

Mass spectrum prediction in non-minimal supersymmetric models

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18.09.2014



Inhalt

① Einführung

Das Standardmodell der Teilchenphysik

Supersymmetrie

Berechnung des Massenspektrums

② Inhalt der Promotion

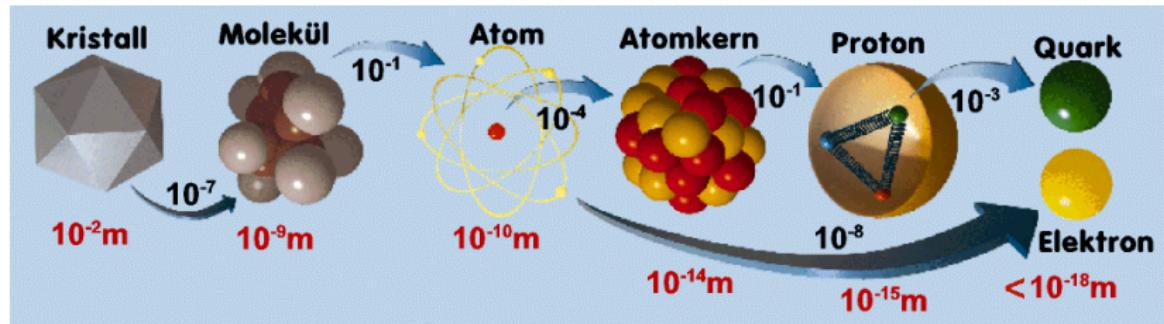
Berechnung von β_v

Genaueres Matching im E₆SSM

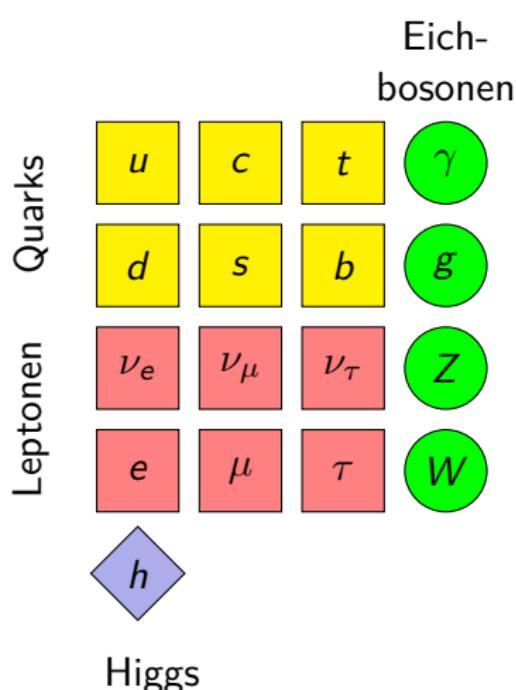
Neuer NMSSM-Spektrumgenerator

Allgemeiner SUSY-Spektrumgenerator-Generator

Die Bausteine der Natur



Das Standardmodell der Teilchenphysik



Beschreibt

- Quarks, Leptonen
- elektromagnetische, starke und schwache WW
- Higgsboson

Probleme:

- keine Gravitation
- keine Dunkle Materie

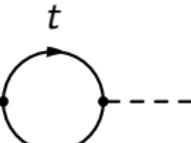
Schwachstellen:

- keine Vereinigung der WW
- Hierarchieproblem

Hierarchieproblem

Higgs-Masse:

$$m_h^2 = (m_h^{\text{tree}})^2 + \Delta m_h^2$$

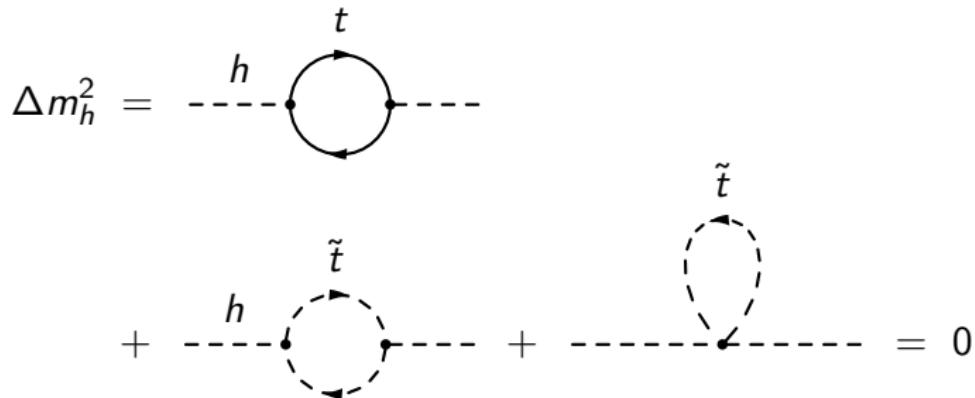
$$\Delta m_h^2 = \text{---} \xrightarrow{h} \text{---}$$


groß!

Hierarchieproblem

Higgs-Masse:

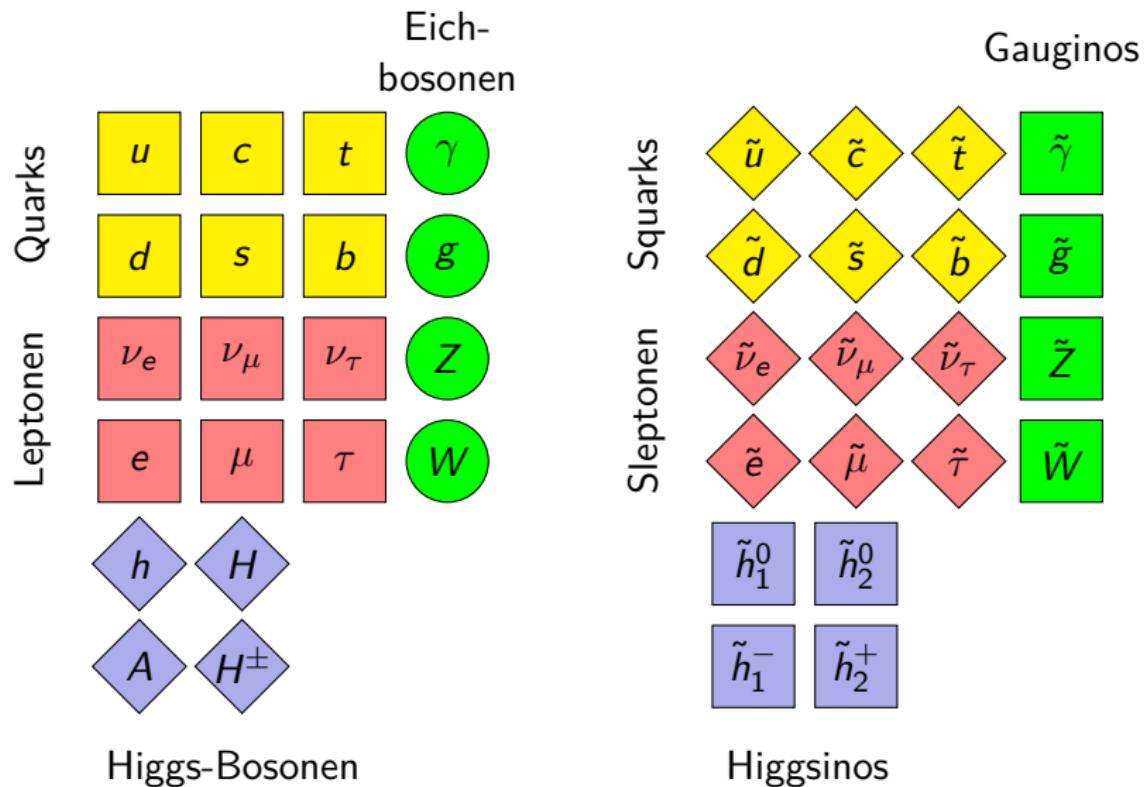
$$m_h^2 = (m_h^{\text{tree}})^2 + \Delta m_h^2$$

$$\Delta m_h^2 = -\frac{h}{t} \cdot \text{(top loop)} + \frac{h}{\tilde{t}} \cdot \text{(middle loop)} + \frac{\tilde{t}}{\tilde{t}} \cdot \text{(bottom loop)} = 0$$


falls $m_t = m_{\tilde{t}}$, $Q_t = Q_{\tilde{t}}$, $I_t = I_{\tilde{t}}$, $T_t = T_{\tilde{t}}$

⇒ **Supersymmetrie**

Minimales Supersymmetrisches Standardmodell (MSSM)



Brechung der Supersymmetrie

Problem: SUSY-Partner bisher nicht gefunden



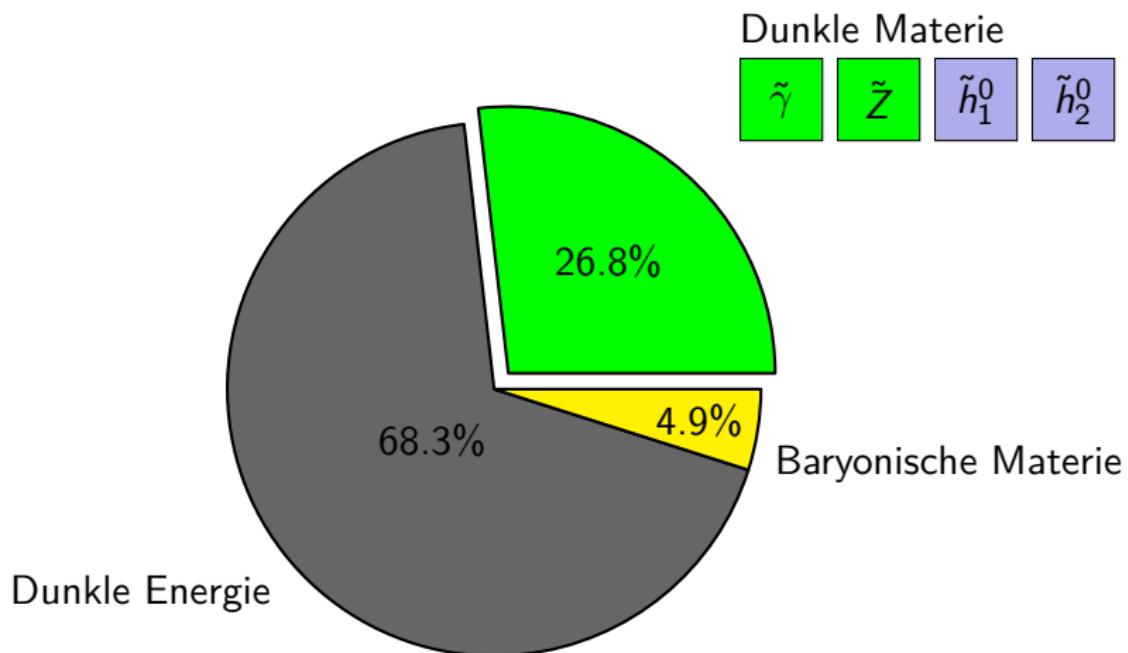
Supersymmetrie muss gebrochen sein!

$$m_{\tilde{t}} \gtrsim m_t$$

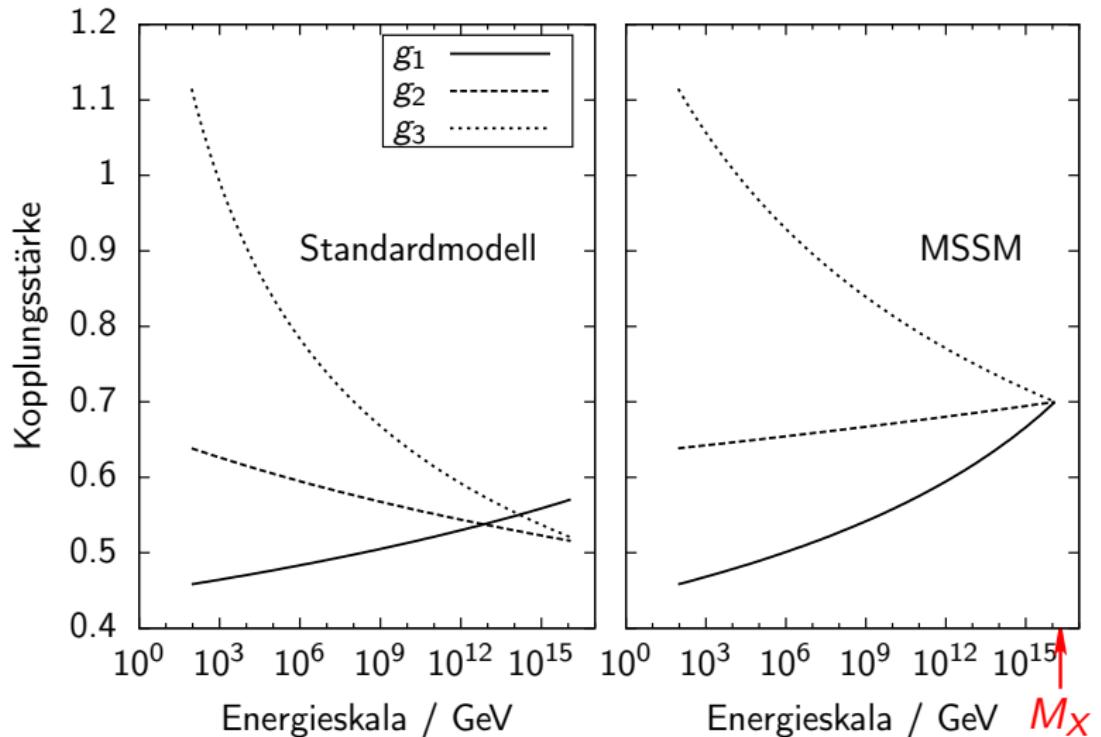
Stärke der Brechung parametrisiert durch:

$$m_0^2, \quad M_{1/2}, \quad A_0$$

Vorteil des MSSM: Dunkle Materie-Kandidat



Vorteil des MSSM: Eichkopplungsvereinigung



Schwachstelle des MSSM: μ -Problem

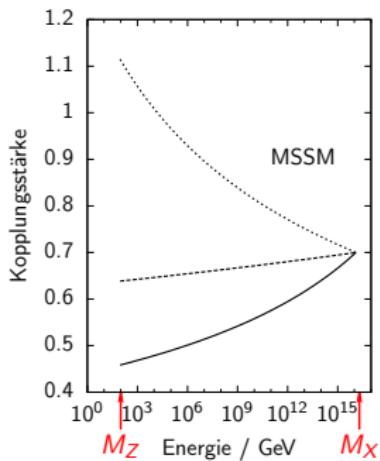
$$\mathcal{L}_{\text{MSSM}} = \mathcal{L}_{\text{Eich-WW}} + \int d^2\theta \left[\mu(H_1 H_2) + \text{Yukawa} \right]$$

μ hat seinen Ursprung an GUT-Skala

$$\Rightarrow \mu \sim M_X \sim 10^{16} \text{ GeV}$$

Aber andererseits: μ festgelegt durch Elektroschwache Symmetriebrechung (EWSB) an M_Z -Skala

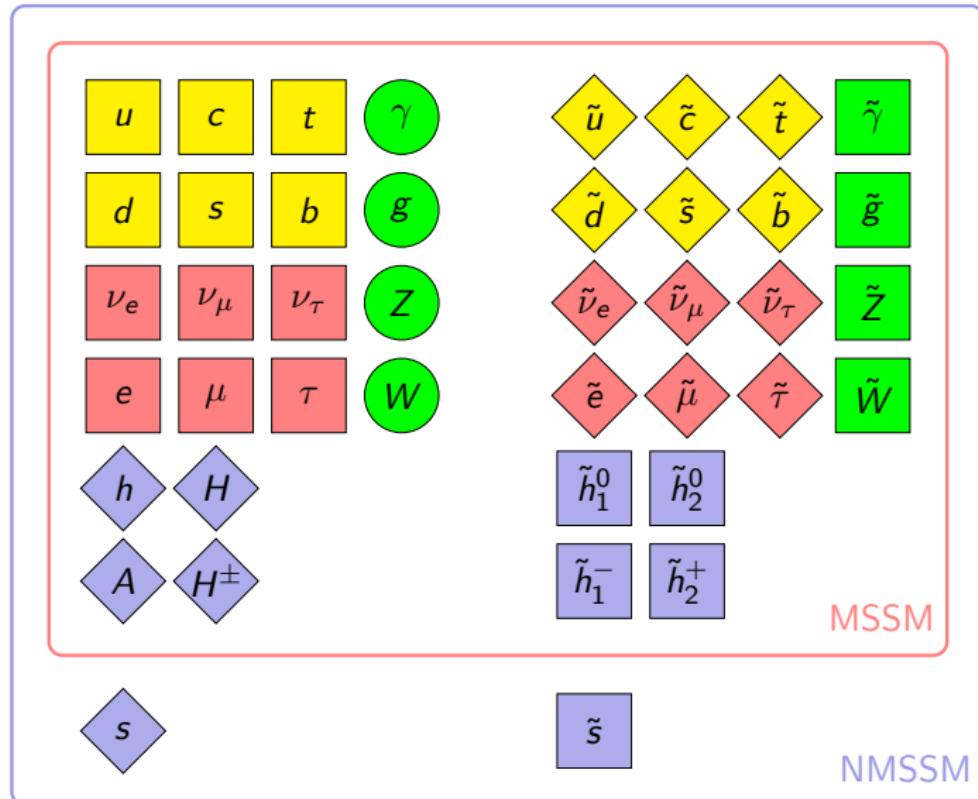
$$\Rightarrow \mu \sim M_Z \sim 10^2 \text{ GeV}$$



