

# Precise Higgs mass prediction in SUSY and non-SUSY models

Alexander Voigt

Aachen–Bonn–Heidelberg–Mainz research group meeting  
“The Future of Searches for Invisible Particles”

14.12.2017

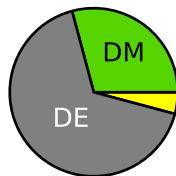
# Contents

- ① BSM Physics and extended Higgs sectors
- ② Higgs mass calculation
  - at fixed loop order
  - in an EFT
  - in a mixed approach
- ③ Current status of Higgs mass prediction in the MSSM
- ④ Summary

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# Why to search for physics beyond the SM?



## Questions:

- What does Dark Matter consist of?
- What causes the deviation of  $(g - 2)_{\mu}$ ?
- Is the vacuum stable up to  $M_{\text{Pl}}$ ?
- Why is  $M_h = 125$  GeV?
- Can the SM Yukawa couplings be predicted?
- Is there a solution to the hierarchy problem?
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Many proposed BSM models to address some of these questions:  
Supersymmetry, Dark Matter models, extra dimensions, . . .

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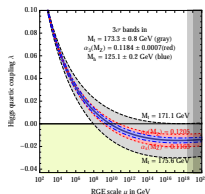


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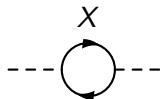


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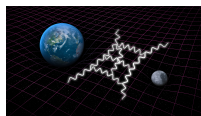
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[SLAC]

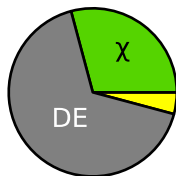
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Still an attractive extension of the Standard Model!  
But not necessarily minimal Supersymmetry.



## Features:

- can provide a Dark Matter candidate
- can explain deviation of  $(g - 2)_\mu$
- can stabilize the electroweak vacuum (see later)
- can predict the SM-like Higgs mass (see later)
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**Problem:** LHC has not found any SUSY particles so far  $\Rightarrow$  SUSY particles are probably heavy

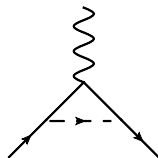
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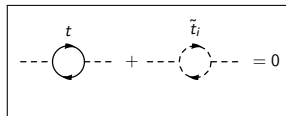
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$$E_8 \times E_8 \rightarrow E_6 \rightarrow G_{\text{SM}}$$

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# Current limits on SUSY particle masses

