T_k^j - D_k^i)^2}{\sigma_k^2}$$

PDF uncertainties with this strategy are **relatively** large at the LHC, with a resulting uncertainty larger than 10 MeV and considerably large spreads between different PDF sets

Cfr. ~ 4 MeV quoted by CDF II with NNLO PDFs

4 MeV also claimed by CDF II to be the shift between NNPDF3.1 NNLO and ~15 years old NLO CTEQ6.6 PDFs



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CERN - Geneva

cuts. We are thus able to sum the contributions of MANY SMALL sources which were absent in previous studies and which can, in the sum, yield a sizeable result. These are the "many roads" of the title. [This concern, that many small numbers can yield a large sum, was colourfully voiced at the meeting by G. Altarelli who described his vision of a mixture of small effects -- the Altarelli cocktail -- leading to the observed signal.] Before proceeding to the

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THE STANDARD MODEL AND MISSING E OR

THE MANY ROADS TO PARADISE

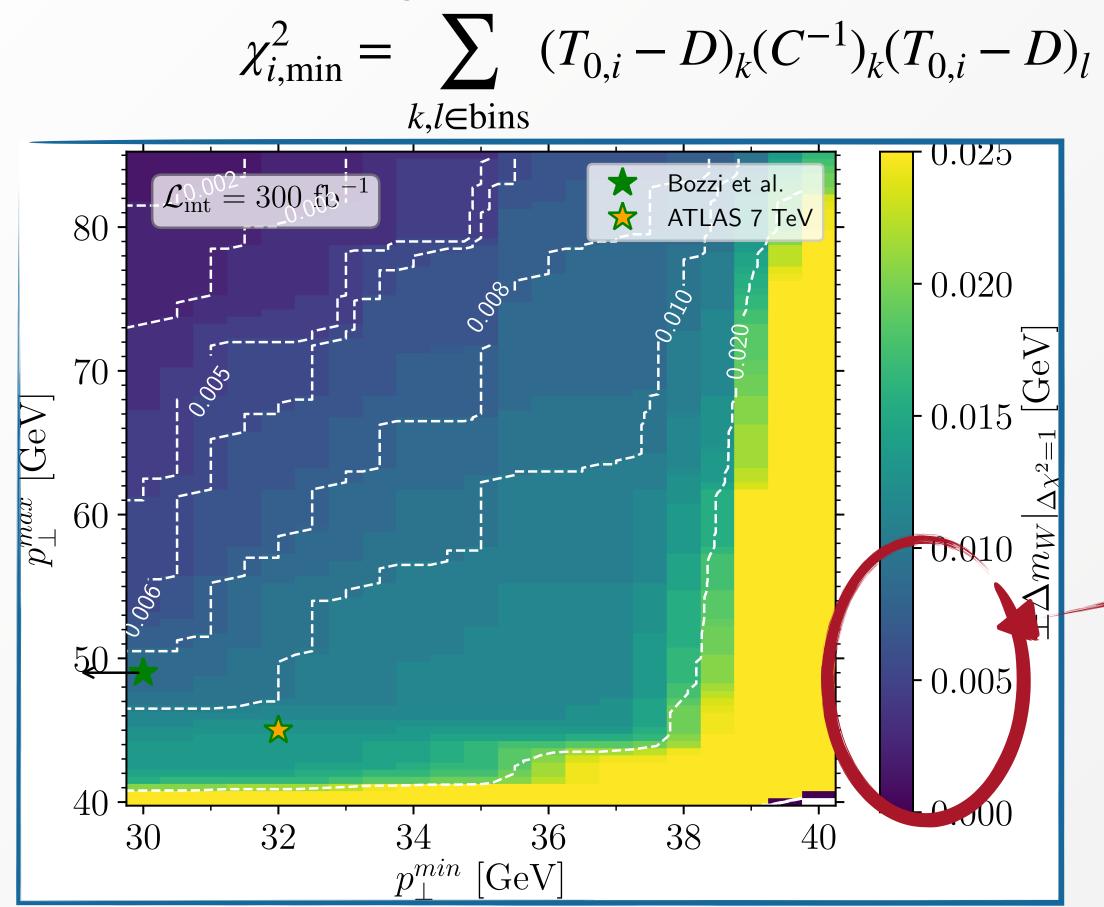
Stephen D. Ellis<sup>#</sup>

### PDFs and their uncertainties: bin-by-bin correlations

**Bin-by-bin correlations** between PDF replicas can be taken into account inserting the information about PDFs in the covariance matrix