Lösung: μ ersetzen durch neues Higgs-Boson s

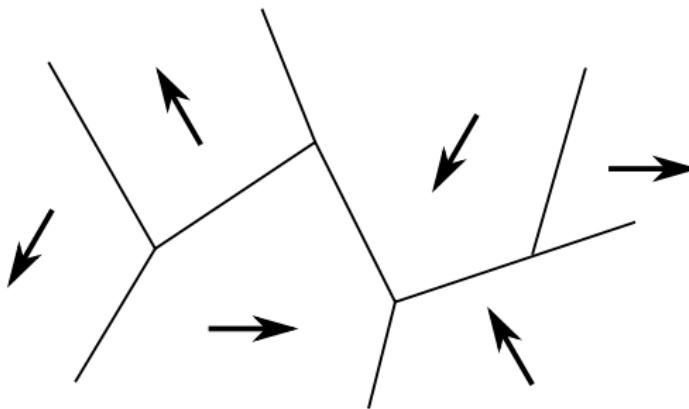
\Rightarrow Nächst-Minimales Supersymmetrisches Standardmodell (NMSSM)

Next-to-MSSM (NMSSM)



Problem des NMSSM: Domänenwände

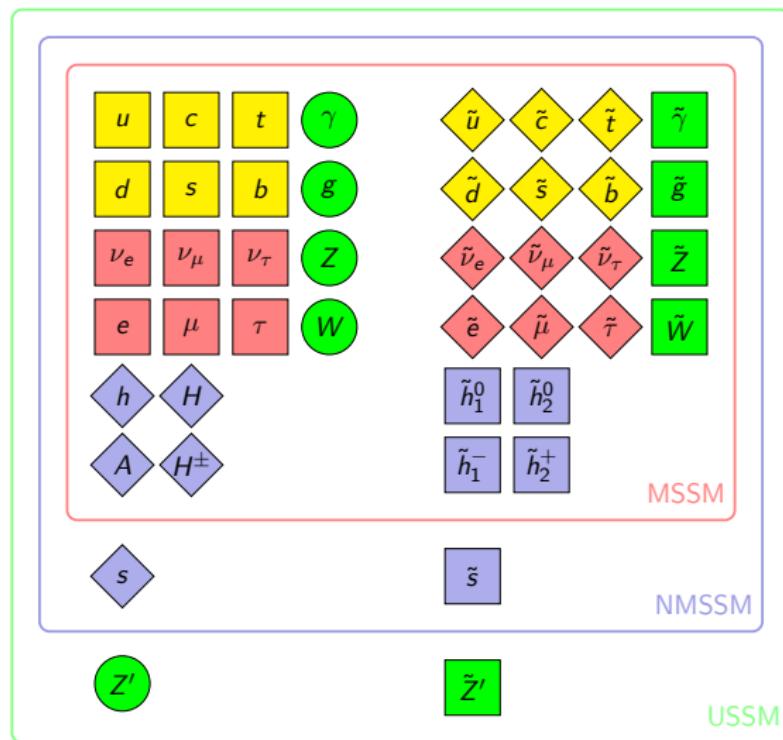
Problem: diskrete Rotationssymmetrie um 120°
⇒ Domänenwände



Lösung: neue kontinuierliche Eichsymmetrie $U(1)'$

⇒ $U(1)'$ -erweitertes Supersymmetrisches Standardmodell (USSM)

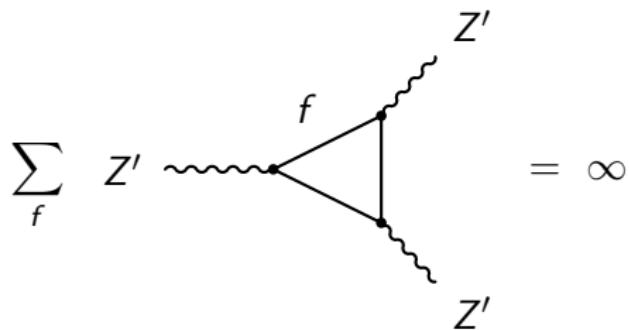
$U(1)'$ -erweitertes Supersymmetrisches Standardmodell (USSM)



Problem des USSM: Anomalien

Problem: $U(1)'$ -Ladungen sind beliebig.

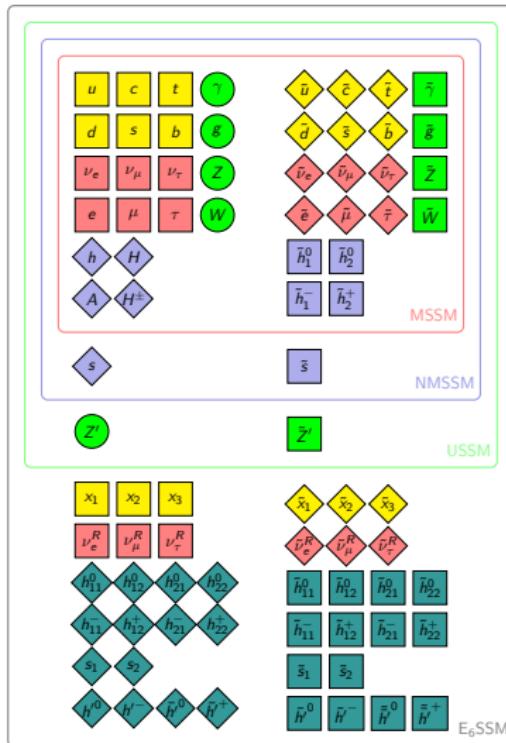
⇒ Ungeschickte Wahl kann zu Anomalien führen:



Lösung: anomaliefreie Eichgruppe, z.B. $SO(10)$ oder E_6

⇒ Exzeptionelles Supersymmetrisches Standardmodell (E_6 SSM)

Exzentrisches Supersymmetrisches Standardmodell (E₆SSM)



Zusammenfassung Supersymmetrie

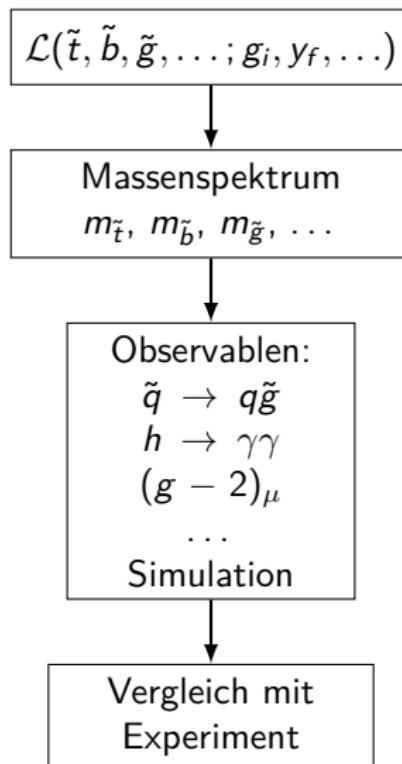
Supersymmetrische Modelle sind attraktive Erweiterungen des SM.

Vorteile:

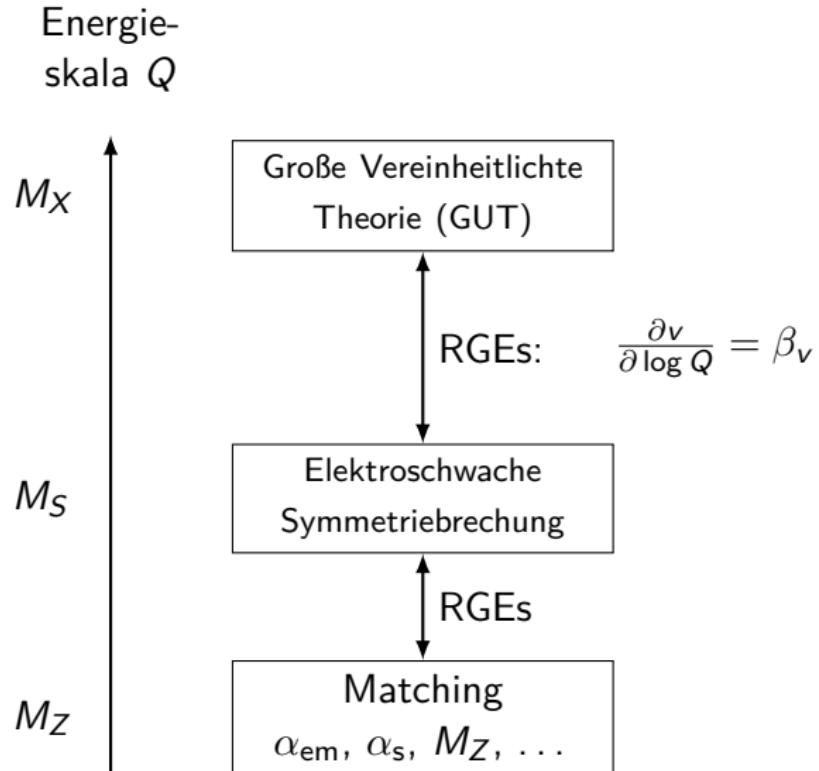
- Lösung des Hierarchieproblems
- Dunkle Materie
- Eichkopplungsvereinigung
- Verbindung zu Supergravitations-Modellen



Warum Berechnung des Massenspektrums?

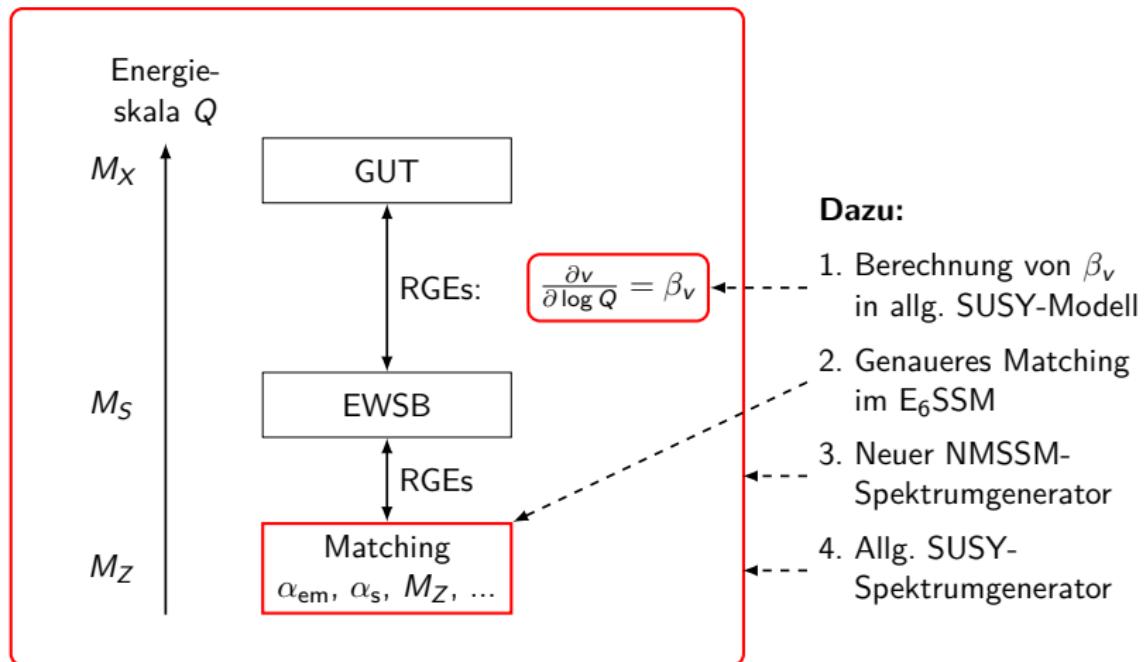


Physikalische Problemstellung



Ziel dieser Promotion

Präzise Berechnung von Massenspektren in SUSY-Modellen



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Allgemeiner SUSY-Spektrumgenerator-Generator

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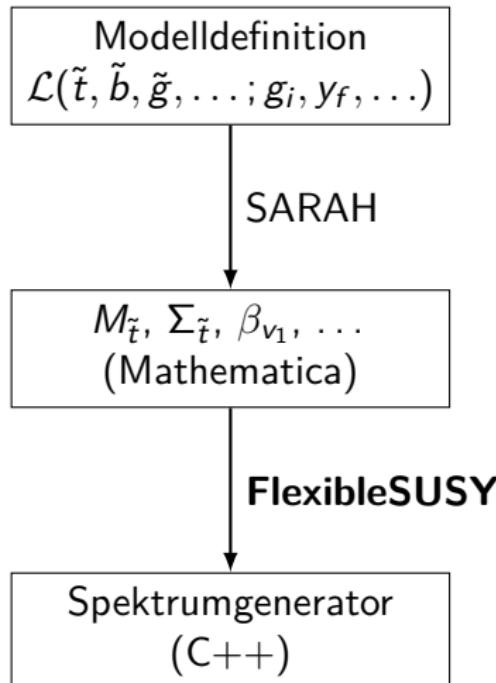
Allgemeiner SUSY-Spektrumgenerator-Generator