## ATLAS SUSY Searches\* - 95% CL Lower Limits

May 2017

ATLAS Preliminary

$\sqrt{s} = 7, 8, 13 \text{ TeV}$

Model	$\epsilon, \mu, \tau, \gamma$	Jets	$E_T^{\text{miss}}$	$[\mathcal{L} \text{ d}(\text{fb}^{-1})]$	Mass limit	$\sqrt{s} = 7, 8 \text{ TeV}$	$\sqrt{s} = 13 \text{ TeV}$	Reference	
Inclusive Searches	MSUGRA/CMSSM	$0.3 \epsilon, \mu, \tau + 2 \epsilon$	2.10 jets/3 b	Yes	20.3	#	1.85 TeV	$m(\tilde{g})=m(\tilde{u})$ 1507.05525	
	$\tilde{g}, \tilde{u}, \tilde{d}$	0	2 jets	Yes	36.1	#	1.57 TeV	$m(\tilde{g})=200 \text{ GeV}, m(\tilde{t}^*) \text{ gen. q}(m(\tilde{t}^*)^2 \text{ gen. q})$ ATLAS-CONF-2017-022	
	$\tilde{g}, \tilde{u}, \tilde{d}$ (compressed)	mono-jet	1-3 jets	Yes	3.2	#	908 GeV	$m(\tilde{g})=m(\tilde{t}^*)=5 \text{ GeV}$ 1604.07773	
	$\tilde{g}, \tilde{u}, \tilde{d}$	0	2-6 jets	Yes	36.1	#	2.02 TeV	$m(\tilde{g})=200 \text{ GeV}$ ATLAS-CONF-2017-022	
	$\tilde{g}, \tilde{u}, \tilde{d}$	0	2-6 jets	Yes	36.1	#	2.01 TeV	$m(\tilde{g})=200 \text{ GeV}, m(\tilde{t}^*)=0.5 m(\tilde{g})+m(\tilde{g}^*)$ ATLAS-CONF-2017-022	
	$\tilde{g}, \tilde{u}, \tilde{d}$	3	4 jets	Yes	36.1	#	1.825 TeV	$m(\tilde{g})=400 \text{ GeV}$ ATLAS-CONF-2017-030	
	$\tilde{g}, \tilde{u}, \tilde{d}$	0	7-11 jets	Yes	36.1	#	1.8 TeV	$m(\tilde{g})=400 \text{ GeV}$ ATLAS-CONF-2017-033	
	GMSB ( $\tilde{g}$ NLSP)	$1.2 \epsilon + 0.1 \epsilon$	0-2 jets	Yes	3.2	#	2.0 TeV	$m(\tilde{g})=200 \text{ GeV}$ 1607.05979	
	GGM (bino NLSP)	$2 \gamma$	-	Yes	3.2	#	1.65 TeV	$\tau+\tau$ NLSP; $\tau < 0.1 \text{ ns}$ 1606.09150	
	GGM (Higgsino-bino NLSP)	$\gamma$	1 jet	Yes	20.3	#	1.37 TeV	$m(\tilde{g})=950 \text{ GeV}, m(\text{NLSP}) < 0.1 \text{ mm}, \mu=0$ 1507.05493	
	GGM (Higgsino-bino NLSP)	$\gamma$	2 jets	Yes	13.8	#	1.8 TeV	$m(\tilde{g})=600 \text{ GeV}, m(\text{NLSP}) < 0.1 \text{ mm}, \mu=0$ ATLAS-CONF-2016-006	
	GGM (Higgsino NLSP)	$2 \epsilon, \mu$ ( $Z$ )	2 jets	Yes	20.3	#	900 GeV	$m(\tilde{g})=430 \text{ GeV}$ 1503.03390	
Gravitino LSP	0	mono-jet	Yes	20.3	# <sup>17</sup> scale	865 GeV	$m(\tilde{G}) > 1.8 \times 10^{13} \text{ eV}, m(\tilde{g})=m(\tilde{g}^*)=1.5 \text{ TeV}$ 1502.01518		
$\tilde{g}, \tilde{u}, \tilde{d}$ direct	$\tilde{g}, \tilde{u}, \tilde{d}$	0	3 b	Yes	36.1	#	1.92 TeV	$m(\tilde{g})=600 \text{ GeV}$ ATLAS-CONF-2017-021	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$0.1 \epsilon, \mu$	3 b	Yes	36.1	#	1.97 TeV	$m(\tilde{g})=200 \text{ GeV}$ ATLAS-CONF-2017-021	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$0.1 \epsilon, \mu$	3 b	Yes	20.1	#	1.37 TeV	$m(\tilde{g})=300 \text{ GeV}$ 1407.8600	
$\tilde{g}, \tilde{u}, \tilde{d}$ squarks	$\tilde{g}, \tilde{u}, \tilde{d}$	0	2 b	Yes	36.1	#	990 GeV	$m(\tilde{g})=420 \text{ GeV}$ ATLAS-CONF-2017-038	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$2 \epsilon, \mu$ (SS)	1 b	Yes	36.1	#	275-700 GeV	$m(\tilde{g})=200 \text{ GeV}, m(\tilde{t}^*)=m(\tilde{t}^*)+100 \text{ GeV}$ ATLAS-CONF-2017-030	
	$\tilde{g}, \tilde{u}, \tilde{d}$	0-2 $\epsilon, \mu$	1-2 b	Yes	4.71/3.13	#	117-170 GeV	$m(\tilde{g})=2 \text{ GeV}(\tilde{t}^*), m(\tilde{t}^*)=55 \text{ GeV}$ 1309.2102, ATLAS-CONF-2016-077	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$0.2 \epsilon, \mu$	0.2 jets/1-2 b	Yes	20.3/36.1	#	90-196 GeV	$m(\tilde{g})=1 \text{ GeV}$ 1506.08616, ATLAS-CONF-2017-020	
	$\tilde{g}, \tilde{u}, \tilde{d}$	0	mono-jet	Yes	3.2	#	90-323 GeV	$m(\tilde{g}), m(\tilde{t}^*) < 5 \text{ GeV}$ 1604.07773	
	$\tilde{g}, \tilde{u}, \tilde{d}$ (natural GMSB)	$2 \epsilon, \mu$ ( $Z$ )	1 b	Yes	20.3	#	150-600 GeV	$m(\tilde{g}) > 150 \text{ GeV}$ 1403.5222	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$3 \epsilon, \mu$ ( $Z$ )	1 b	Yes	36.1	#	290-790 GeV	$m(\tilde{g})=0 \text{ GeV}$ ATLAS-CONF-2017-019	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$1.2 \epsilon, \mu$	4 b	Yes	36.1	#	320-850 GeV	$m(\tilde{g})=0 \text{ GeV}$ ATLAS-CONF-2017-019	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$2 \epsilon, \mu$	0	Yes	36.1	#	90-440 GeV	$m(\tilde{g})=0$ ATLAS-CONF-2017-039	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$2 \epsilon, \mu$	0	Yes	36.1	#	719 GeV	$m(\tilde{g})=0, m(\tilde{t}^*) > 0.5 m(\tilde{t}^*)+m(\tilde{t}^*)$ ATLAS-CONF-2017-038	
$\tilde{g}, \tilde{u}, \tilde{d}$	$2 \epsilon, \mu$	0	Yes	36.1	#	760 GeV	$m(\tilde{g})=0, m(\tilde{t}^*) > 0.5 m(\tilde{t}^*)+m(\tilde{t}^*)$ ATLAS-CONF-2017-035		