$$(\Sigma_{\rm PDF})_{ij} = \langle (\mathcal{T} - \langle \mathcal{T} \rangle_{\rm PDF})_i (\mathcal{T} - \langle \mathcal{T} \rangle_{\rm PDF})_j \rangle_{\rm PDFs}$$

Compute  $\chi^2$  using full covariance matrix in the definition

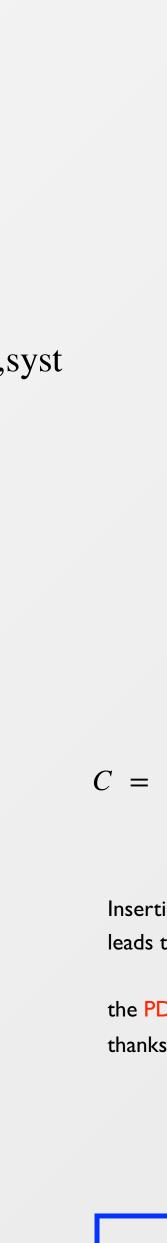


[Bagnaschi, Vicini 1910.04726]

$$\forall m_{W,i}$$
  $C = \Sigma_{\text{PDF}} + \Sigma_{\text{MC}} + \Sigma_{\text{stat}} + \Sigma_{\text{exp}},$ 

Inserting the information about PDFs in the covariance matrix leads to a profiling action given by the data

PDF uncertainty can be reduced to the **few MeV level** thanks to the **strong anti correlated Denaviour** of the two tails of  $n^{\ell}$ 



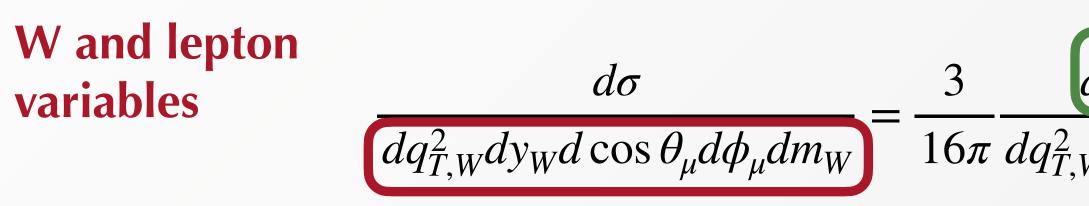
### Data-driven approach to m<sub>W</sub> extraction

A theory-agnostic extraction of  $m_W$ 

[E. Manca, PhD Thesis 2016; V. Bertacchi, Tesi di Perfezionamento 2021]

Exploit statistics collected by CMS during Run II at the LHC to extract the value of  $m_W$  simultaneously with  $q_T^W$ ,  $y_W$  and polarization spectra to obtain a statistically-dominated measurement of  $m_W$ 

Decoupling of the (unknown) production physics from the (known) decay physics



1. Decompose inclusive  $\eta^{\mu} \times p_{T}^{\mu}$  distribution in bins 2. Fit  $\eta^{\mu} \times p_{T}^{\mu}$  distribution measured on data 3. Unfolding from the sole lepton kinematics to the underling boson kinematics

### unpolarised cross section

$$\frac{d\sigma^{U+L}}{W^{d}W^{d}M_{W}}\left[(1+\cos^{2}\theta_{\mu})+\sum_{i=0}^{7}A_{i}P_{i}(\cos\theta_{\mu},\phi_{\mu})\right]$$
angular coefficients

s of 
$$m_{W'}$$
,  $Y_{W'}$ ,  $q_T^W$  for each  $P_i$