Allgemeiner SUSY-Spektrumgenerator-Generator

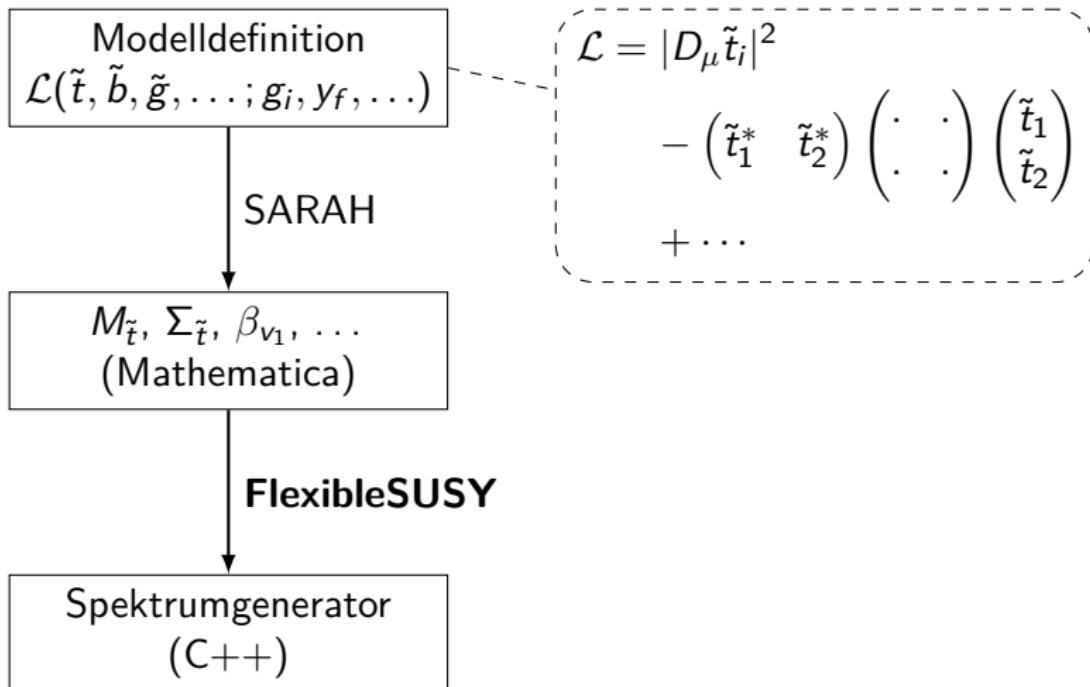
FlexibleSUSY



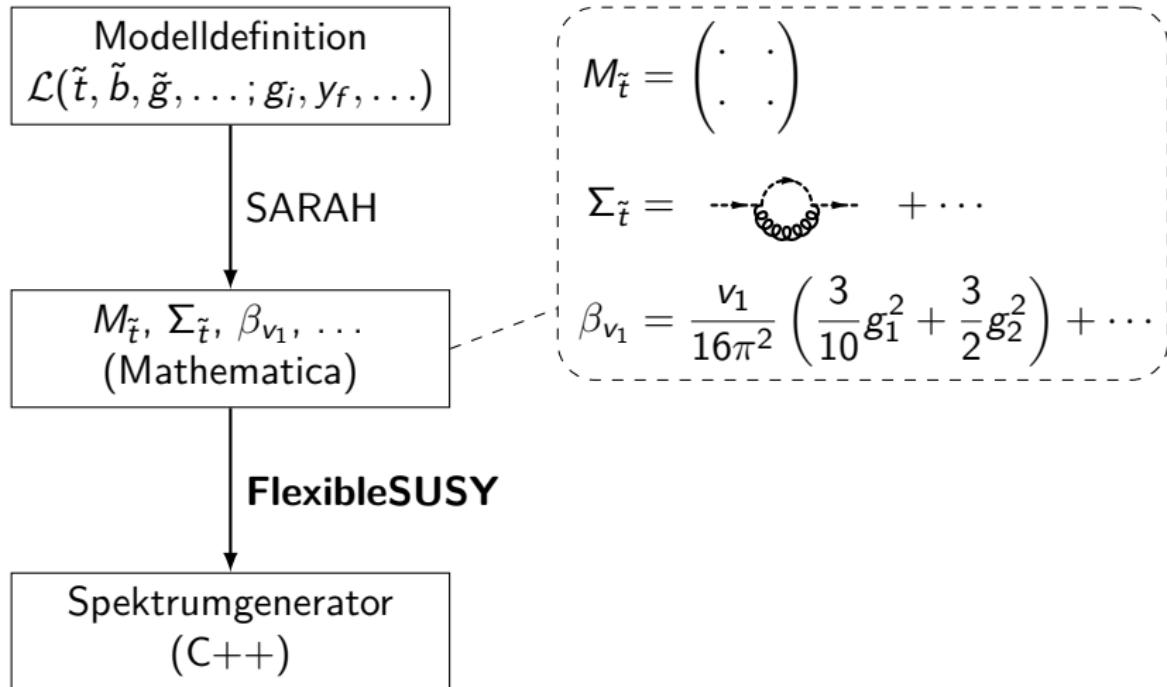
Erzeugung eines Spektrumgenerators



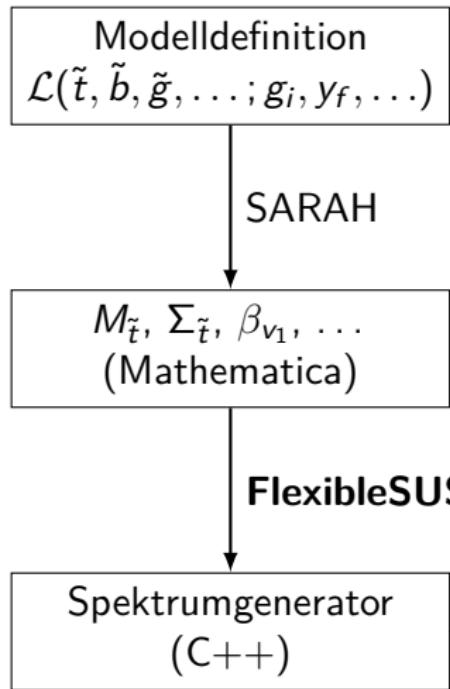
Erzeugung eines Spektrumgenerators



Erzeugung eines Spektrumgenerators



Erzeugung eines Spektrumgenerators



```
Matrix<2,2> get_mass_matrix_St() {
    Matrix<2,2> mass_matrix;
    mass_matrix(0,0) = ...;
    mass_matrix(0,1) = ...;
    mass_matrix(1,0) = ...;
    mass_matrix(1,1) = ...;

    return mass_matrix;
}

complex<double> self_energy_St() {
    complex<double> self_energy;

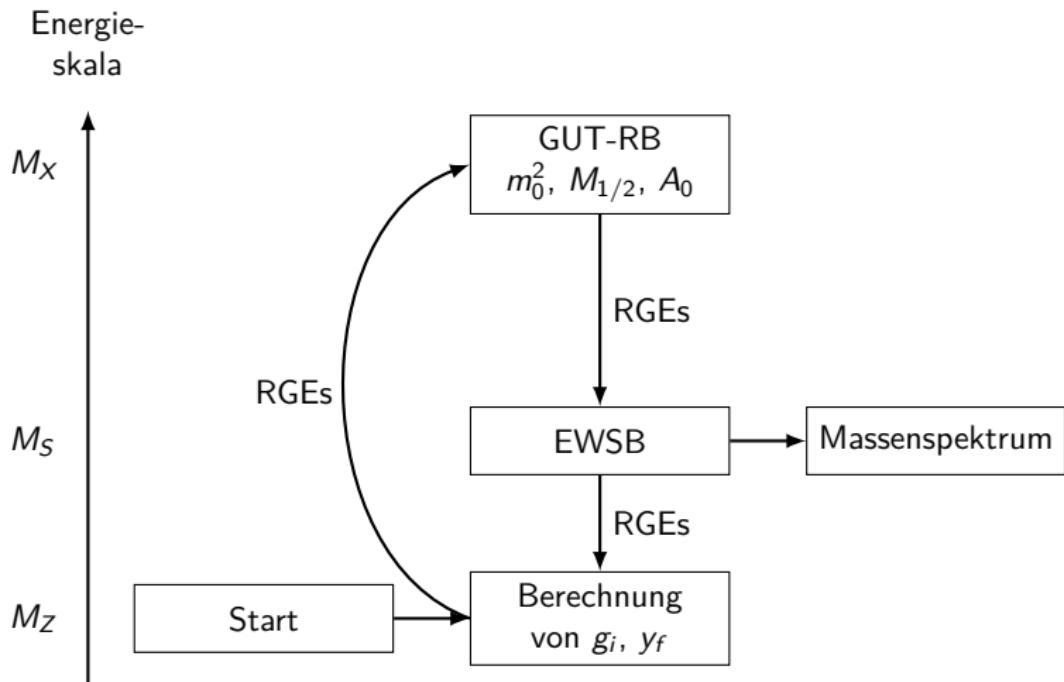
    self_energy += ...;
    self_energy += ...;
    self_energy += ...;

    return self_energy;
}

double beta_v1() {
    double beta_v1;
    beta_v1 = v1*(0.3*Sqr(g1)
        + 1.5*.Sqrt(g2))/(16.*Sqr(Pi) + ...);

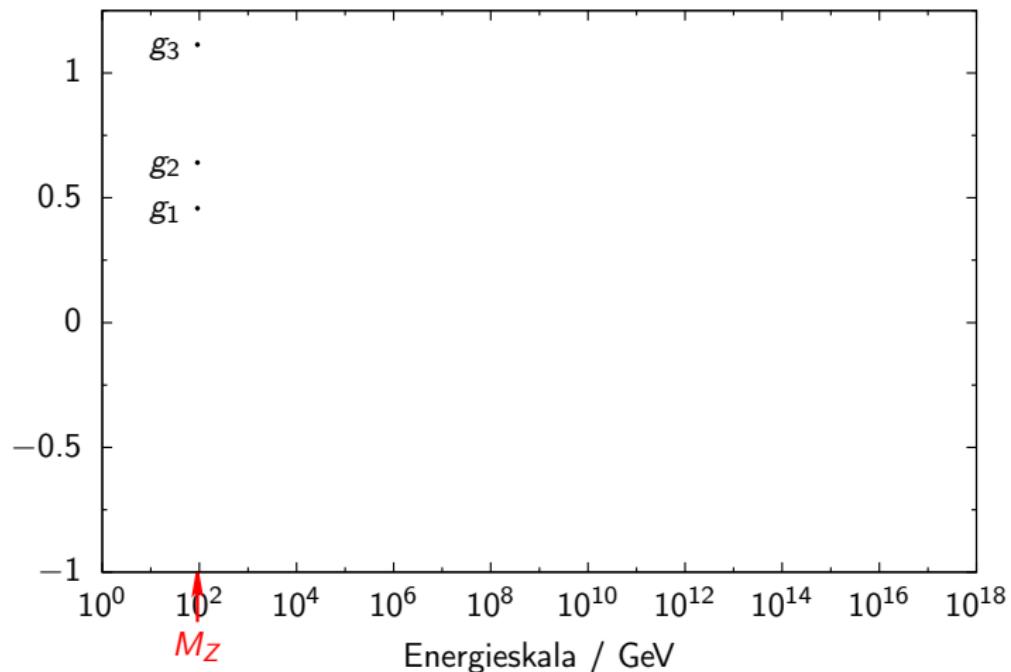
    return beta_v1;
}
```

Algorithmus zur Berechnung des Massenspektrums



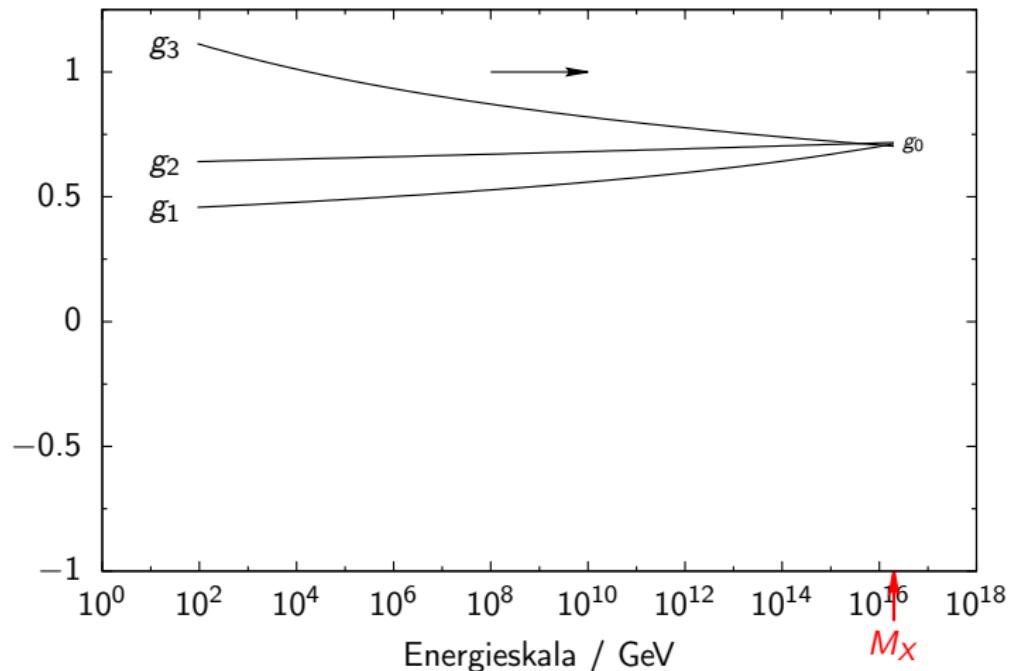
Algorithmus zur Berechnung des Massenspektrums

Iterationsschritt 1: Eichkopplungen an M_Z



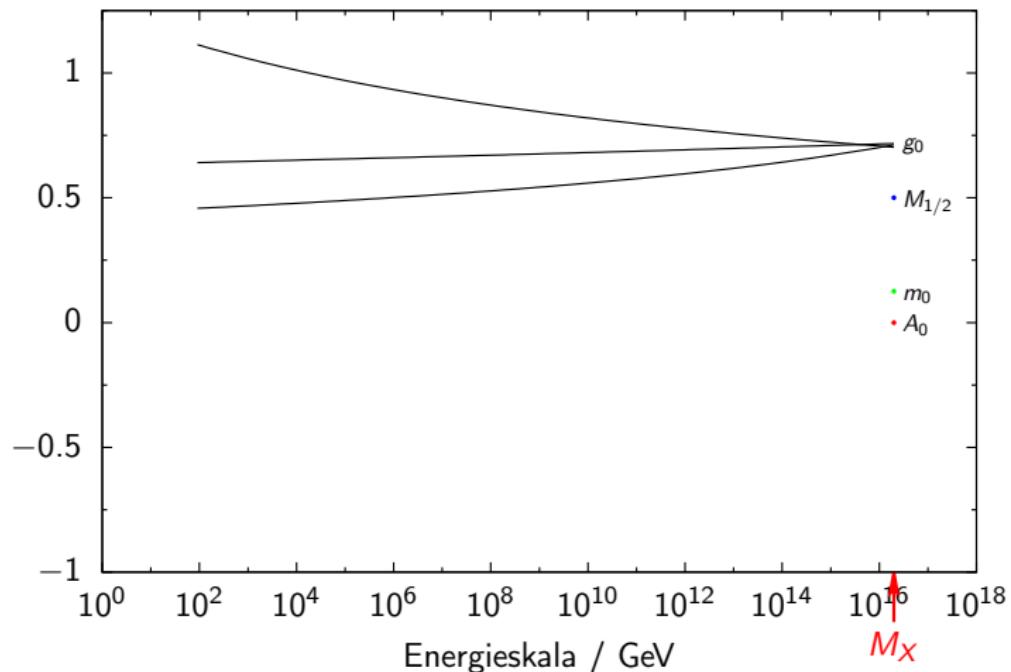
Algorithmus zur Berechnung des Massenspektrums

Iterationsschritt 1: RG-Laufen der Eichkopplungen zu M_X



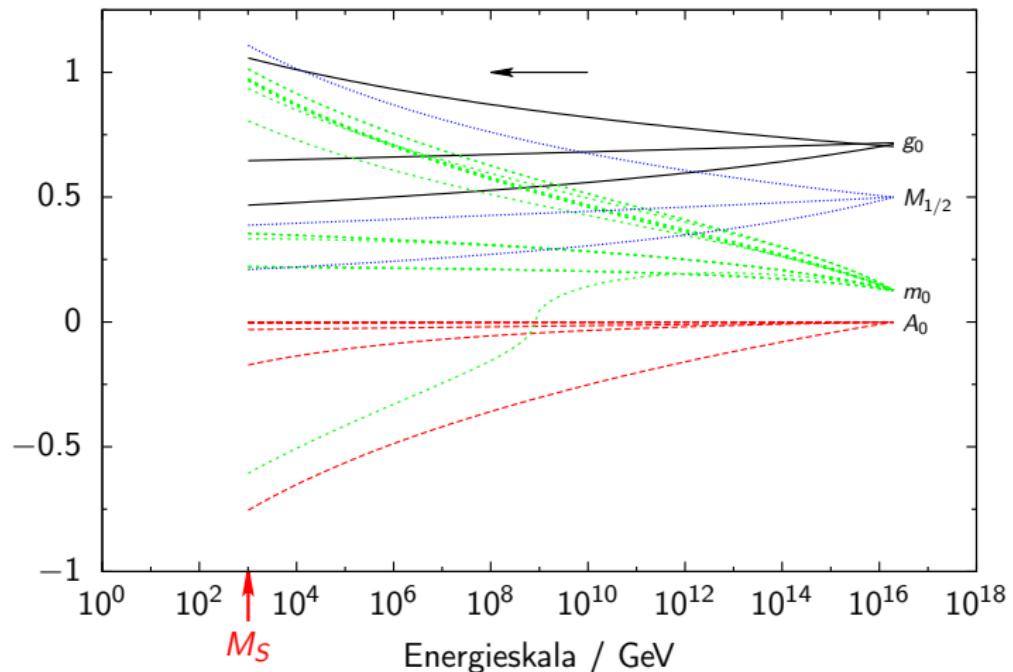
Algorithmus zur Berechnung des Massenspektrums

Iterationsschritt 1: Randbedingungen setzen an M_X



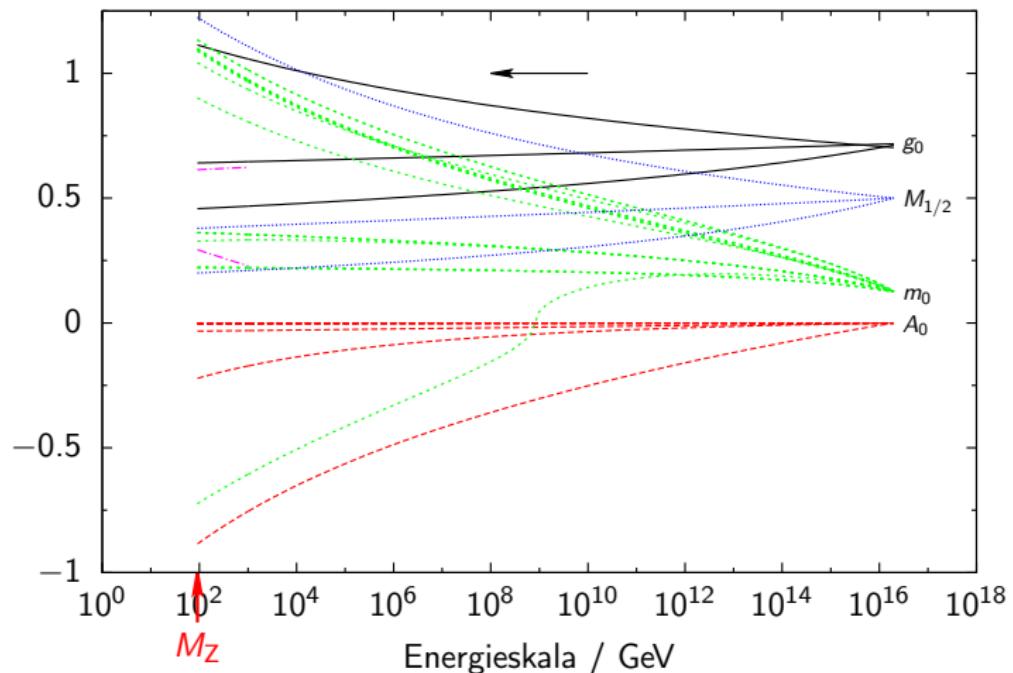
Algorithmus zur Berechnung des Massenspektrums