EW direct	$\tilde{g}, \tilde{u}, \tilde{d}$	$2 \epsilon, \mu$	0	Yes	36.1	#	1.16 TeV	$m(\tilde{t}^*)=m(\tilde{t}^*), m(\tilde{t}^*)=0, m(\tilde{t}^*) > 0.5 m(\tilde{t}^*)+m(\tilde{t}^*)$ ATLAS-CONF-2017-039	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$2 \epsilon, \mu$	0-2 jets	Yes	36.1	#	580 GeV	$m(\tilde{g})=m(\tilde{t}^*), m(\tilde{t}^*)=0, \tilde{f}$ decoupled ATLAS-CONF-2017-039	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$2 \epsilon, \mu$	0	Yes	20.3	#	270 GeV	$m(\tilde{g})=m(\tilde{t}^*), m(\tilde{t}^*)=0, \tilde{f}$ decoupled 1501.07110	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$4 \epsilon, \mu$	0	Yes	20.3	#	635 GeV	$m(\tilde{g})=m(\tilde{t}^*), m(\tilde{t}^*)=0, m(\tilde{t}^*) > 0.5 m(\tilde{t}^*)+m(\tilde{t}^*)$ 1405.5086	
	GGM (wino NLSP) weak prod., $\tilde{t}^* \rightarrow \tilde{g}$	$1 \epsilon, \mu + \gamma$	-	Yes	20.3	#	115-370 GeV	$\tau < 1 \text{ mm}$ 1507.05493	
	GGM (bino NLSP) weak prod., $\tilde{t}^* \rightarrow \tilde{g}$	$2 \gamma$	-	Yes	20.3	#	590 GeV	$\tau < 1 \text{ mm}$ 1507.05493	
	Long-lived particles	Direct $\tilde{t}^* \tilde{t}^*$ prod., long-lived $\tilde{t}^*$	Disapp. trk	1 jet	Yes	36.1	#	430 GeV	$m(\tilde{g})=m(\tilde{t}^*)=160 \text{ MeV}, \tau(\tilde{t}^*) > 2 \text{ ns}$ ATLAS-CONF-2017-017
		Direct $\tilde{t}^* \tilde{t}^*$ prod., long-lived $\tilde{t}^*$	dE/dx trk	-	Yes	18.4	#	405 GeV	$m(\tilde{g})=m(\tilde{t}^*)=180 \text{ MeV}, \tau(\tilde{t}^*) > 15 \text{ ns}$ 1506.09332
		Stable $\tilde{g}$ R-hadron	0	1-5 jets	Yes	27.9	#	850 GeV	$m(\tilde{g}) > 100 \text{ GeV}, 10 \mu\text{s} < \tau < 1000 \text{ s}$ 1306.05264
		Metastable $\tilde{g}$ R-hadron	trk	-	3.2	#	#	1.58 TeV	$m(\tilde{g}) > 100 \text{ GeV}, \tau > 10 \text{ ns}$ 1606.05129
Metastable $\tilde{g}$ R-hadron		dE/dx trk	-	3.2	#	#	1.57 TeV	$m(\tilde{g}) > 100 \text{ GeV}, \tau > 10 \text{ ns}$ 1604.04520	
GMSB, stable $\tilde{t}^*, \tilde{t}^* \rightarrow (\tilde{g}, \tilde{u}) + (\nu, \mu)$		1-2 $\mu$	-	Yes	19.1	#	537 GeV	$10 \text{ -} 100 \mu\text{s}$ 1411.6795	
GMSB, $\tilde{t}^* \rightarrow \tilde{g}, \text{ long-lived } \tilde{t}^*$		$2 \gamma$	-	Yes	20.3	#	440 GeV	$1 < \tau(\tilde{t}^*) < 2 \text{ ns}, \text{SPS8 model}$ 1409.5042	
GGM $\tilde{g}, \tilde{t}^* \rightarrow \tilde{g}, \nu + \tilde{g}$		displ. vtx $\mu$ jets	-	Yes	20.3	#	1.0 TeV	$7 < \tau(\tilde{g}) < 740 \text{ mm}, m(\tilde{g}) > 1.3 \text{ TeV}$ 1504.05162	
GGM $\tilde{g}, \tilde{t}^* \rightarrow \tilde{g}, \nu + \tilde{g}$		displ. vtx $\mu$ jets	-	Yes	20.3	#	1.0 TeV	$6 < \tau(\tilde{g}) < 480 \text{ mm}, m(\tilde{g}) > 1.1 \text{ TeV}$ 1504.05162	
RPV		LFV $\tilde{g}\tilde{g}\tilde{g} + X, \tilde{t}^* \rightarrow \nu\tau/\nu\mu$	$\nu\tau/\nu\mu$	-	Yes	3.2	#	1.9 TeV	$A_{12} < 0.11, A_{13} < 0.0000007$ 1607.28079
	Bilinear RPV CMSSM	$2 \epsilon, \mu$ (SS)	0.3 b	Yes	20.3	#	1.45 TeV	$m(\tilde{g})=m(\tilde{t}^*), \tau_{\text{RPV}} < 1 \text{ mm}$ 1404.2500	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$4 \epsilon, \mu + \tau$	-	Yes	13.3	#	1.14 TeV	$m(\tilde{g}) > 400 \text{ GeV}, A_{13} > 0 (\theta = 1, 2)$ ATLAS-CONF-2016-075	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$3 \epsilon, \mu + \tau$	-	Yes	20.3	#	450 GeV	$m(\tilde{g}) > 0.2 \text{ mm}(\tilde{t}^*), A_{13} > 0$ 1405.5086	
	$\tilde{g}, \tilde{u}, \tilde{d}$	0	4.5 large- $\theta$ jets	-	14.8	#	1.08 TeV	$\text{BR}(\tilde{g} \rightarrow \text{RPV}) < \text{BR}(\tilde{g} \rightarrow \text{SM})$ ATLAS-CONF-2016-057	
	$\tilde{g}, \tilde{u}, \tilde{d}$	0	4.5 large- $\theta$ jets	-	14.8	#	1.55 TeV	$m(\tilde{g})=800 \text{ GeV}$ ATLAS-CONF-2016-057	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$1 \epsilon, \mu$	8-10 jets/0-4 b	-	36.1	#	2.1 TeV	$m(\tilde{g})=1 \text{ TeV}, A_{12} > 0$ ATLAS-CONF-2017-013	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$1 \epsilon, \mu$	8-10 jets/0-4 b	-	36.1	#	1.65 TeV	$m(\tilde{g})=1 \text{ TeV}, A_{12} > 0$ ATLAS-CONF-2017-013	
	$\tilde{g}, \tilde{u}, \tilde{d}$	0	2 jets + 2 b	-	15.4	#	410 GeV	$\text{BR}(\tilde{g} \rightarrow \text{RPV}) < 20\%$ ATLAS-CONF-2016-022, ATLAS-CONF-2016-084	
	$\tilde{g}, \tilde{u}, \tilde{d}$	$2 \epsilon, \mu$	2 b	-	36.1	#	0.4-1.45 TeV	$m(\tilde{g})=200 \text{ GeV}$ ATLAS-CONF-2017-036	
Other	Scalar charm, $\tilde{t}^* \rightarrow c\tilde{t}^*$	0	$2 \epsilon$	Yes	20.3	#	510 GeV	$m(\tilde{g})=200 \text{ GeV}$ 1501.01325	

\*Only a selection of the available mass limits on new states or phenomena is shown. Many of the limits are based on simplified models, c.f. refs. for the assumptions made.

10<sup>-1</sup> 1 Mass scale [TeV]

## Higgs sectors in (B)SM models

---

Model	Higgs representations $SU(3)_c \times SU(2)_L \times U(1)_Y \times X$
SM	$(\mathbf{1}, \mathbf{2}, \frac{1}{2})$
2HDM	$(\mathbf{1}, \mathbf{2}, \frac{1}{2}), (\mathbf{1}, \mathbf{2}, \frac{1}{2})$
SSM	$(\mathbf{1}, \mathbf{2}, \frac{1}{2}), (\mathbf{1}, \mathbf{1}, 0)$
MSSM	$(\mathbf{1}, \mathbf{2}, \frac{1}{2}), (\mathbf{1}, \mathbf{2}, -\frac{1}{2})$
NMSSM	$(\mathbf{1}, \mathbf{2}, \frac{1}{2}), (\mathbf{1}, \mathbf{2}, -\frac{1}{2}), (\mathbf{1}, \mathbf{1}, 0)$
MRSSM	$(\mathbf{1}, \mathbf{2}, \frac{1}{2}), (\mathbf{1}, \mathbf{2}, -\frac{1}{2}), (\mathbf{1}, \mathbf{1}, 0), (\mathbf{1}, \mathbf{3}, 0)$
E <sub>6</sub> SSM	$(\mathbf{1}, \mathbf{2}, \frac{1}{2}, -\frac{2}{\sqrt{40}}), (\mathbf{1}, \mathbf{2}, -\frac{1}{2}, -\frac{3}{\sqrt{40}}), (\mathbf{1}, \mathbf{1}, 0, \frac{5}{\sqrt{40}})$
...	

---

Feature of SUSY models: The mass of the SM-like Higgs is a prediction!

# Higgs masses in the SM

Higgs potential

$$V_{\text{Higgs}} = -\mu^2 |\Phi|^2 + \frac{1}{2} \lambda |\Phi|^4$$

Decompose  $\Phi$  as

$$\Phi = \begin{pmatrix} G^\pm \\ \frac{1}{\sqrt{2}}(v + h + iG^0) \end{pmatrix}$$

$\Rightarrow$  mass of the Higgs after EWSB

$$m_h^2 = \lambda v^2 \quad (\text{tree-level})$$

**Until 2012:**  $M_h = ? \Leftrightarrow \lambda = ?$

**Since 2012:**  $M_h \approx 125 \text{ GeV} \Rightarrow \lambda \approx 0.26$

## Higgs masses in the real MSSM

$$\begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix}, \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix} \rightarrow \begin{pmatrix} h \\ H \end{pmatrix}, \begin{pmatrix} G^0 \\ A \end{pmatrix}, \begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix}$$

$$m_{h,H}^2 = \frac{1}{2} \left[ m_Z^2 + m_A^2 \mp \sqrt{(m_Z^2 + m_A^2)^2 - 4m_Z^2 m_A^2 c_{2\beta}^2} \right]$$

$\Rightarrow$  **prediction** (if  $m_A \gg m_Z$ ):

$$m_h^2 \approx m_Z^2 c_{2\beta}^2 \leq (91.2 \text{ GeV})^2 \quad (\text{tree-level})$$

$\Rightarrow M_h \approx 125 \text{ GeV}$  requires **large loop corrections!**

$$M_h^2 = m_h^2 + \Delta m_h^2 \quad \Rightarrow \quad \Delta m_h^2 \geq (85 \text{ GeV})^2$$

Because of large loop corrections  $\Delta m_h^2$ :

$$\Delta M_h^{\text{theo}} \gtrsim (1 \dots 2) \text{ GeV} \quad \text{at least!}$$

$$\Delta M_h^{\text{exp}} = 0.24 \text{ GeV} \quad [\text{PDG-2017}]$$

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# Fixed loop order calculation

Dominant contribution to  $M_h$  at the 1-loop level:

$$(\Delta m_h^2)^{1L} = -\Sigma_h^{1L}(p^2) + \frac{t_h^{1L}}{v}$$

The diagram shows five terms representing 1-loop corrections. The first row contains three terms: a dashed line with a solid loop labeled  $t$ , a dashed line with a dashed loop labeled  $\tilde{t}_i$ , and a dashed line with a dashed loop labeled  $\tilde{t}_i$ . The second row contains two terms: a dashed line with a solid loop labeled  $t$  and a dashed line with a dashed loop labeled  $\tilde{t}_i$ . All loops are oriented counter-clockwise.

$$\approx \frac{12m_t^2 y_t^2}{(4\pi)^2} \left( \ln \frac{M_S^2}{m_t^2} + \frac{X_t^2}{M_S^2} - \frac{X_t^4}{12M_S^4} \right) + O(p^2)$$

## Higgs mass at 1-loop level

$$(\Delta m_h^2)^{1L} \approx \frac{12m_t^2 y_t^2}{(4\pi)^2} \left( \ln \frac{M_S^2}{m_t^2} + \frac{X_t^2}{M_S^2} - \frac{X_t^4}{12M_S^4} \right) + O(p^2)$$

$X_t = A_t - \mu/t_\beta =$  stop mixing parameter,  $M_S = (m_Q)_{33} = (m_U)_{33}$