Iterationsschritt 1: RG-Laufen zu M_S , EWSB



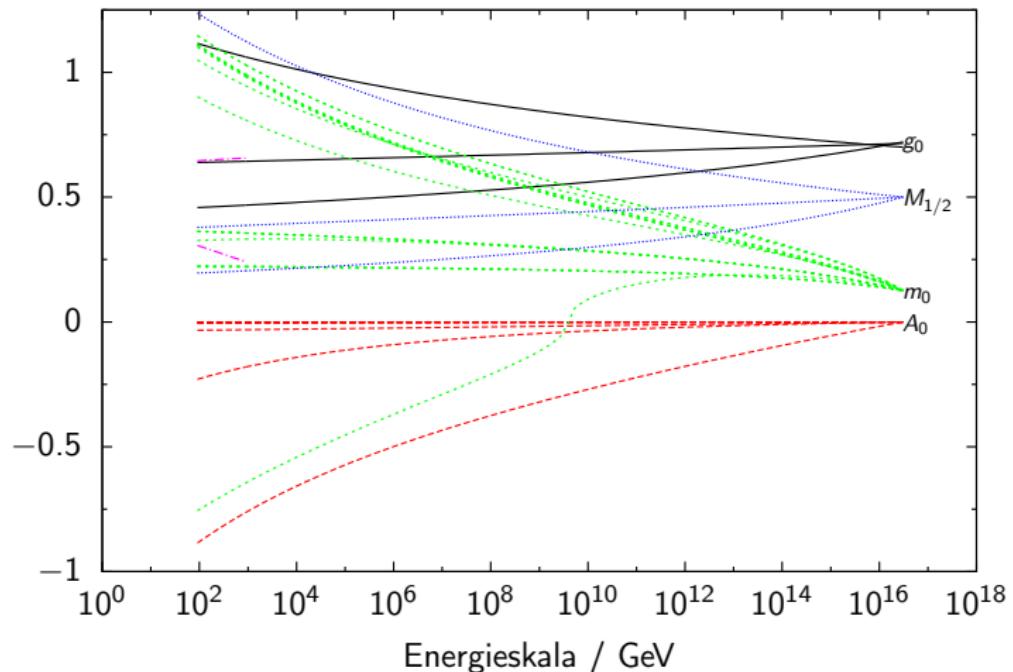
Algorithmus zur Berechnung des Massenspektrums

Iterationsschritt 1: RG-Laufen zu M_Z



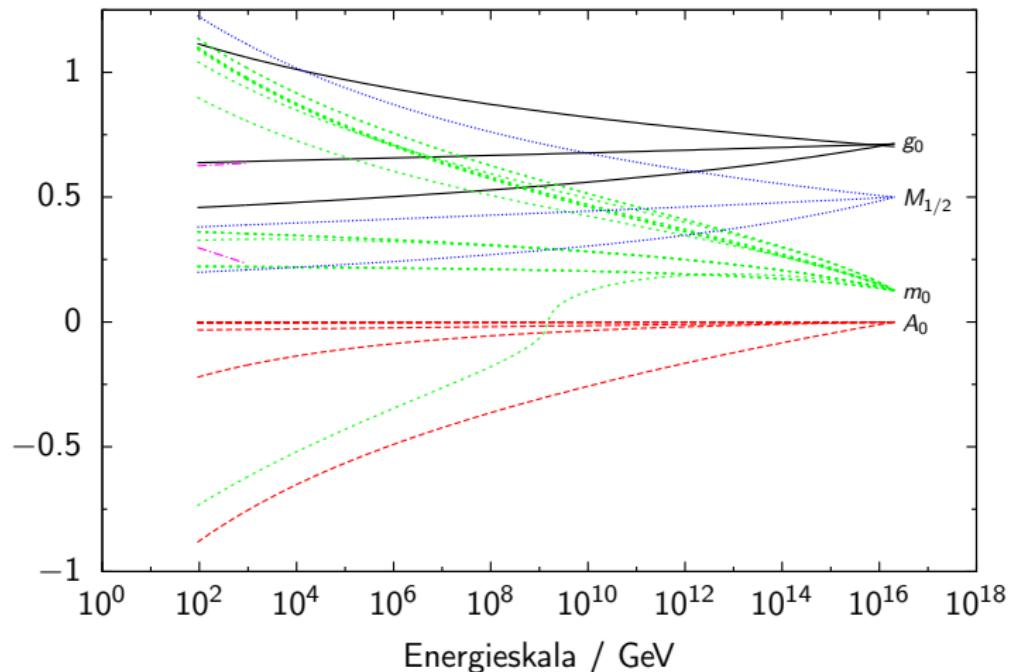
Algorithmus zur Berechnung des Massenspektrums

Iterationsschritt 2:



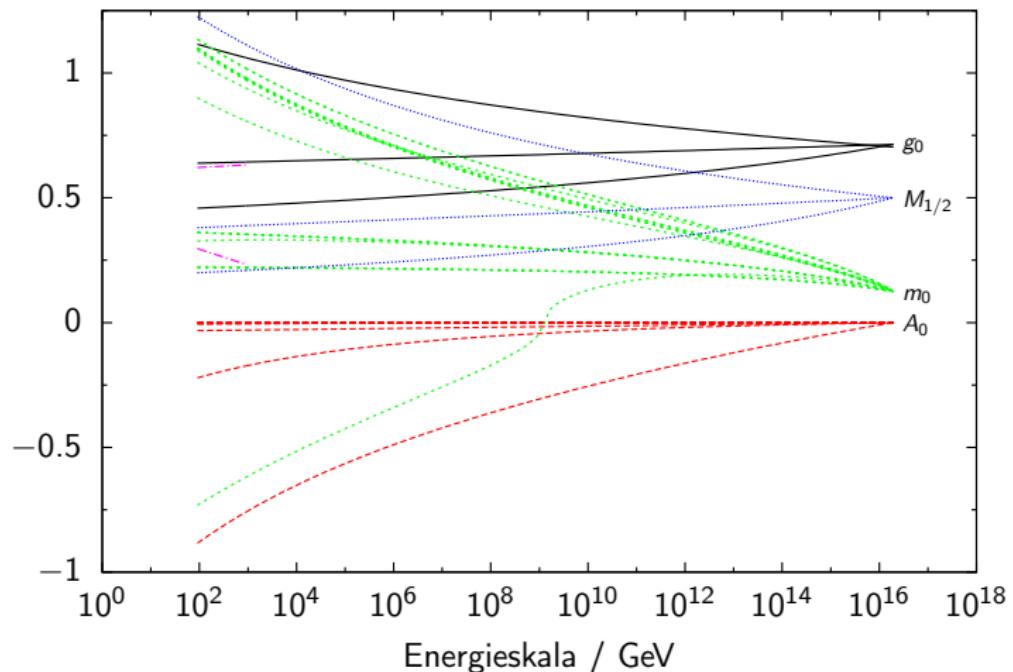
Algorithmus zur Berechnung des Massenspektrums

Iterationsschritt 3:

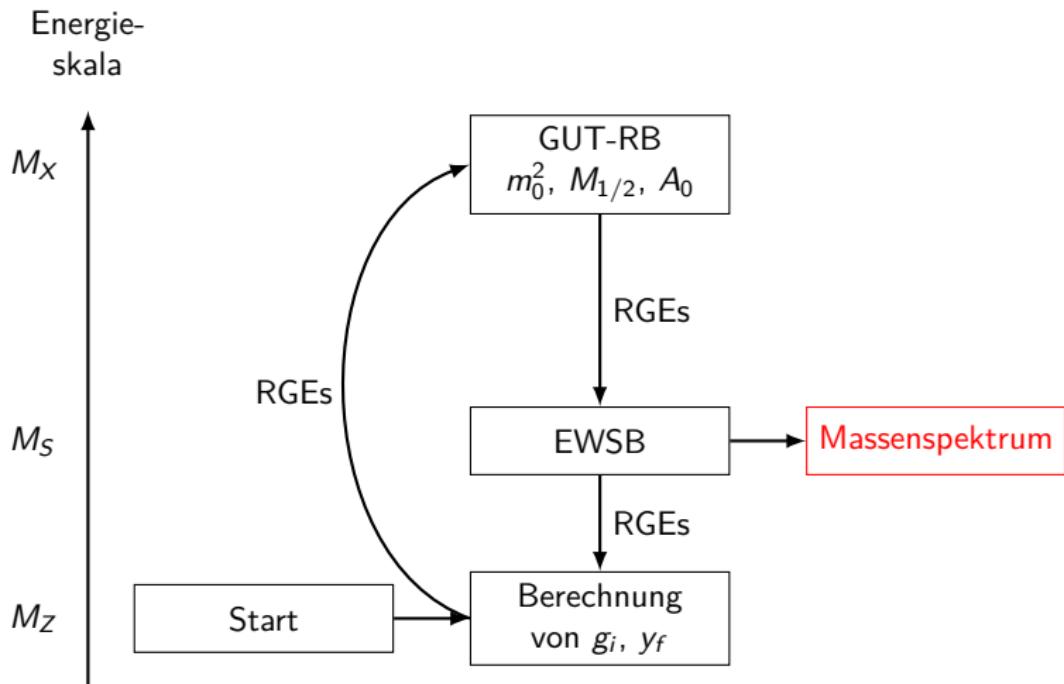


Algorithmus zur Berechnung des Massenspektrums

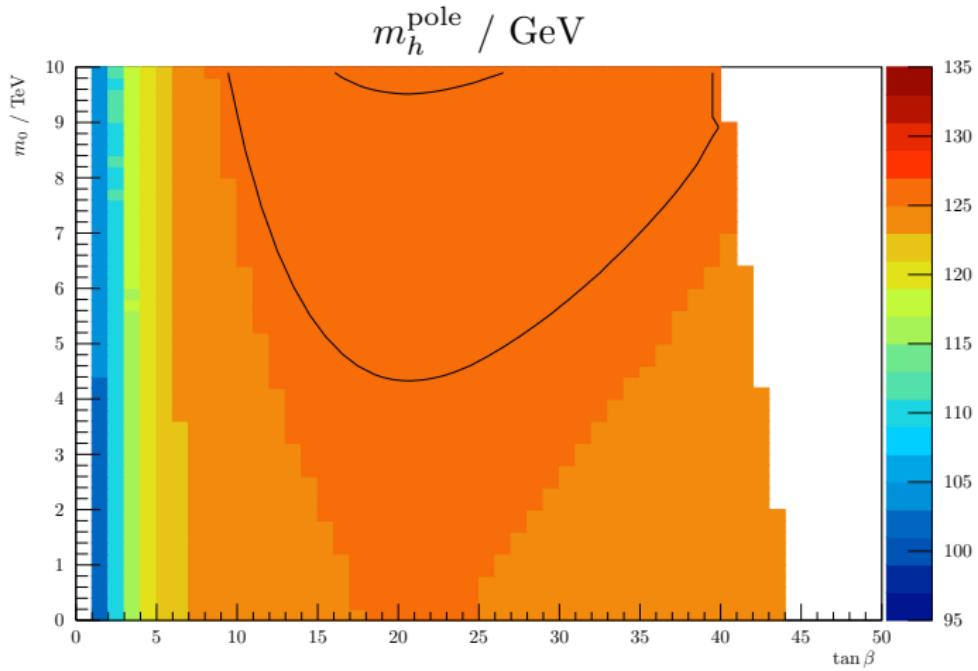
Iterationsschritt 8: Konvergenz



Algorithmus zur Berechnung des Massenspektrums



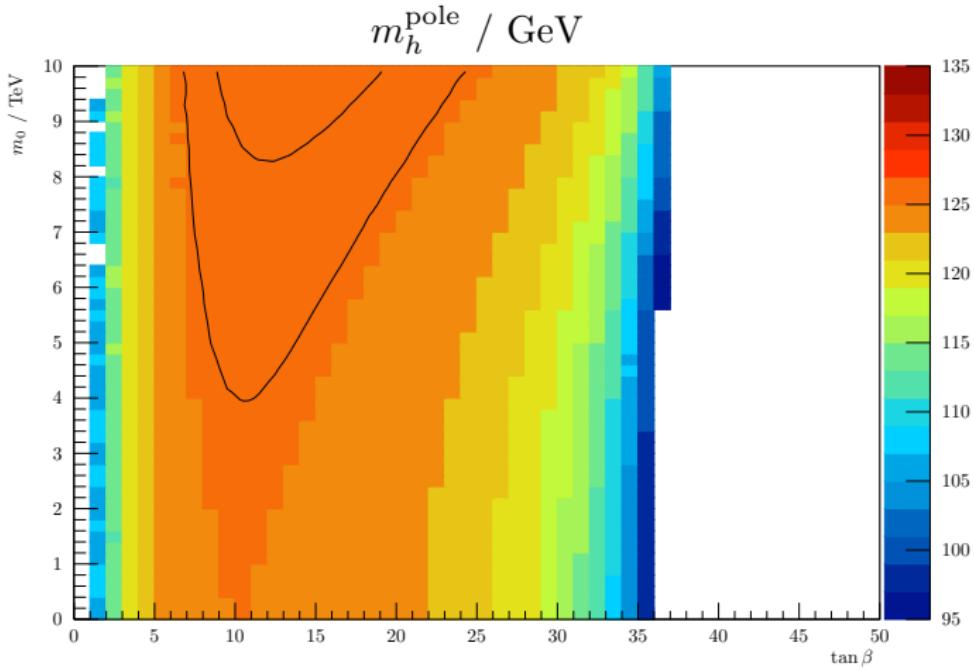
MSSM-Parameterscan



$$M_{1/2} = A_0 = 5 \text{ TeV}, \text{sign } \mu = +1$$

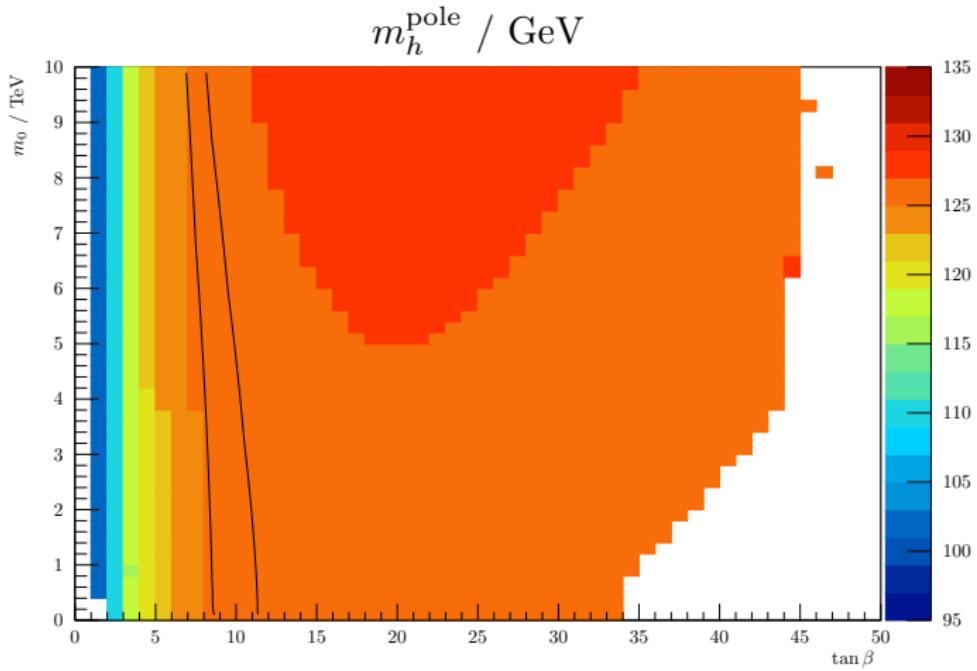
Higgs-Massenkonturen bei $m_h^{\text{pole}} = (125.7 \pm 0.4) \text{ GeV}$

NMSSM-Parameterscan



$M_{1/2} = -A_0 = 5 \text{ TeV}$, $\lambda(M_X) = 0.1$, $\text{sign } v_s = +1$
Higgs-Massenkonturen bei $m_h^{\text{pole}} = (125.7 \pm 0.4) \text{ GeV}$

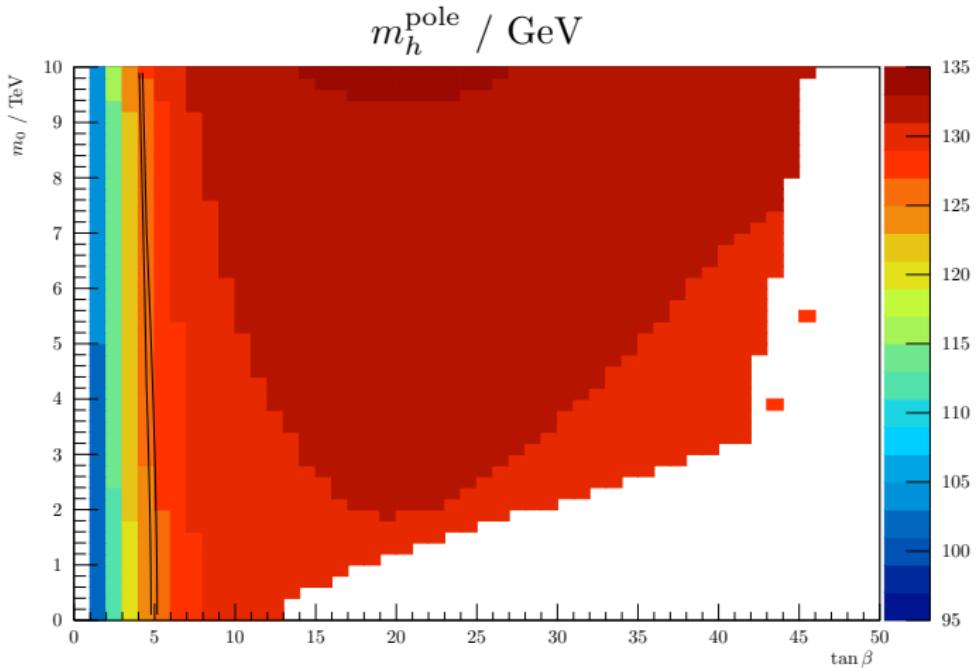
USSM-Parameterscan



$$M_{1/2} = A_0 = 5 \text{ TeV}, \lambda(M_X) = 0.1, v_s = 10 \text{ TeV}$$

Higgs-Massenkonturen bei $m_h^{\text{pole}} = (125.7 \pm 0.4) \text{ GeV}$

E_6 SSM-Parameterscan



$M_{1/2} = A_0 = 5 \text{ TeV}$, $\lambda(M_X) = \kappa(M_X) = 0.1$, $v_s = 10 \text{ TeV}$
Higgs-Massenkonturen bei $m_h^{\text{pole}} = (125.7 \pm 0.4) \text{ GeV}$

Zusammenfassung

Ziel dieser Promotion:

Präzise Berechnung von Massenspektren in SUSY-Modellen

Dazu:

- Berechnung von β_v auf 1- und 2-Loop-Niveau

[Sperling, Stöckinger, AV, JHEP 1307 (2013), JHEP 1401 (2014)]

- E₆SSM-Spektrumgenerator mit genauem Matching
(CE6SSMSpecGen)

[Athron, Stöckinger, AV, Phys.Rev. D86 (2012)]

- Neuer NMSSM-Spektrumgenerator (NMSSM-SOFTSUSY)

[Allanach, Athron, Tunstall, AV, Williams, Comput.Phys.Comm. 185 (2014)]

- Allgemeiner, automatischer
SUSY-Spektrumgenerator-Generator (FlexibleSUSY)

[Athron, Park, Stöckinger, AV, arXiv:1406.2319 (2014)]

Vielen Dank!