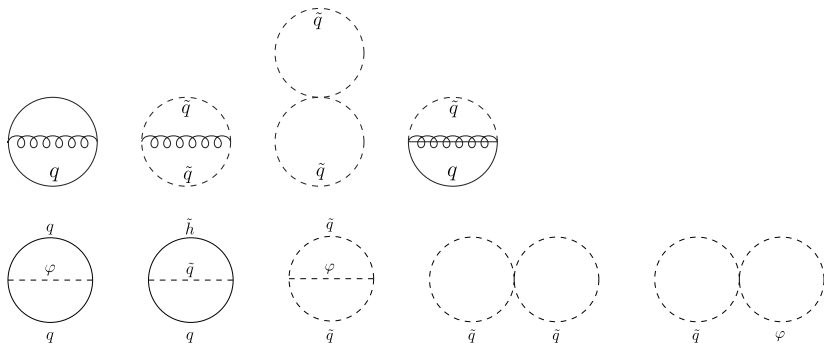
### Observations:

- logarithmically enhanced by  $M_S/m_t$
- maximal for  $X_t \approx \sqrt{6}M_S$
- high sensitivity on  $m_t$ , due to prefactor  $m_t^2 y_t^2 = 2m_t^4/v^2$
- ambiguity of definition of  $m_t$ : pole mass or  $\overline{\text{DR}}$  mass?  
 $M_t \approx 173.3 \text{ GeV}$ ,  $m_t^{\overline{\text{DR}}} \approx 165 \text{ GeV}$   
 $\Rightarrow$  huge theoretical uncertainty!  
 $\Rightarrow$  2-loop calculation needed to resolve this ambiguity
- to get  $M_h \approx 125 \text{ GeV}$ ,  $M_S \gtrsim 5 \text{ TeV}$  needed (see later)



# Higgs mass at 2-loop level

Known contributions:  $O(\alpha_s(\alpha_t + \alpha_b) + (\alpha_t + \alpha_b)^2 + \alpha_\tau^2)$  for  $p^2 = 0$  [hep-ph/0105096, hep-ph/0112177]



## Higgs mass at 2-loop level

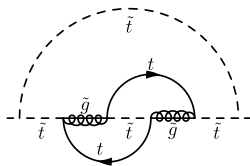
$$\begin{aligned}(\Delta m_h^2)^{2L} &\approx \frac{m_t^2 y_t^4}{(4\pi)^4} \left( c_1 \ln^2 \frac{M_S^2}{m_t^2} + c_2 \ln \frac{M_S^2}{m_t^2} + c_3 \right) \\ &+ \frac{m_t^2 y_t^2 g_3^2}{(4\pi)^4} \left( c_4 \ln^2 \frac{M_S^2}{m_t^2} + c_5 \ln \frac{M_S^2}{m_t^2} + c_6 \right)\end{aligned}$$

### Observations:

- logarithmically enhanced by  $M_S/m_t$
- still high sensitivity on  $m_t$
- ambiguity of definition of  $m_t$  is resolved ✓
- ambiguity of definition of  $\alpha_s$ :  $\alpha_s^{\text{SM}}(M_Z)$ ,  $\alpha_s^{\text{MSSM}}(M_S)$ , ... ?  
⇒ 3-loop calculation needed to resolve this ambiguity

# Higgs mass at 3-loop level

Known contributions:  $O(\alpha_t \alpha_s^2)$  for  $p^2 = 0$  [1005.5709]



$$(\Delta m_h^2)^{3L} \approx \frac{m_t^2 y_t^2 g_3^4}{(4\pi)^6} \left( c_7 \ln^3 \frac{M_S^2}{m_t^2} + c_8 \ln^2 \frac{M_S^2}{m_t^2} + c_9 \ln \frac{M_S^2}{m_t^2} + c_{10} \right)$$

## Observations:

- logarithmically enhanced by  $M_S/m_t$
- still high sensitivity on  $m_t$
- ambiguity of definition of  $m_t$  is resolved ✓
- ambiguity of definition of  $\alpha_s$  is resolved ✓

# Summary of fixed loop order calculation

Typical order of magnitude of loop contributions (depends on parameter scenario):

$$M_h = m_h + \Delta m_h^{1L} + \Delta m_h^{2L} + \Delta m_h^{3L} + \dots \\ \approx [91 + O(20 \dots 30) + O(2 \dots 4) + O(1 \dots 2)] \text{ GeV}$$

## Advantages:

- includes logarithmic, non-logarithmic and suppressed terms of the order  $O(v^2/M_S^2)$  at fixed loop order
- precise prediction if  $M_S \sim m_t$

## Problem:

- large logarithmic corrections, if  $M_S \gg m_t$   
 $\Rightarrow$  slow convergence of perturbation series  
 $\Rightarrow$  large theoretical uncertainty, (1–2 GeV, or more)  
recall:  $M_h^{\text{exp}} = (125.09 \pm 0.24) \text{ GeV}$

**Note:** 3-loop MSSM calculation implemented in FS+H [1708.05720]

# Contents

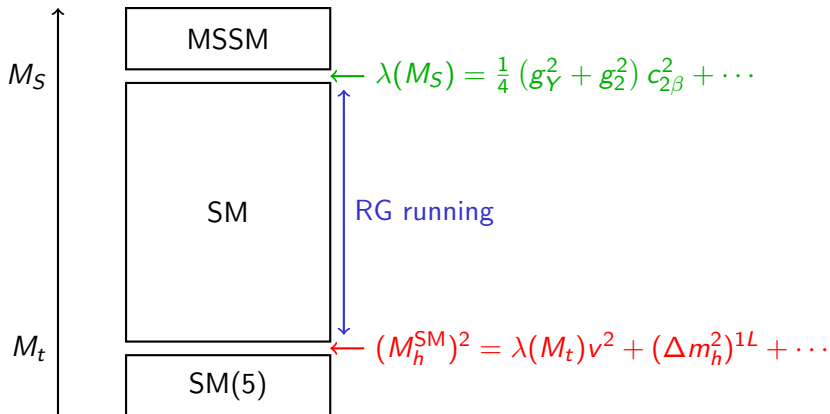
- ① BSM Physics and extended Higgs sectors
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# Higgs mass calculation in an EFT

**Idea:** Integrate out SUSY particles at  $M_S$  (expand in  $v^2/M_S^2$ )

$\Rightarrow \lambda(M_S)$  is fixed by the MSSM

$\Rightarrow$  effectively: separation of scales  $M_S$  and  $M_t$ .



# EFT avoids large logarithmic corrections

- ① Calculate  $\lambda$  from the condition ( $p^2 = v^2 = 0$ ):

$$\partial_{p^2}^{(k)} \Gamma_{h,\dots,h}^{\text{MSSM},(n)} = \partial_{p^2}^{(k)} \Gamma_{h,\dots,h}^{\text{SM},(n)}$$

$\Rightarrow$

$$\begin{aligned}\lambda(Q) &= \frac{1}{4} \left[ g_Y^2 + g_2^2 \right] c_{2\beta}^2 + \Delta\lambda^{1L} + \Delta\lambda^{2L} + \dots \\ &= \frac{1}{4} \left[ g_Y^2 + g_2^2 \right] c_{2\beta}^2 + \frac{12m_t^2 y_t^2}{(4\pi)^2 v^2} \left[ \ln \frac{M_S^2}{Q^2} + \frac{X_t^2}{M_S^2} - \frac{X_t^4}{12M_S^4} \right] + \dots\end{aligned}$$

$\Rightarrow$  no large logs for  $Q \approx M_S$

- ② RG running of  $\lambda$  from  $Q = M_S \rightarrow M_t$ .

$\Rightarrow$  logs are resummed to all orders

- ③ Calculate  $M_h$  in the SM at  $Q = M_t$ :

$$(M_h^{\text{SM}})^2 = \lambda(Q)v^2 + \frac{12m_t^2 y_t^2}{(4\pi)^2 v^2} \ln \frac{Q^2}{m_t^2} + \dots$$

$\Rightarrow$  no large logs for  $Q \approx M_t$

# Summary of EFT approach

Typical order of magnitude of loop contributions (depends on parameter scenario, here  $X_t = 0$ ,  $M_S = 20$  TeV):

$$M_h = m_h + \Delta m_h^{1L} + \Delta m_h^{2L} + \Delta m_h^{3L} + \dots \\ \approx [O(124) + O(0.5 \dots 1) + O(0.1 \dots 0.2) + O(0.02 \dots 0.04)] \text{ GeV}$$

## Advantages:

- large logarithmic fixed order loop corrections are avoided
- large logarithms  $\propto \ln(M_S/M_t)$  are resummed to all orders

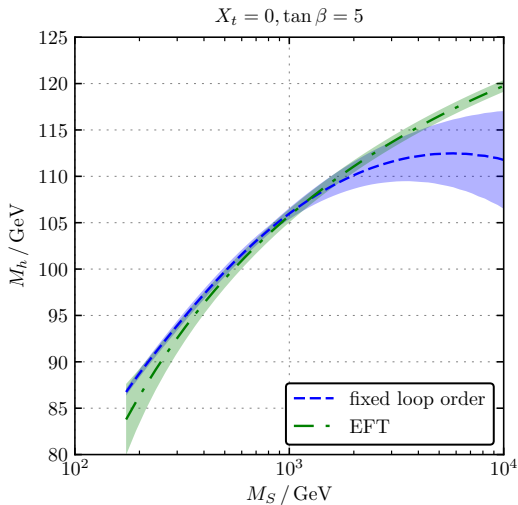
**Disadvantage:** usually terms  $O(v^2/M_S^2)$  are neglected

$\Rightarrow$  imprecise when  $v \sim M_S$

$\Rightarrow$  large theoretical uncertainty when  $v \sim M_S$



# Comparison of fixed-order and EFT approaches



## Summary of fixed-order and EFT approaches

	low $M_S$ $M_S \lesssim 2 \text{ TeV}$	high $M_S$ $M_S \gtrsim 2 \text{ TeV}$
fixed-order	✓	✗
EFT	✗	✓
? mixed	✓	✓

Q: Can the fixed-order and EFT approaches be combined?

A: Yes! [1312.4937, 1609.00371, 1710.03760]

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# Mixed fixed-order and EFT approaches

**Goal:** resum large logarithms **and** include suppressed  $O(v^2/M_S^2)$  terms

## Two known approaches:

- FeynHiggs [1312.4937]: Replace logs from fixed-order calculation by resummed logs

$$M_h^2 = (M_h^2)_{\text{fixed-order}} - (M_h^2)_{\text{logs}} + (M_h^2)_{\text{resummed logs}}$$

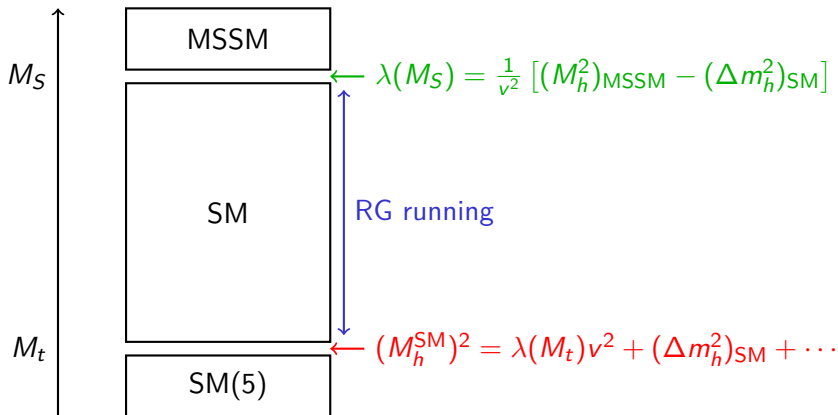
- FlexibleEFTHiggs [1609.00371, 1710.03760]: Incorporate  $O(v^2/M_S^2)$  terms into  $\lambda$  by using the matching condition

$$(M_h^2)_{\text{SM}} \stackrel{!}{=} (M_h^2)_{\text{MSSM}} \quad \text{at 1L level at } Q = M_S$$