Backup

Kleines Hierarchieproblem

$$(m_h^{\text{pole}})^2 = (m_h^{\text{tree}})^2 + \Delta m_h^2 = (125.7 \text{ GeV})^2$$

$$(m_h^{\text{tree}})^2 \approx \underbrace{m_Z^2 \cos^2 2\beta}_{\text{MSSM}} + \underbrace{\frac{\lambda^2 v^2}{2} \sin^2 2\beta}_{\text{NMSSM}} + \underbrace{\frac{m_Z^2}{4} \left(1 + \frac{1}{4} \cos 2\beta\right)^2}_{\text{USSM, E}_6\text{SSM}}$$

\Rightarrow

$$\Delta m_h^2 \geq \begin{cases} (87 \text{ GeV})^2 & \text{MSSM} \\ (55 \text{ GeV})^2 & \text{NMSSM} \\ (32 \text{ GeV})^2 & \text{USSM, E}_6\text{SSM} \end{cases} \Rightarrow \begin{aligned} m_{\tilde{t}} &\gg m_t \\ m_{\tilde{t}} &\gg m_t \\ m_{\tilde{t}} &> m_t \end{aligned}$$

Berechnung der Higgs-Masse im MSSM

$$M_h^2 = \begin{pmatrix} (M_h^2)_{11} & (M_h^2)_{12} \\ (M_h^2)_{12} & (M_h^2)_{22} \end{pmatrix}$$

$$(M_h^2)_{11} = m_{h_d}^2 + |\mu|^2 + \frac{1}{8}(g_Y^2 + g_2^2)(3v_d^2 - v_u^2)$$

$$(M_h^2)_{12} = -\frac{1}{2}(B\mu + B\mu^*) - \frac{1}{4}v_u v_d(g_Y^2 + g_2^2)$$

$$(M_h^2)_{22} = m_{h_u}^2 + |\mu|^2 + \frac{1}{8}(g_Y^2 + g_2^2)(3v_u^2 - v_d^2)$$

Higgs-Massen sind Nullstellen von

$$0 = \det [p^2 \mathbf{1} - M_h^2 + \hat{\Sigma}_h(p^2)]$$

mit

$$\hat{\Sigma}_h(p^2) = \Sigma_h(p^2) - \delta M_h^2 + (p^2 - M_h^2)\delta Z_h,$$

$$\delta M_h^2 = \Sigma_h(p^2) \Big|_{\Delta}, \quad \delta Z_h = -\Sigma'_h(p^2) \Big|_{\Delta}$$

MSSM EWSB-Gleichungen (tree-level)

$$0 = \frac{\partial V}{\partial v_d} = m_{h_d}^2 v_d + |\mu|^2 v_d - B\mu v_u + \frac{\bar{g}^2}{8}(v_d^2 - v_u^2)v_d$$

$$0 = \frac{\partial V}{\partial v_u} = m_{h_u}^2 v_u + |\mu|^2 v_u - B\mu v_d - \frac{\bar{g}^2}{8}(v_d^2 - v_u^2)v_u$$

mit $\bar{g}^2 = g_Y^2 + g_2^2$

Renormierung von v

Allgemeine Renormierungstransformation:

$$(\phi + v) \rightarrow \sqrt{Z} \phi + v + \delta v$$

oder $(\phi + v) \rightarrow \sqrt{Z}(\phi + v + \delta \bar{v})$

Mit $\sqrt{Z} = 1 + \frac{1}{2}\delta Z$ folgt:

$$\delta v = \frac{1}{2}\delta Z v + \delta \bar{v}$$

Trick: Hintergrundfeld einführen

$$\phi \rightarrow \phi_{\text{eff}} = \phi + \hat{\phi} + \hat{v}$$

$$\phi_{\text{eff}} \rightarrow \sqrt{Z} \left[\phi + \sqrt{\hat{Z}} (\hat{\phi} + \hat{v}) \right]$$

Damit folgt für $\hat{\phi} = 0$

$$\delta v = \frac{1}{2} (\delta Z + \delta \hat{Z}) v$$

$$\beta_v = (\gamma + \hat{\gamma}) v$$

Berechnung von β_v

Allgemeine Eichtheorie:

$$\beta_v = (\gamma + \hat{\gamma})v$$

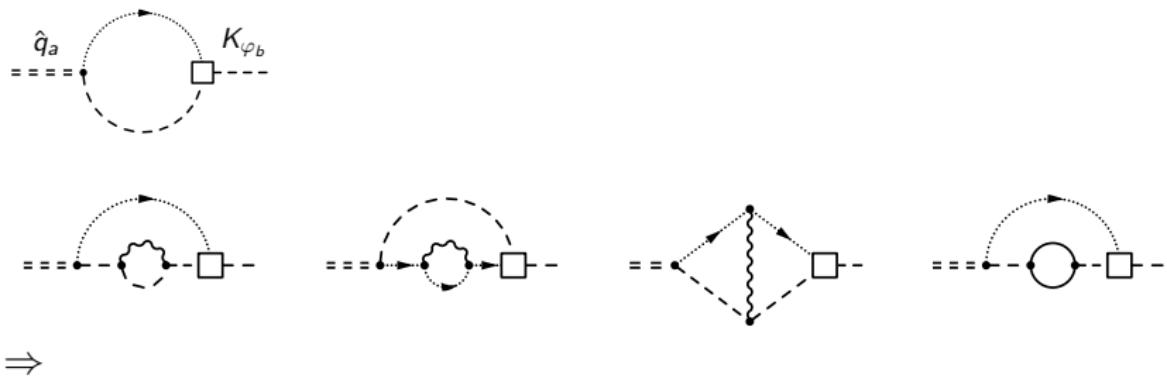
γ ... anomale Dimension des Higgsfeldes

[Machacek, Vaughn (1983)]

$\hat{\gamma}$... anomale Dimension eines Hintergrundfeldes

unbekannt!

Berechnung von β_v



$$\hat{\gamma}^{(1)} = \frac{\xi}{(4\pi)^2} 2g^2 C^2(S)$$

$$\hat{\gamma}^{(2)} = \frac{\xi}{(4\pi)^4} 2g^2 C^2(S)$$

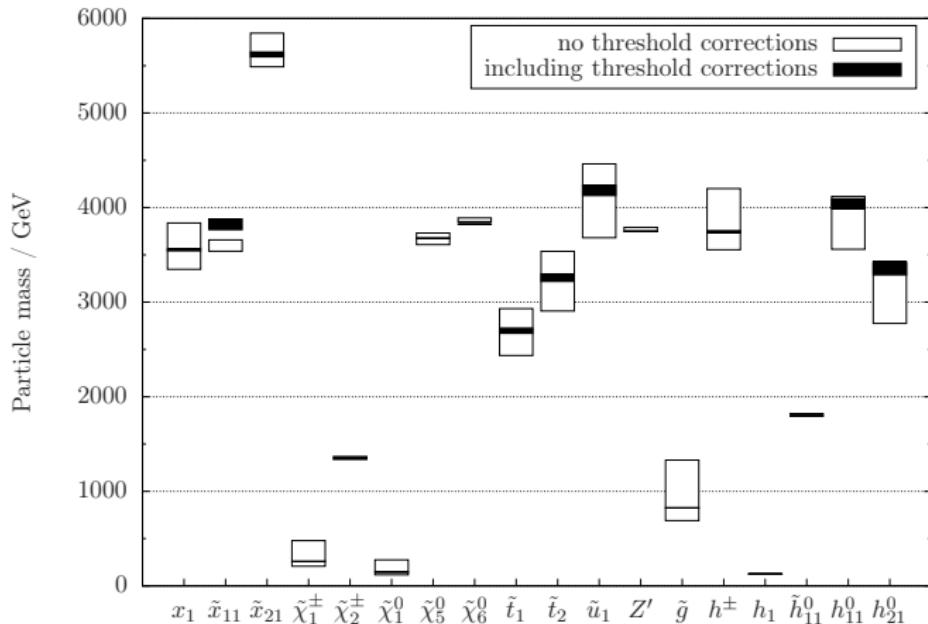
$$\times \left[g^2 (1 + \xi) C^2(S) + g^2 \frac{7 - \xi}{4} C_2(G) - Y^2(S) \right]$$

E_6 SSM-Schwellenkorrekturen

$$g_i^{\overline{DR}, E_6 \text{SSM}}(Q) = g_i^{\overline{MS}, \text{SM}}(Q) + \Delta g_i(Q) \quad (i = 1, 2, 3),$$

$$\begin{aligned} \Delta g_3(Q) = & \frac{g_3^3}{(4\pi)^2} \left[\frac{1}{2} - 2 \log \frac{m_{\tilde{g}}}{Q} - \frac{1}{6} \sum_{\tilde{q} \in \{\tilde{u}, \tilde{d}\}} \sum_{i=1}^3 \sum_{k=1}^2 \log \frac{m_{\tilde{q}_{ik}}}{Q} \right. \\ & \left. - \frac{2}{3} \sum_{i=1}^3 \log \frac{m_{x_i}}{Q} - \frac{1}{6} \sum_{i=1}^3 \sum_{k=1}^2 \log \frac{m_{\tilde{x}_{ik}}}{Q} \right] \end{aligned}$$

CE₆SSM-Massenspektrum

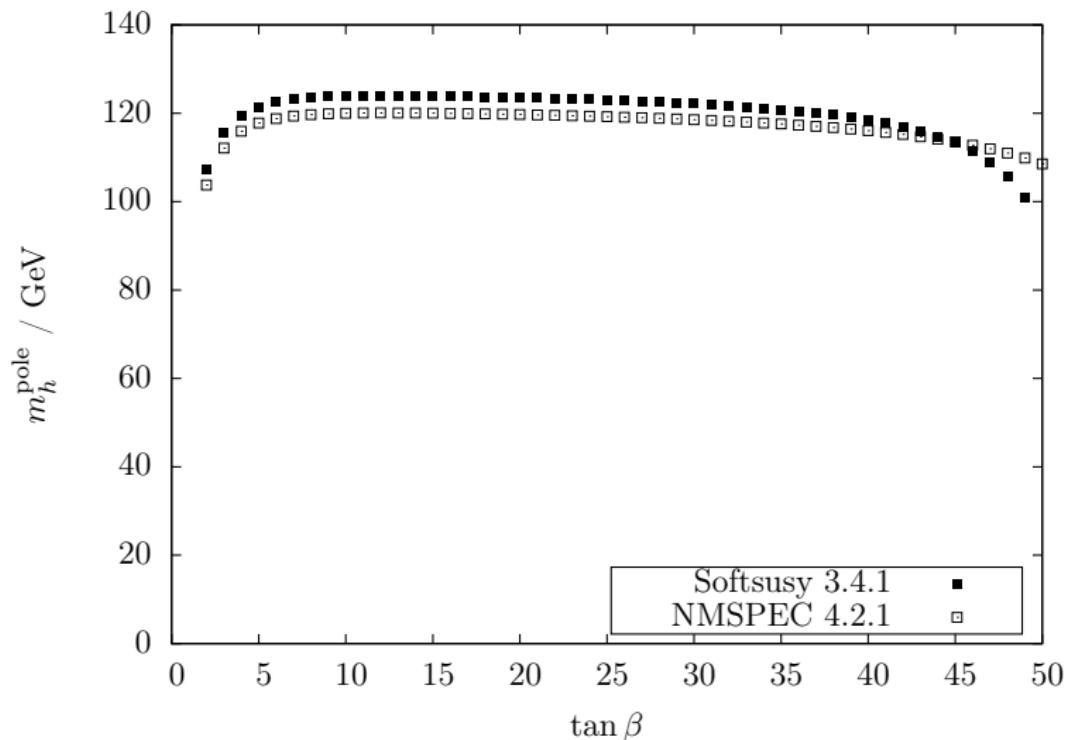


$\tan\beta = 35, \quad \lambda_{1,2,3} = \kappa_{1,2,3} = 0.2, \quad v_s = 10 \text{ TeV},$

$\mu' = m_{h'} = m_{\bar{h}'} = 10 \text{ TeV}, \quad B\mu' = 0,$

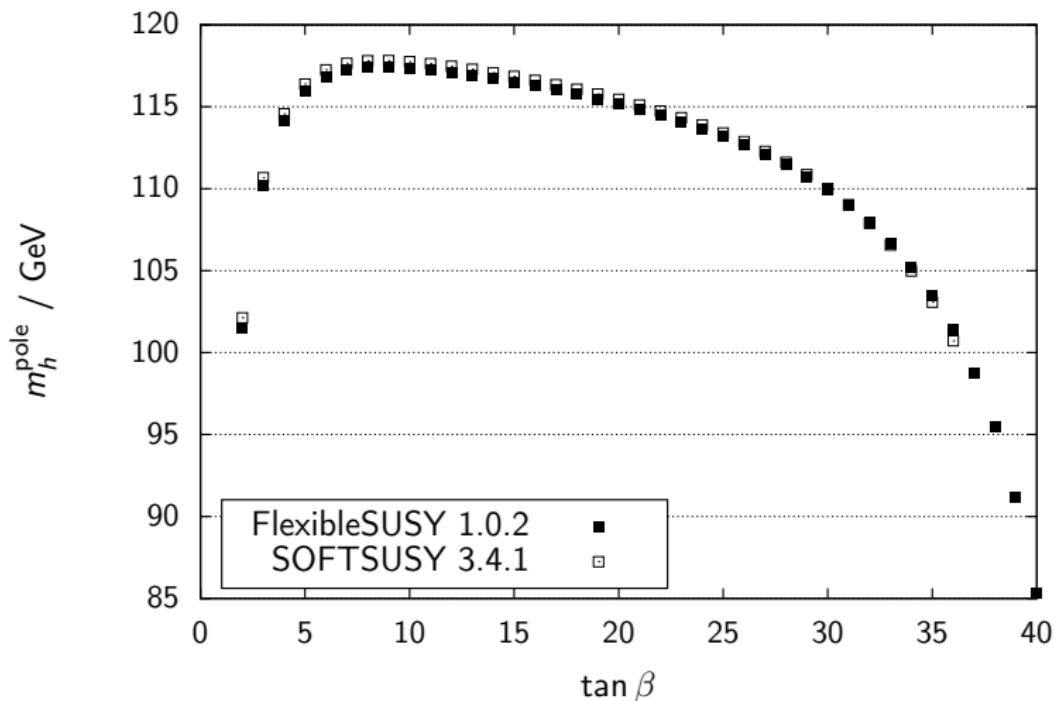
$T_{\text{match}} = \frac{1}{2} T_0 \dots 2 T_0, \quad T_0 = 1.9 \text{ TeV}$

NMSSM Higgs-Masse SOFTSUSY vs. NMSPEC



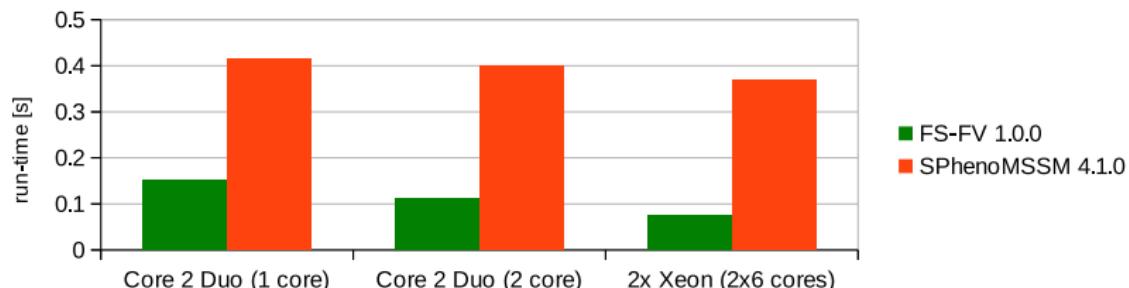
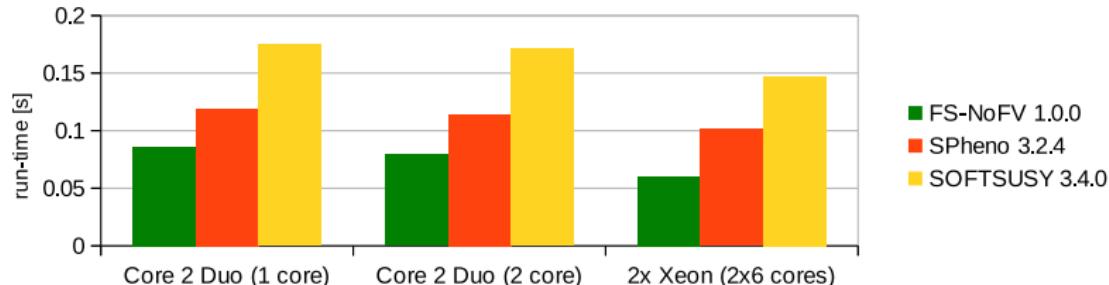
$m_0 = M_{1/2} = -A_0 = 5 \text{ TeV}$, $\lambda(M_S) = 0.1$, $\text{sign } v_s = +1$