# FlexibleEFTHiggs approach [1609.00371, 1710.03760]

**Idea:** Determine  $\lambda(M_S)$  from the condition

$$(M_h^2)_{SM} \equiv \lambda(M_S)v^2 + (\Delta m_h^2)_{SM} \stackrel{!}{=} (M_h^2)_{MSSM}, \quad Q = M_S$$



# FlexibleEFT Higgs – EFT equivalence

**Proof of equivalence:** Start with matching condition:

$$(M_h^2)_{SM} = (M_h^2)_{MSSM} \quad 1L, Q = M_S$$
$$\lambda v^2 + (\Delta m_h^2)_{SM}^{1L} = (M_h^2)_{MSSM}$$

$\Rightarrow$

$$\lambda(M_S) = \frac{1}{v^2} \left[ (M_h^2)_{MSSM} - (\Delta m_h^2)_{SM}^{1L} \right]$$
$$= \frac{1}{v^2} \left[ (m_h^2)_{MSSM} + (\Delta m_h^2)_{MSSM}^{1L} - (\Delta m_h^2)_{SM}^{1L} \right]$$

Now insert  $(m_h^2)_{MSSM}$  and  $(\Delta m_h^2)_{MSSM}^{1L} \dots$

# FlexibleEFT Higgs – EFT equivalence

Inserting  $(m_h^2)_{\text{MSSM}}$  and  $(\Delta m_h^2)_{\text{MSSM}}^{1L}$  (for  $X_t = 0$ ):

$$\lambda(M_S) = \frac{1}{v^2} \left[ \frac{1}{4} (g_Y^2 + g_2^2) v^2 c_{2\beta}^2 + \frac{c_\alpha^2}{s_\beta^2} (\Delta m_h^2)_{\text{SM}}^{1L} - \frac{c_\alpha^2}{s_\beta^2} \frac{12 (y_t^{\text{SM}})^2 m_t^2}{(4\pi)^2} B_0(m_h^2, M_S^2, M_S^2) - (\Delta m_h^2)_{\text{SM}}^{1L} \right]$$

Now go to the decoupling limit  $c_\alpha^2/s_\beta^2 \rightarrow 1 \dots$

# FlexibleEFTHiggs – EFT equivalence

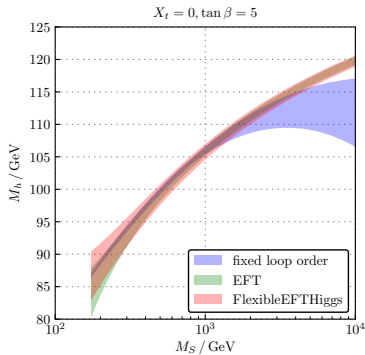
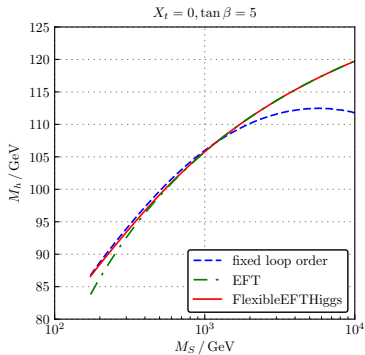
In the decoupling limit  $c_\alpha^2/s_\beta^2 \rightarrow 1$ :

$$\begin{aligned}\lambda(M_S) &= \frac{1}{4}(g_Y^2 + g_2^2)c_{2\beta}^2 - 12 \frac{m_t^2 (y_t^{\text{SM}})^2}{(4\pi)^2 v^2} B_0(m_h^2, M_S^2, M_S^2) \\ &= \frac{1}{4}(g_Y^2 + g_2^2)c_{2\beta}^2 - 12 \frac{m_t^2 (y_t^{\text{SM}})^2}{(4\pi)^2 v^2} \left[ -\log \frac{M_S^2}{Q^2} + \frac{m_h^2}{6M_S^2} + O\left(\frac{m_h^4}{M_S^4}\right) \right] \\ &= \frac{1}{4}(g_Y^2 + g_2^2)c_{2\beta}^2 + 12 \frac{m_t^2 (y_t^{\text{SM}})^2}{(4\pi)^2 v^2} \left[ \log \frac{M_S^2}{Q^2} \right] + O\left(\frac{v^2}{M_S^2}\right) \\ &= \lambda^{\text{EFT,tree}} + \Delta\lambda^{\text{EFT,1L}} + O\left(\frac{v^2}{M_S^2}\right)\end{aligned}$$

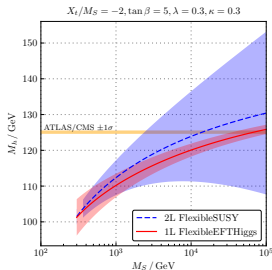
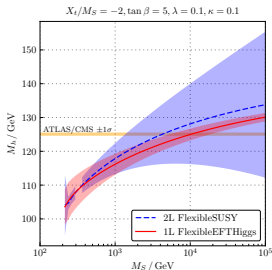
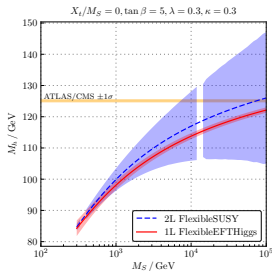
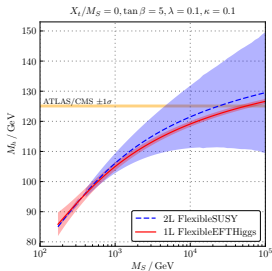
In the decoupling limit  $\lambda(M_S)$  in the FlexibleEFTHiggs approach is equivalent to the EFT approach at 1-loop, up to suppressed terms  $O(v^2/M_S^2)$