NMSSM Higgs-Masse FlexibleSUSY vs. SOFTSUSY



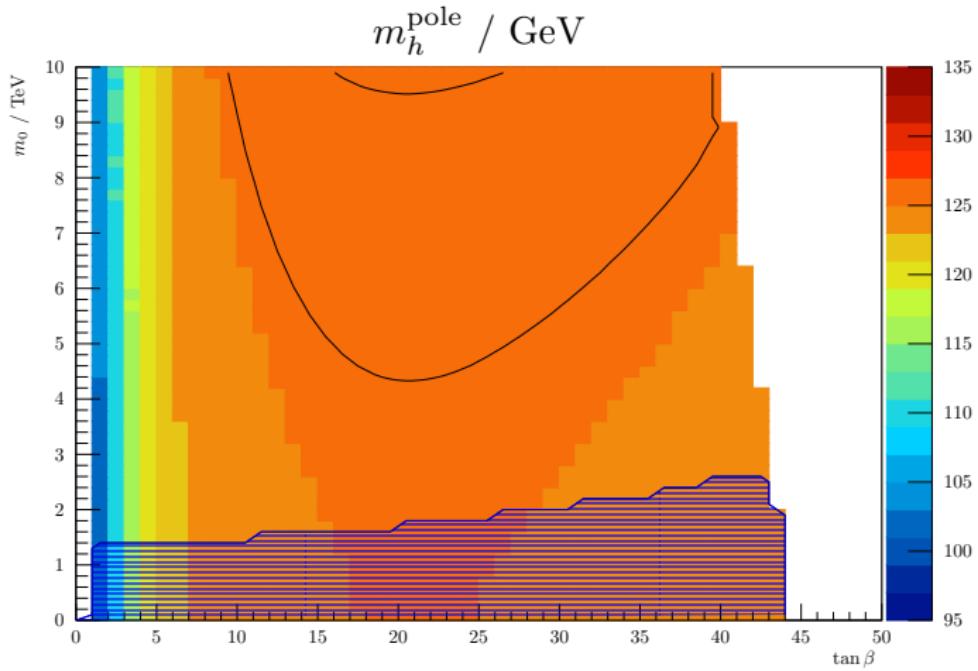
$m_0 = M_{1/2} = -A_0 = 1 \text{ TeV}$, $\lambda(M_X) = 0.1$, $\text{sign } v_s = +1$

CMSSM-Laufzeitvergleich



g++ 4.8.0, ifort 13.1.3 20130607

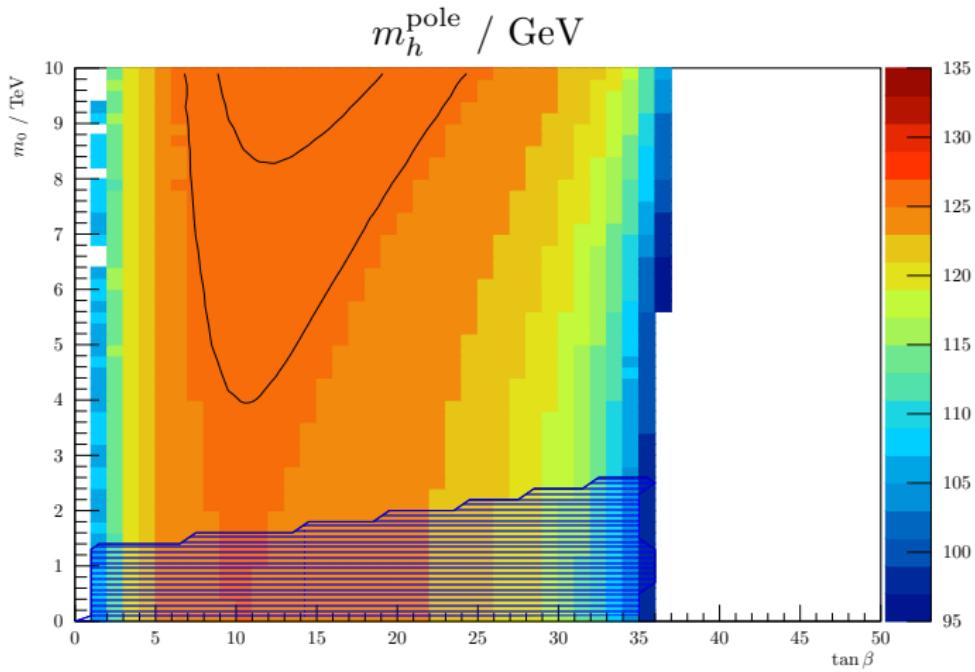
MSSM-Parameterscan



$$M_{1/2} = A_0 = 5 \text{ TeV}, \text{sign } \mu = +1$$

Higgs-Massenkonturen bei $m_h^{\text{pole}} = (125.7 \pm 0.4) \text{ GeV}$

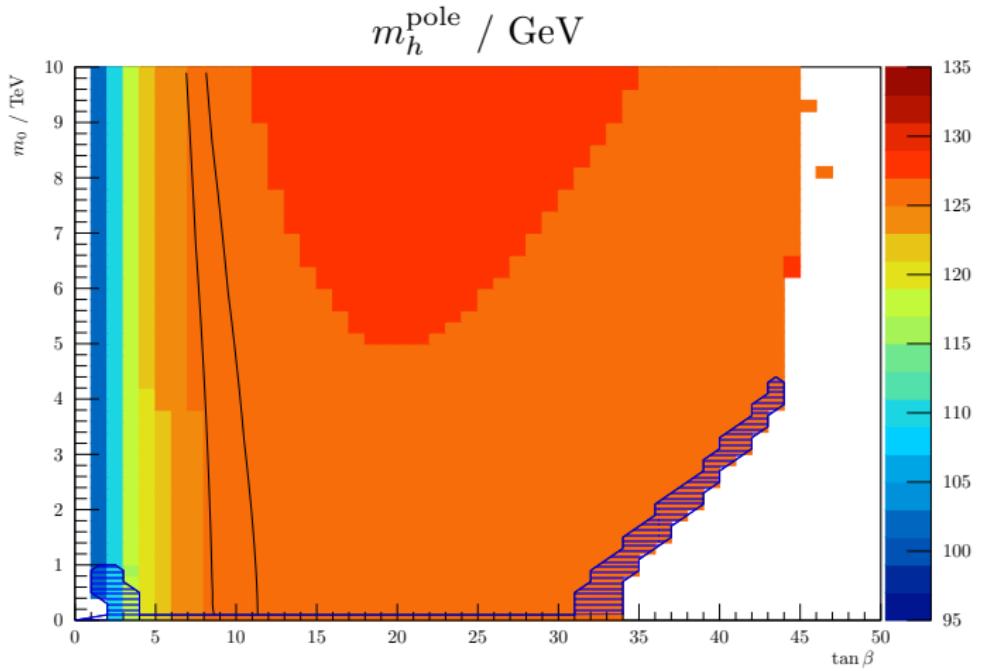
NMSSM-Parameterscan



$$M_{1/2} = -A_0 = 5 \text{ TeV}, \lambda(M_X) = 0.1, \text{sign } v_s = +1$$

Higgs-Massenkonturen bei $m_h^{\text{pole}} = (125.7 \pm 0.4) \text{ GeV}$

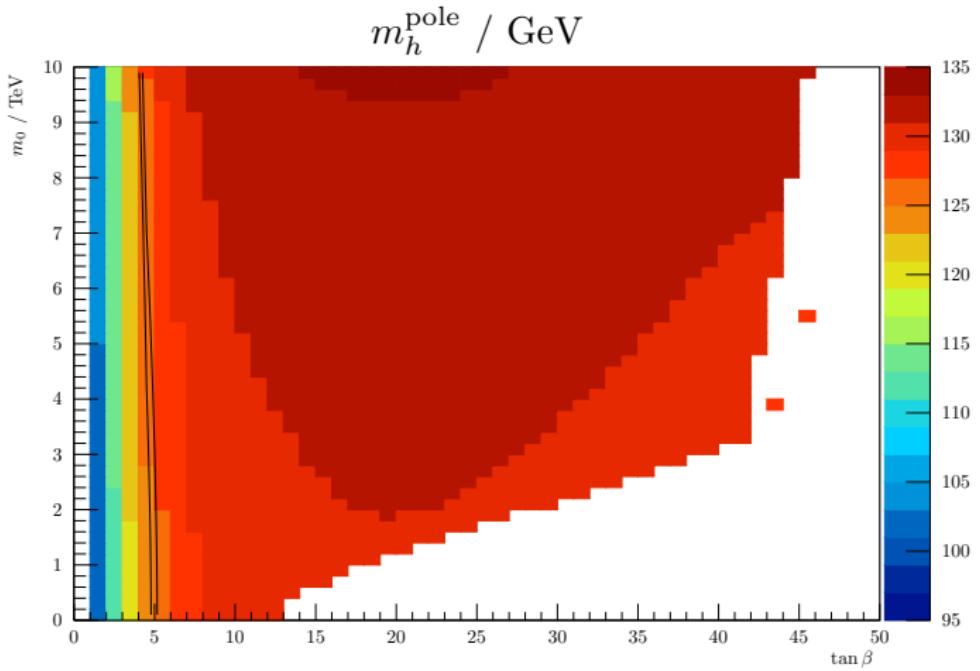
USSM-Parameterscan



$$M_{1/2} = A_0 = 5 \text{ TeV}, \lambda(M_X) = 0.1, v_s = 10 \text{ TeV}$$

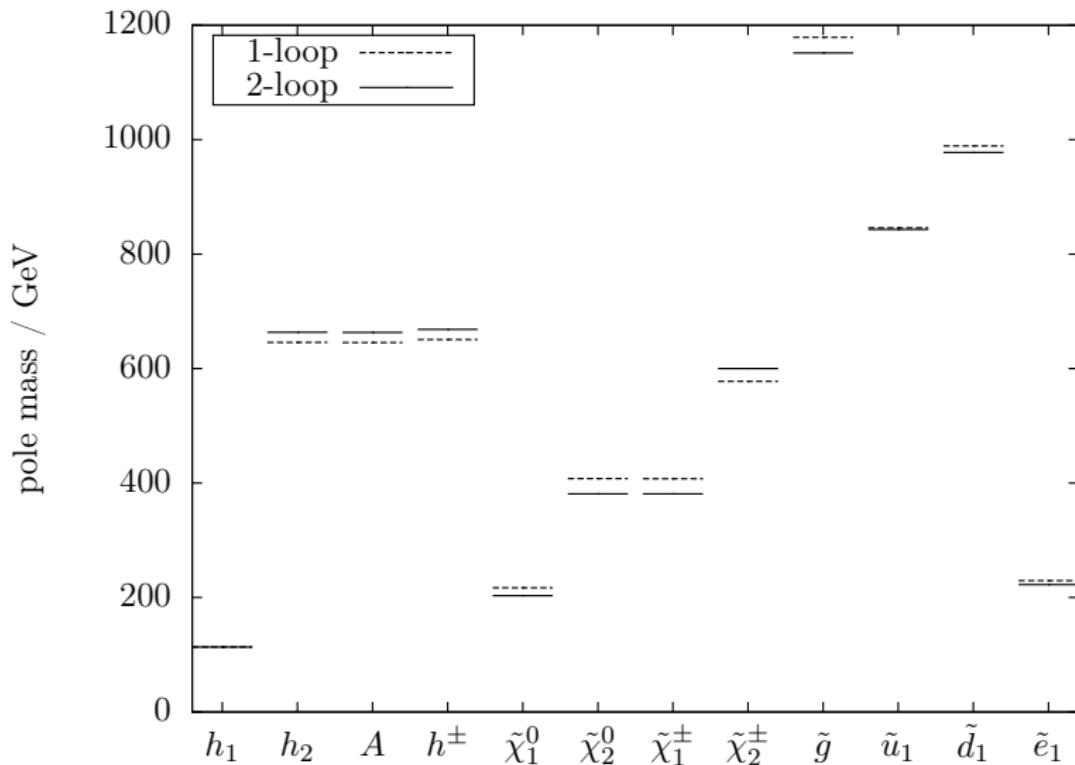
Higgs-Massenkonturen bei $m_h^{\text{pole}} = (125.7 \pm 0.4) \text{ GeV}$

E_6 SSM-Parameterscan

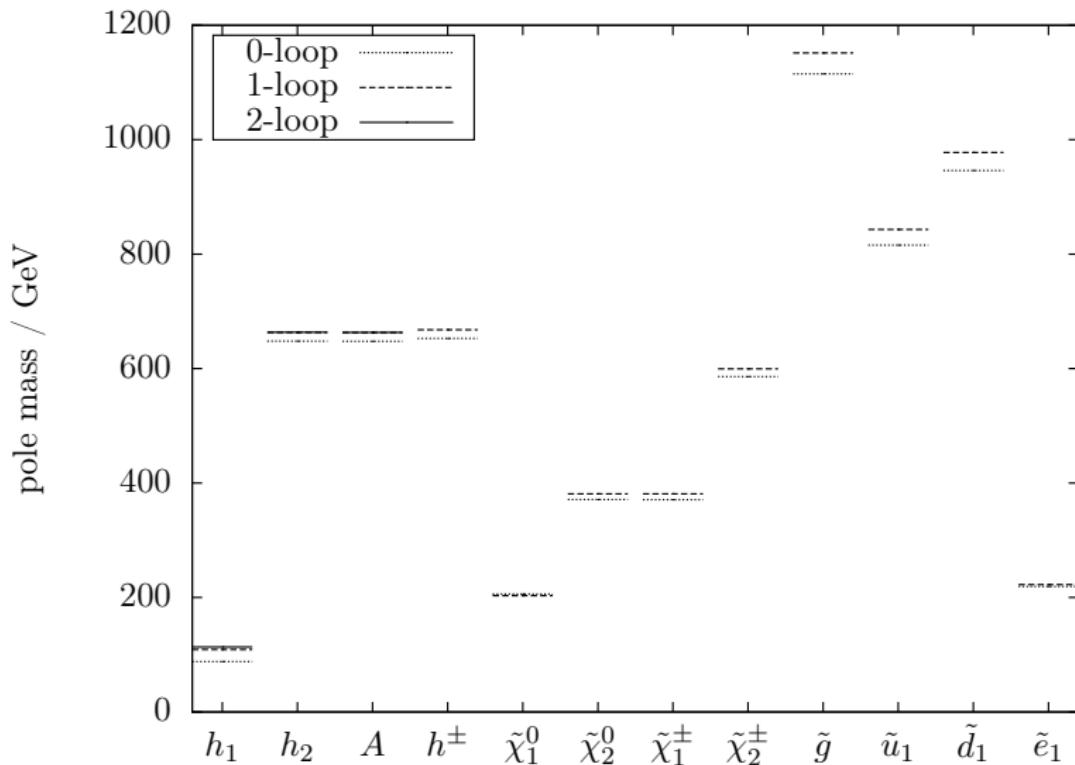


$M_{1/2} = A_0 = 5 \text{ TeV}$, $\lambda(M_X) = \kappa(M_X) = 0.1$, $v_s = 10 \text{ TeV}$
Higgs-Massenkonturen bei $m_h^{\text{pole}} = (125.7 \pm 0.4) \text{ GeV}$

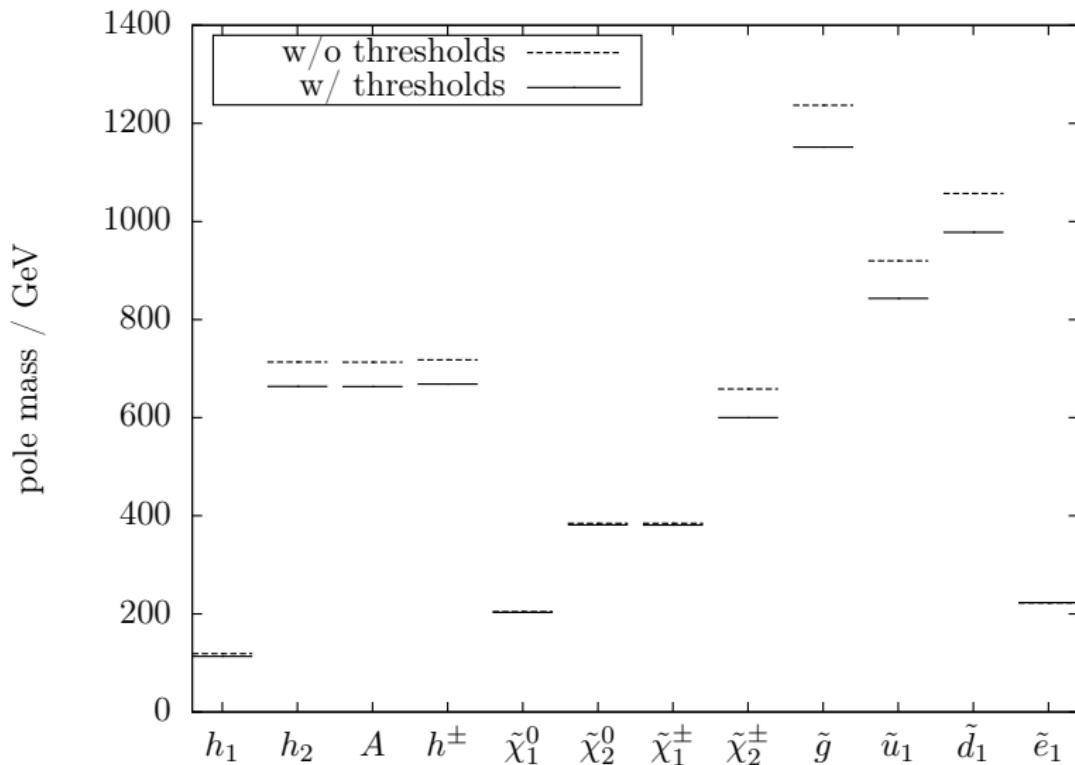
Einfluss der β -Funktionen-Loop-Ordnung (MSSM)



Einfluss der Selbstenergie-Loop-Ordnung (MSSM)



Einfluss der Schwellenkorrekturen-Loop-Ordnung (MSSM)



NMSSM-SOFTSUSY vs. NMSSM-FlexibleSUSY

NMSSM-SOFTSUSY	NMSSM-FlexibleSUSY
Decay interface for NMHDECAY	FlexibleDecay
optimized couplings	automatically generated couplings
2 EWSB variants	user-defined
BCs via C++	BCS via Mathematica
fast pole masses	fast RGE running
stable code basis	automatically generated
few dependencies	requires Mathematica, SARAH, Boost, etc.
G_μ input	M_W input

Verfügbare SUSY-Spektrumgeneratoren

Modell	Spektrumgenerator
MSSM	ISASUSY, SOFTSUSY, SPheno, SuSeFlav, SuSpect
NMSSM	NMSPEC, SOFTSUSY
USSM	–
CE ₆ SSM	CE6SSMSpecGen
beliebiges SUSY-Modell	SARAH, FlexibleSUSY

FlexibleSUSY Design-Ziele

- **modularer, gut lesbarer C++-Code**

Grund: große Vielfalt an SUSY-Modellen
→ Benutzereingriff wahrscheinlich

- **hohe Rechengenauigkeit**

Grund: Higgsmasse gemessen mit $\sigma \approx 0.4 \text{ GeV}$
(führende 2-Loop m_h , $y_{t,b}$; volle 2-Loop β_i , 1-Loop Σ_i)

- **verschiedene RGE+RB-Lösungsalgorithmen**

Grund: Konvergenzprobleme
(Two-scale, Lattice, ...)

- **hohe Rechengeschwindigkeit**

Grund: viele freie Modellparameter
(C++ expression templates, multithreading, ...)

NMSSM-Spektrumgenerator in FlexibleSUSY

1. Get the source code from <https://flexiblesusy.hepforge.org>
2. Create a NMSSM spectrum generator:

```
$ ./install-sarah # if not already installed  
$ ./createmodel --name=NMSSM  
$ ./configure --with-models=NMSSM  
$ make
```

3. Calculate spectrum for given parameter point (SLHA format):

```
$ ./models/NMSSM/run_NMSSM.x \  
--slha-input-file=models/NMSSM/LesHouches.in.NMSSM  
  
Block MASS  
1000021      5.05906233E+02    # Glu  
1000024      1.46609728E+02    # Cha_1  
1000037      3.99399367E+02    # Cha_2  
37          4.33363816E+02    # Hpm_2  
...
```

Definition der NMSSM-Randbedingungen

```
$ cat models/NMSSM/FlexibleSUSY.m
```

```
FSModelName = "NMSSM";  
  
MINPAR = { {1, m0}, {2, m12}, {3, TanBeta}, {5, Azero} };  
  
EXTPAR = { {61, LambdaInput} };  
  
EWSBOutputParameters = { \[Kappa], vS, ms2 };  
  
SUSYScale = Sqrt[M[Su[1]]*M[Su[6]]];  
  
HighScale = g1 == g2;  
  
HighScaleInput = {  
    {mHd2, m0^2}, {mHu2, m0^2}, {mq2, UNITMATRIX[3] m0^2},  
    ...  
};  
  
LowScale = SM[MZ];  
  
LowScaleInput = { ... };
```

Generated NMSSM spectrum generator C++ code

```
typedef Two_scale T; // or Lattice
NMSSM<T> nmssm;
NMSSM_input_parameters input;
QedQcd qedqcd;

// create BCs
std::vector<Constraint<T>*> constraints = {
    new NMSSM_low_scale_constraint<T>(input, qedqcd),
    new NMSSM_susy_scale_constraint<T>(input),
    new NMSSM_high_scale_constraint<T>(input)
};

// solve RG eqs. with the above BCs
RGFlow<T> solver;
solver.add_model(&nmssm, constraints);
solver.solve();

nmssm.calculate_spectrum();
```

MSSM

$$SU(3)_c \times SU(2)_L \times U(1)_Y$$

$$\mathcal{W}_{\text{MSSM}} = \mu(H_1 H_2) - y_{ij}^e (H_1 L_i) \bar{E}_j - y_{ij}^d (H_1 Q_i) \bar{D}_j - y_{ij}^u (Q_i H_2) \bar{U}_j$$

$$h_1^0 \rightarrow \frac{v_1}{\sqrt{2}} + h_1^0, \quad h_2^0 \rightarrow \frac{v_2}{\sqrt{2}} + h_2^0,$$

mSUGRA GUT constraint:

$$\begin{aligned} (m_f^2)_{ij}(M_X) &= m_0^2 \delta_{ij} & (f = q, \ell, u, d, e, h_1, h_2), \\ A_{ij}^f(M_X) &= A_0, & (f = u, d, e), \\ M_i(M_X) &= M_{1/2} & (i = 1, 2, 3). \end{aligned}$$

EWSB output: $\mu(M_S), B\mu(M_S)$

NMSSM

$$SU(3)_c \times SU(2)_L \times U(1)_Y$$

$$\begin{aligned}\mathcal{W}_{\text{NMSSM}} = & \lambda S(H_1 H_2) - y_{ij}^e (H_1 L_i) \bar{E}_j - y_{ij}^d (H_1 Q_i) \bar{D}_j - y_{ij}^u (Q_i H_2) \bar{U}_j \\ & + \frac{\kappa}{3} S^3\end{aligned}$$

$$h_1^0 \rightarrow \frac{v_1}{\sqrt{2}} + h_1^0, \quad h_2^0 \rightarrow \frac{v_2}{\sqrt{2}} + h_2^0, \quad s \rightarrow \frac{v_s}{\sqrt{2}} + s$$

mSUGRA-inspired GUT constraint:

$$\begin{aligned}(m_f^2)_{ij}(M_X) &= m_0^2 \delta_{ij} \quad (f = q, \ell, u, d, e, h_1, h_2), \\ A_{ij}^f(M_X) &= A_0, \quad (f = u, d, e, \lambda, \kappa), \\ M_i(M_X) &= M_{1/2} \quad (i = 1, 2, 3).\end{aligned}$$

EWSB output: $\kappa(M_S)$, $v_s(M_S)$, $m_s^2(M_S)$

USSM

$$SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)'$$

$$\mathcal{W}_{\text{USSM}} = \lambda S(H_1 H_2) - y_{ij}^e (H_1 L_i) \bar{E}_j - y_{ij}^d (H_1 Q_i) \bar{D}_j - y_{ij}^u (Q_i H_2) \bar{U}_j$$

$$h_1^0 \rightarrow \frac{v_1}{\sqrt{2}} + h_1^0, \quad h_2^0 \rightarrow \frac{v_2}{\sqrt{2}} + h_2^0, \quad s \rightarrow \frac{v_s}{\sqrt{2}} + s$$

mSUGRA-inspired GUT constraint:

$$(m_f^2)_{ij}(M_X) = m_0^2 \delta_{ij} \quad (f = q, \ell, u, d, e),$$

$$A_{ij}^f(M_X) = A_0, \quad (f = u, d, e, \lambda),$$

$$M_i(M_X) = M_{1/2} \quad (i = 1, 2, 3, 4).$$

EWsb output: $m_{h_1}^2(M_S), m_{h_2}^2(M_S), m_s^2(M_S)$

E_6 SSM

$$SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)_N$$

$$\begin{aligned}\mathcal{W}_{E_6SSM} = & \lambda_3 S_3(H_{13}H_{23}) - y_{ij}^e(H_{13}L_i)\bar{E}_j - y_{ij}^d(H_{13}Q_i)\bar{D}_j - y_{ij}^u(Q_iH_{23})\bar{U}_j \\ & + \kappa_{ij}S_3(X_i\bar{X}_j) + \lambda_{\alpha\beta}S_3(H_{1\alpha}H_{2\beta}) + \mu'(H'\bar{H}')\end{aligned}$$

$$h_1^0 \rightarrow \frac{v_1}{\sqrt{2}} + h_1^0, \quad h_2^0 \rightarrow \frac{v_2}{\sqrt{2}} + h_2^0, \quad s \rightarrow \frac{v_s}{\sqrt{2}} + s$$

mSUGRA-inspired GUT constraint:

$$(m_f^2)_{ij}(M_X) = m_0^2 \delta_{ij} \quad (\forall \text{ scalars, except } h_1, h_2, s),$$

$$A_{ij}^f(M_X) = A_0, \quad (f = u, d, e, \lambda, \kappa),$$

$$M_i(M_X) = M_{1/2} \quad (i = 1, 2, 3, 4).$$

EWsb output: $m_{h_1}^2(M_S), m_{h_2}^2(M_S), m_s^2(M_S)$

E_6 SSM-Teilcheninhalt

Feld	$G_{\text{SM}} \times U(1)_N$	$SU(5) \times U(1)_N$	E_6
$Q_i = (Q_{u_i} \ Q_{d_i})$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6}, 1)_i$	$\left. \begin{array}{l} (\mathbf{10}, 1)_i \\ (\bar{\mathbf{5}}, 2)_i \\ (\bar{\mathbf{5}}, -3)_i \\ (\mathbf{5}, -2)_i \\ (\mathbf{1}, 5)_i \\ (\mathbf{1}, 0)_i \end{array} \right\}$	$(27)_i$
\bar{U}_i	$(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3}, 1)_i$		
\bar{E}_i	$(\mathbf{1}, \mathbf{1}, 1, 1)_i$		
\bar{D}_i	$(\bar{\mathbf{3}}, \mathbf{1}, \frac{1}{3}, 2)_i$		
$L_i = (L_{\nu_i} \ L_{e_i})$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2}, 2)_i$		
\bar{X}_i	$(\bar{\mathbf{3}}, \mathbf{1}, \frac{1}{3}, -3)_i$		
$H_{1i} = (H_{1i}^0 \ H_{1i}^-)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2}, -3)_i$		
X_i	$(\mathbf{3}, \mathbf{1}, -\frac{1}{3}, -2)_i$		
$H_{2i} = (H_{2i}^+ \ H_{2i}^0)$	$(\mathbf{1}, \mathbf{2}, \frac{1}{2}, -2)_i$		
S_i	$(\mathbf{1}, \mathbf{1}, 0, 5)_i$		
\bar{N}_i	$(\mathbf{1}, \mathbf{1}, 0, 0)_i$		
$H' = (H'^0 \ H'^-)$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2}, 2)$	$\ni (\bar{\mathbf{5}}, 2)'$	$\ni (27)'$
$\bar{H}' = (\bar{H}'^+ \ \bar{H}'^0)$	$(\mathbf{1}, \mathbf{2}, \frac{1}{2}, -2)$	$\ni (\mathbf{5}, -2)'$	$\ni (\bar{27})'$
V_g^a	$(\mathbf{8}, \mathbf{1}, 0, 0)$	$\ni (\mathbf{24}, 0)$	$\ni (78)$
V_W^i	$(\mathbf{1}, \mathbf{3}, 0, 0)$	$\ni (\mathbf{24}, 0)$	$\ni (78)$
V_Y	$(\mathbf{1}, \mathbf{1}, 0, 0)$	$\ni (\mathbf{24}, 0)$	$\ni (78)$
V_N	$(\mathbf{1}, \mathbf{1}, 0, 0)$	$\ni (\mathbf{1}, 0)$	$\ni (78)$

Brechung der E_6

het. Stringtheorie: $E_8 \times E'_8$



SUSY-Eichtheorie: $E_6 \rightarrow SO(10) \times U(1)_\psi$

$\hookrightarrow SU(5) \times U(1)_\chi$

$\hookrightarrow SU(3)_c \times \underbrace{SU(2)_L \times U(1)_Y}_{\rightarrow U(1)_{\text{em}}}$

het. Stringtheorie: $SO(32)$



SUSY-Eichtheorie: $SO(10) \times U(1)_\psi$

$\hookrightarrow SU(5) \times U(1)_\chi$

$\hookrightarrow SU(3)_c \times SU(2)_L \times U(1)_Y$

Brechung der E_6

Zerlegung der E_6 bezüglich $SO(10) \times U(1)_\psi$:

$$(\mathbf{27})_{E_6} \rightarrow (\mathbf{16}, 1) + (\mathbf{10}, -2) + (\mathbf{1}, 4)$$

$$(\mathbf{78})_{E_6} \rightarrow (\mathbf{45}, 0) + (\mathbf{16}, -3) + (\overline{\mathbf{16}}, 3) + (\mathbf{1}, 0)$$

Zerlegung der $SO(10)$ bezüglich $SU(5) \times U(1)_\chi$:

$$(\mathbf{10})_{SO(10)} \rightarrow (\mathbf{5}, -2) + (\overline{\mathbf{5}}, 2)$$

$$(\mathbf{45})_{SO(10)} \rightarrow (\mathbf{24}, 0) + (\mathbf{10}, -4) + (\overline{\mathbf{10}}, 4) + (\mathbf{1}, 0)$$

$$(\mathbf{16})_{SO(10)} \rightarrow (\mathbf{10}, 1) + (\overline{\mathbf{5}}, -3) + (\mathbf{1}, 5)$$

Dynkin-Diagramme halbeinfacher Lie-Algebren

Order	Cartan's Notation	Group	Dynkin Diagram	Solutions
$l(l+2)$	A_l	$SU(l+1)$		$e_i - e_j (i, j = 1, \dots, l+1)$
$l(2l+1)$ $l \geq 2$	B_l	$SO(2l+1)$		$\pm e_i$ and $\pm e_i \pm e_j (i, j = 1, \dots, l)$
$l(2l+1)$ $l \geq 3$	C_l	$Sp(2l)$		$\pm 2e_i$ and $\pm e_i \pm e_j (i, j = 1, \dots, l)$
$l(2l-1)$ $l \geq 4$	D_l	$SO(2l)$		$\pm e_i \pm e_j (i, j = 1, \dots, l)$
14	G_2	G_2		$e_i - e_j (i, j = 1, 2, 3; i \neq j)$ $\pm 2e_i \mp e_j \mp e_k (i, j, k = 1, 2, 3, i \neq j \neq k)$
52	F_4	F_4		As for B_4 plus the 16 solutions $\frac{1}{2}(\pm e_1 \pm e_2 \pm e_3 \pm e_4)$
78	E_6	E_6		As for A_5 plus solutions $\pm \sqrt{2}e_i$ and $\frac{1}{2}(\pm e_1 \pm e_2 \pm e_3 \pm e_4 \pm e_5 \pm e_6) \pm e_7/\sqrt{2}$ (an arbitrary choice of 3 "+" and 3 "-" signs for the terms in parentheses)
133	E_7	E_7		As for A_7 plus the solutions $\frac{1}{2}(\pm e_1 \pm e_2 \pm e_3 \pm e_4 \pm e_5 \pm e_6 \pm e_7 \pm e_8)$ (an arbitrary choice of 4 "+" and 4 "-" signs for the terms in parentheses)
248	E_8	E_8		As for D_8 plus the solutions $\frac{1}{2}(\pm e_1 \pm e_2 \pm e_3 \pm e_4 \pm e_5 \pm e_6 \pm e_7 \pm e_8)$ with an even number of plus signs.

$$U(1) \subset SU(2) \subset SU(3) \subset SU(4) \subset SU(5) \subset SO(10) \subset E_6 \subset E_7 \subset E_8$$