# Comparison of the three approaches in the MSSM



# Comparison of the three approaches in the NMSSM



# Summary FlexibleEFTHiggs approach

$$(M_h^2)_{\text{SM}} = (M_h^2)_{\text{MSSM}} \quad \text{at 1L, } Q = M_S$$

## Advantages:

- large logarithms  $\propto \ln(M_S/M_t)$  are resummed to all orders
- all suppressed terms  $O(v^2/M_S^2)$  are incorporated in  $\lambda$

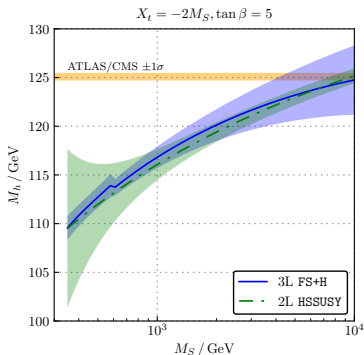
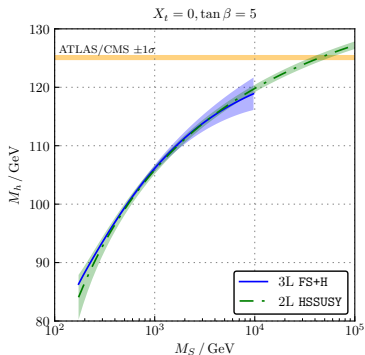
⇒ FlexibleEFTHiggs leads to a correct Higgs mass prediction at the full 1-loop level (including suppressed terms) with additional NLL resummation.

## Disadvantage:

- tricky to extend to 2-loop accuracy (work in progress)

# Current status of high precision calculation in the MSSM

Currently most precise tools: FS+H (3-loop fixed order [1708.05720]), HSSUSY (2-loop EFT [1710.03760]), FeynHiggs (2-loop mixed [1312.4937, 1608.01880, 1706.00346]), SPheno (2-loop\* mixed [1703.03267])



$M_S \lesssim 2 \text{ TeV} \Rightarrow \text{FS+H more accurate than HSSUSY}$

$M_S \gtrsim 2 \text{ TeV} \Rightarrow \text{FS+H less accurate than HSSUSY}$

# Summary

**Supersymmetry** is still viable, but LHC continuously excludes light SUSY scenarios

**Approaches to calculate  $M_h$ :**

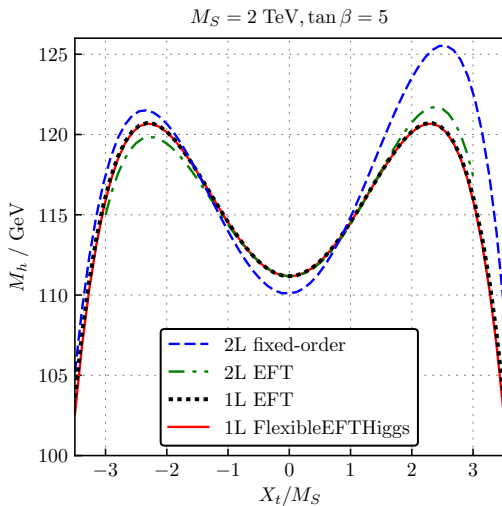
	low $M_S$ $M_S \lesssim 2 \text{ TeV}$	high $M_S$ $M_S \gtrsim 2 \text{ TeV}$
fixed-order	✓	✗
EFT	✗	✓
mixed (FlexibleEFTHiggs)	✓	✓

**FlexibleEFTHiggs:**

- full NLO + NLL resummation
- can be applied to **any** BSM model (SUSY or non-SUSY)
- can be easily automatized
- tricky to extend to 2-loop level (work in progress)

# Backup

# Comparison of the three approaches



# Higgs mass uncertainty estimate

## FS+H:

- $|M_h^{3L}(Q_{\text{pole}} = M_S/2) - M_h^{3L}(Q_{\text{pole}} = 2M_S)|$
- $|M_h^{2L}(\alpha_s^{1L}) - M_h^{2L}(\alpha_s^{2L})|$

## EFT (HSSUSY):

- $|M_h^{2L}(Q_{\text{pole}} = M_t/2) - M_h^{2L}(Q_{\text{pole}} = 2M_t)|$
- $|M_h^{2L}(y_t^{2L}) - M_h^{2L}(y_t^{3L})|$
- $|M_h^{2L}(Q_{\text{match}} = M_S/2) - M_h^{2L}(Q_{\text{match}} = 2M_S)|$
- $|M_h^{2L} - M_h^{2L}(\lambda \rightarrow \lambda(1 + v^2/M_S^2))|$
- $|M_h^{2L}(y_t^{\text{SM}}) - M_h^{2L}(y_t^{\text{MSSM}})|$

## FlexibleEFT Higgs:

- $|M_h^{2L}(Q_{\text{pole}} = M_t/2) - M_h^{2L}(Q_{\text{pole}} = 2M_t)|$
- $|M_h^{2L}(y_t^{2L}) - M_h^{2L}(y_t^{3L})|$
- $|M_h^{2L}(Q_{\text{match}} = M_S/2) - M_h^{2L}(Q_{\text{match}} = 2M_S)|$