E_6 SSM EWSB-Gleichungen (tree-level)

$$0 = \frac{\partial V}{\partial v_d} = m_{h_{13}}^2 v_d - \frac{\lambda_3 A_{\lambda_3}}{\sqrt{2}} v_s v_u + \frac{\lambda_3^2}{2} (v_u^2 + v_s^2) v_d + \frac{\bar{g}^2}{8} (v_d^2 - v_u^2) v_d$$

$$+ \frac{g_N^2}{2} \left(\frac{N_{H_{13}}}{2} v_d^2 + \frac{N_{H_{23}}}{2} v_u^2 + \frac{N_{S_3}}{2} v_s^2 \right) \frac{N_{H_{13}}}{2} v_d$$

$$0 = \frac{\partial V}{\partial v_u} = m_{h_{23}}^2 v_u - \frac{\lambda_3 A_{\lambda_3}}{\sqrt{2}} v_s v_d + \frac{\lambda_3^2}{2} (v_d^2 + v_s^2) v_u + \frac{\bar{g}^2}{8} (v_u^2 - v_d^2) v_u$$

$$+ \frac{g_N^2}{2} \left(\frac{N_{H_{13}}}{2} v_d^2 + \frac{N_{H_{23}}}{2} v_u^2 + \frac{N_{S_3}}{2} v_s^2 \right) \frac{N_{H_{23}}}{2} v_u$$

$$0 = \frac{\partial V}{\partial v_s} = m_{S_3}^2 v_s - \frac{\lambda_3 A_{\lambda_3}}{\sqrt{2}} v_d v_u + \frac{\lambda_3^2}{2} (v_d^2 + v_u^2) v_s$$

$$+ \frac{g_N^2}{2} \left(\frac{N_{H_{13}}}{2} v_d^2 + \frac{N_{H_{23}}}{2} v_u^2 + \frac{N_{S_3}}{2} v_s^2 \right) \frac{N_{S_3}}{2} v_s$$

mit $\bar{g}^2 = g_Y^2 + g_2^2$

Sanfte Supersymmetrie-Brechung

$$\begin{aligned}\mathcal{L}_{\text{soft}} = & -m_{ij}^2 \phi_i^* \phi_j - \frac{1}{2} (M \lambda^a \lambda^a + \text{h.c.}) \\ & + \left(\frac{1}{3!} A_{ijk} \phi_i \phi_j \phi_k - \frac{1}{2} B_{ij} \phi_i \phi_j + C_i \phi_i + \text{h.c.} \right)\end{aligned}$$

Gravity Mediated SUSY Breaking (PMSB)

Superpotential includes effective gravitational interactions:

$$\mathcal{W} = \mathcal{W}_{\text{MSSM}} - \frac{1}{M_{\text{Pl}}} \left[y^{Xijk} X \Phi_i \Phi_j \Phi_k + \mu^{Xij} X \Phi_i \Phi_j + \dots \right]$$

$$K = \Phi_i^\dagger \Phi_i + \frac{1}{M_{\text{Pl}}} \left[n^{ij} X + \bar{n}^{ij} X^\dagger \right] \Phi_i^\dagger \Phi_j - \frac{1}{M_{\text{Pl}}^2} k^{ij} X X^\dagger \Phi_i^\dagger \Phi_j$$

X and X^\dagger break SUSY via an F -term VEV:

$$X \rightarrow \theta \theta \langle F \rangle \quad X^\dagger \rightarrow \bar{\theta} \bar{\theta} \langle F \rangle^*$$

Integrate X out \Rightarrow

$$\begin{aligned} -\mathcal{L}_{\text{soft}} &= \frac{\langle F \rangle}{M_{\text{Pl}}} \left[f_A \lambda^A \lambda^A + g^{ijk} \phi_i \phi_j \phi_k + h^{ij} \phi_i \phi_j + k^i \phi_i + \text{h.c.} \right] \\ &\quad + \frac{|\langle F \rangle|^2}{M_{\text{Pl}}^2} m^{ij} \phi_i^* \phi_j \end{aligned}$$

Gauge Mediated SUSY Breaking (GMSB)

Messenger Superfields transform under $SU(3)_c \times SU(2)_L \times U(1)_Y$:

$$\mathcal{Q} = (\mathbf{3}, \mathbf{1}, -1/3), \quad \ell = (\mathbf{1}, \mathbf{2}, 1/2), \quad \bar{\mathcal{Q}}, \quad \bar{\ell}$$

Coupled to a gauge singlet S in the messenger sector:

$$\mathcal{W}_{\text{mess}} = y_2 S \ell \bar{\ell} + y_3 S \mathcal{Q} \bar{\mathcal{Q}}$$

Scalar and F -component of S get VEVs $\langle S \rangle$ and $\langle F_S \rangle$

\Rightarrow SUSY broken in messenger sector

SUSY breaking is communicated to the MSSM via loop diagrams:

$$\bar{B}, \bar{W}, \bar{g} \sim \begin{array}{c} \langle F_S \rangle \\ \hbox{\scriptsize wavy line} \\ \hbox{\scriptsize dashed circle} \end{array} \sim \frac{g_i^2}{(4\pi)^2} \frac{\langle F_S \rangle}{\langle S \rangle} \lambda_i \lambda_i$$

ATLAS SUSY Searches* - 95% CL Lower Limits

Status: ICHEP 2014

ATLAS Preliminary

$\sqrt{s} = 7, 8 \text{ TeV}$

Reference

Model	e, μ, τ, γ	Jets	E_T^{miss}	$\int L dt (\text{fb}^{-1})$	Mass limit	
Inclusive Searches	MSUGRA/CMSSM	0	2-6 jets	Yes	20.3	\tilde{q}, \tilde{g}
	MSUGRA/CMSSM	1 e, μ	3-6 jets	Yes	20.3	\tilde{g}
	MSUGRA/CMSSM	0	7-10 jets	Yes	20.3	\tilde{g}
	$\tilde{q}\bar{q}, \tilde{g}\rightarrow\tilde{q}\bar{q}\chi_1^0$	0	2-6 jets	Yes	20.3	\tilde{g}
	$\tilde{g}, \tilde{g}\rightarrow\tilde{q}\bar{q}\chi_1^0$	0	2-6 jets	Yes	20.3	\tilde{g}
	$\tilde{g}, \tilde{g}\rightarrow\tilde{q}\bar{q}\chi_1^0$	1 e, μ	3-6 jets	Yes	20.3	\tilde{g}
	$\tilde{g}, \tilde{g}\rightarrow\tilde{q}\bar{q}\chi_1^0$	2 e, μ	0-3 jets	-	20.3	\tilde{g}
	GMSB ($T \text{ NLSP}$)	1-2 e, μ	2-4 jets	Yes	4.7	\tilde{g}
	GGM (bino NLSP)	2 e, μ	0 jets	Yes	20.3	\tilde{g}
	GGM (higgsino-bino NLSP)	1 $e, \mu, \tau + \gamma$	-	Yes	4.8	\tilde{g}
	GGM (higgsino-bino NLSP)	τ	1 b	Yes	4.8	\tilde{g}
	GGM (higgsino NLSP)	2 e, μ (Z)	0-3 jets	Yes	5.8	\tilde{g}
	Gravitino LSP	0	mono-jet	Yes	10.5	\tilde{g}
	$\tilde{g}\rightarrow b\bar{b}\chi_1^0$	0	3 b	Yes	20.1	\tilde{g}
	$\tilde{g}\rightarrow c\bar{c}\chi_1^0$	0	7-10 jets	Yes	20.3	\tilde{g}
	$\tilde{g}\rightarrow s\bar{s}\chi_1^0$	0.1 e, μ	3 b	Yes	20.1	\tilde{g}
	$\tilde{g}\rightarrow t\bar{t}\chi_1^0$	0.1 e, μ	3 b	Yes	20.1	\tilde{g}
$3^{\text{rd}} \text{ gen. squarks}$ direct signal	$\tilde{b}_1, \tilde{b}_2, \tilde{b}_1\rightarrow\tilde{b}\tilde{b}^0$	0	2 b	Yes	20.1	\tilde{b}_1
	$\tilde{b}_1, \tilde{b}_2, \tilde{b}_1\rightarrow\tilde{b}\tilde{b}^0$	2 e, μ (SS)	0-3 b	Yes	20.3	\tilde{b}_1
	$\tilde{b}_1(\text{light}), \tilde{b}_1\rightarrow\tilde{b}\tilde{b}^0$	1-2 e, μ	1-2 jets	Yes	4.7	\tilde{b}_1
	$\tilde{b}_1(\text{medium}), \tilde{b}_1\rightarrow W\tilde{b}\tilde{b}^0$	2 e, μ	0-2 jets	Yes	20.3	\tilde{b}_1
	$\tilde{b}_1(\text{medium}), \tilde{b}_1\rightarrow\tilde{b}\tilde{b}^0$	2 e, μ	2 jets	Yes	20.3	\tilde{b}_1
	$\tilde{b}_1(\text{medium}), \tilde{b}_1\rightarrow\tilde{b}\tilde{b}^0$	2 e, μ	2 jets	Yes	20.1	\tilde{b}_1
	$\tilde{b}_1(\text{heavy}), \tilde{b}_1\rightarrow\tilde{b}\tilde{b}^0$	1-2 e, μ	1 b	Yes	20	\tilde{b}_1
	$\tilde{b}_1(\text{heavy}), \tilde{b}_1\rightarrow\tilde{b}\tilde{b}^0$	1-2 e, μ	2 b	Yes	20.1	\tilde{b}_1
	$\tilde{b}_1(\text{heavy}), \tilde{b}_1\rightarrow\tilde{b}\tilde{b}^0$	0	mono-jet+tag	Yes	20.3	\tilde{b}_1
	$\tilde{b}_1(\text{neutral GMSB})$	2 e, μ (Z)	1 b	Yes	20.3	\tilde{b}_1
	$\tilde{b}_1(\text{neutral GMSB})$	3 e, μ (Z)	1 b	Yes	20.3	\tilde{b}_1
	$\tilde{b}_2, \tilde{b}_2\rightarrow\tilde{t}_2 + Z$	0	2 b	Yes	20.3	\tilde{b}_2
EW direct	$\tilde{l}_{1,2}, \tilde{l}_{1,2}\rightarrow\tilde{l}\tilde{l}^0$	2 e, μ	0	Yes	20.3	\tilde{l}
	$\tilde{l}_{1,2}, \tilde{l}_{1,2}\rightarrow\tilde{l}\tilde{l}^0$	2 e, μ	0	Yes	20.3	\tilde{l}
	$\tilde{l}_{1,2}, \tilde{l}_{1,2}\rightarrow\tilde{l}\tilde{l}^0$	2 τ	-	Yes	20.3	\tilde{l}
	$\tilde{l}_{1,2}, \tilde{l}_{1,2}\rightarrow\tilde{l}\tilde{l}^0$	3 e, μ	0	Yes	20.3	\tilde{l}
	$\tilde{l}_{1,2}, \tilde{l}_{1,2}\rightarrow\tilde{l}\tilde{l}^0$	2-3 e, μ	0	Yes	20.3	\tilde{l}
	$\tilde{l}_{1,2}, \tilde{l}_{1,2}\rightarrow W\tilde{l}_1 Z\tilde{l}_2$	1-2 e, μ	2 b	Yes	20.3	\tilde{l}
	$\tilde{l}_{1,2}, \tilde{l}_{1,2}\rightarrow W\tilde{l}_1 Z\tilde{l}_2$	4 e, μ	0	Yes	20.3	\tilde{l}
Long-lived particles	Direct $\tilde{l}, \tilde{l} \rightarrow l \text{ prod.}$, long-lived $\tilde{\chi}_1^0$	Disparr. trk	1 jet	Yes	20.3	\tilde{l}, \tilde{l}^0
	Stable $\tilde{l}, \tilde{l} \rightarrow R$ -hadron	0	1-5 jets	Yes	27.9	\tilde{l}, \tilde{l}^0
	GMSSB, stable $\tilde{\tau}, \tilde{\tau} \rightarrow \tilde{\ell}, \tilde{\nu}, \tilde{\mu}, \tau, \tau, \mu, \tau, \mu, \tau, \mu$	1-2 μ	-	-	15.9	$\tilde{\tau}, \tilde{\tau}^0$
	GMSB, $\tilde{\chi}_1^0 \rightarrow q\bar{q}$, long-lived $\tilde{\chi}_1^0$	2 γ	-	Yes	4.7	$\tilde{\chi}_1^0, \tilde{\chi}_1^0$
	$\tilde{q}, \tilde{q} \rightarrow qq$ (RPV)	1 μ , displ. vtx	-	Yes	20.3	\tilde{q}, \tilde{q}
	LFV $p\bar{p} \rightarrow \tilde{e}, X, \tilde{e} \tilde{v} \rightarrow e \mu$	2 e, μ	-	-	4.6	\tilde{e}, \tilde{e}^0
RPV	LFV $p\bar{p} \rightarrow \tilde{e}, X, \tilde{e} \tilde{v} \rightarrow \tilde{e} \mu + T$	1 $e, \mu + \tau$	-	-	4.6	\tilde{e}, \tilde{e}^0
	Bilinear RPV CMSSM	2 e, μ (SS)	0-3 b	Yes	20.3	\tilde{e}, \tilde{e}^0
	$\tilde{e}_1^{\pm}, \tilde{e}_1^{\pm}, \tilde{e}_1^{\pm} \rightarrow W\tilde{l}_1^{\pm}, \tilde{e}\nu\tilde{v}_1^{\pm}, \tilde{e}\bar{\nu}_1^{\pm}$	4 e, μ	-	Yes	20.3	$\tilde{e}_1^{\pm}, \tilde{e}_1^{\pm}$
	$\tilde{e}_1^{\pm}, \tilde{e}_1^{\pm}, \tilde{e}_1^{\pm} \rightarrow W\tilde{l}_1^{\pm}, \tilde{e}\nu\tilde{v}_1^{\pm}, \tilde{e}\bar{\nu}_1^{\pm}$	3 $e, \mu + \tau$	-	Yes	20.3	$\tilde{e}_1^{\pm}, \tilde{e}_1^{\pm}$
	$\tilde{e}_1^{\pm}, \tilde{e}_1^{\pm}, \tilde{e}_1^{\pm} \rightarrow 6-7 \text{ jets}$	0	6-7 jets	Yes	20.3	$\tilde{e}_1^{\pm}, \tilde{e}_1^{\pm}$
	$\tilde{g} \rightarrow \tilde{t}_1 \tilde{t}_2$	2 e, μ (SS)	0-3 b	Yes	20.3	\tilde{g}
	$\tilde{g} \rightarrow b\bar{b} \tilde{\chi}_1^0$	0	4 jets	-	4.6	\tilde{g}
Other	Scalar gluon pair, sgluon $\rightarrow q\bar{q}$	0	4 jets	-	4.6	sgluon
	Scalar gluon pair, sgluon $\rightarrow i\bar{i}$	2 e, μ	2 b	Yes	14.3	sgluon
	WIMP interaction (D_ϕ , Dirac χ)	0	mono-jet	Yes	10.5	M _{wimp}

$\sqrt{s} = 7 \text{ TeV}$

full data

$\sqrt{s} = 8 \text{ TeV}$

partial data

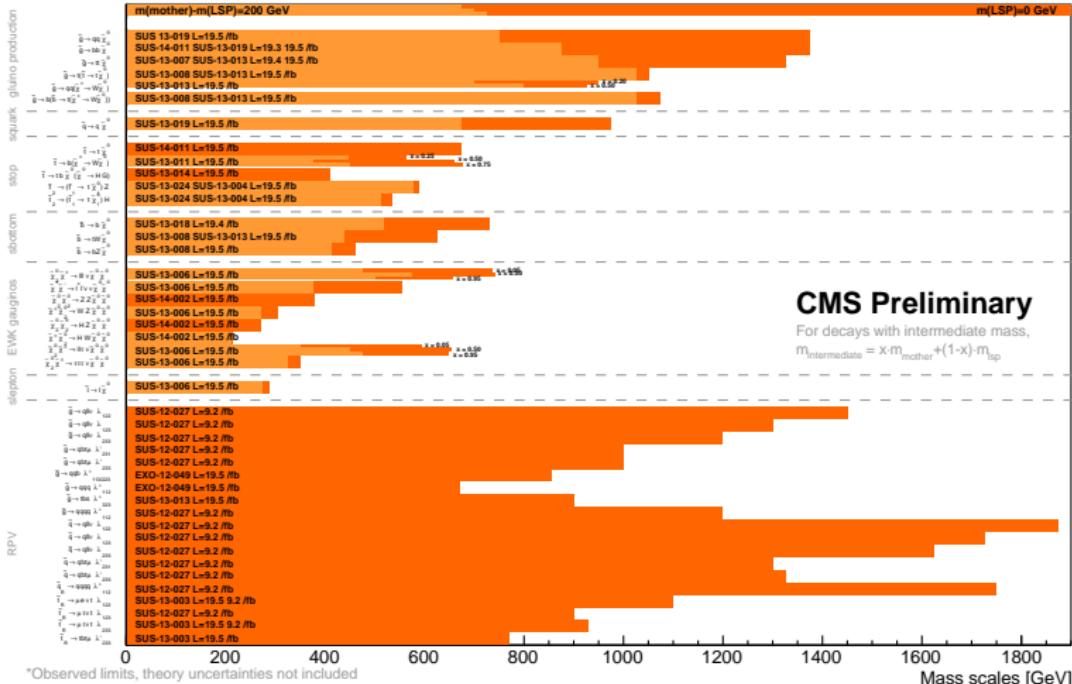
$\sqrt{s} = 8 \text{ TeV}$

full data

*Only a selection of the available mass limits on new states or phenomena is shown. All limits quoted are observed minus 1 σ theoretical signal cross section uncertainty.

Summary of CMS SUSY Results* in SMS framework

ICHEP 2014



*Observed limits, theory uncertainties not included
 Only a selection of available mass limits
 Probe "up" to the quoted mass limit